Package 'fpc'

December 6, 2020

Title Flexible Procedures for Clustering

Version 2.2-9 **Date** 2020-12-06

Author Christian Hennig <christian.hennig@unibo.it>

Depends R (>= 2.0)

Imports MASS, cluster, mclust, flexmix, prabclus, class, diptest, robustbase, kernlab, grDevices, graphics, methods, stats, utils, parallel

Suggests tclust, pdfCluster, mvtnorm

Description Various methods for clustering and cluster validation.

Fixed point clustering. Linear regression clustering. Clustering by merging Gaussian mixture components. Symmetric and asymmetric discriminant projections for visualisation of the separation of groupings. Cluster validation statistics for distance based clustering including corrected Rand index. Standardisation of cluster validation statistics by random clusterings and comparison between many clustering methods and numbers of clusters based on this.

Cluster-wise cluster stability assessment. Methods for estimation of the number of clusters: Calinski-Harabasz, Tibshirani and Walther's prediction strength, Fang and Wang's bootstrap stability.

Gaussian/multinomial mixture fitting for mixed continuous/categorical variables. Variable-wise statistics for cluster interpretation. DBSCAN clustering. Interface functions for many clustering methods implemented in R, including estimating the number of clusters with kmeans, pam and clara. Modality diagnosis for Gaussian mixtures. For an overview see package?fpc.

Maintainer Christian Hennig <christian.hennig@unibo.it> License GPL

URL https://www.unibo.it/sitoweb/christian.hennig/en/

NeedsCompilation no **Repository** CRAN

Date/Publication 2020-12-06 20:10:02 UTC

R topics documented:

rpc-package	4
adcoord	6
ancoord	8
awcoord	9
batcoord	1
bhattacharyya.dist	3
bhattacharyya.matrix	4
calinhara	5
can	6
cat2bin	
cdbw	
cgrestandard	9
classifdist	
clucols	3
clujaccard	4
clusexpect	5
clustatsum	6
cluster.magazine	
cluster.stats	
cluster.varstats	
clusterbenchstats	
clusterboot	
cmahal	_
con.comp	1
confusion	_
cov.wml	1
cqcluster.stats	
cvnn	
cweight	1
dbscan	
dipp.tantrum	
diptest.multi	
discreoord	
discrete.recode	
discrproj	
distancefactor	
disteritmulti	
dudahart2	
extract.mixturepars	
findrep	
fixmahal	
fixreg	
flexmixedruns	
fpclusters	2

itnumber	
jittervar	
kmeansCBI	95
kmeansruns	100
lcmixed	102
localshape	104
mahalanodisc	105
mahalanofix	106
mahalconf	107
mergenormals	108
mergeparameters	112
minsize	113
mixdens	114
mixpredictive	115
mvdcoord	116
ncoord	117
neginc	
nselectboot	
pamk	
piridge	
	125
	126
	128
	131
randematrix	133
randconf	134
	135
regmix	137
rFace	140
ridgeline	141
ridgeline.diagnosis	142
simmatrix	144
solvecov	
sseg	146
stupidkaven	
stupidkcentroids	147
stupidkfn	148
stupidknn	149
tdecomp	150
tonedata	151
unimodal.ind	152
valstat.object	152
weightplots	155
wfu	156
xtable	157
zmisclassification.matrix	158

4 fpc-package

fpc-package

fpc package overview

Description

Here is a list of the main functions in package fpc. Most other functions are auxiliary functions for these.

Clustering methods

dbscan Computes DBSCAN density based clustering as introduced in Ester et al. (1996).

fixmahal Mahalanobis Fixed Point Clustering, Hennig and Christlieb (2002), Hennig (2005).

fixreg Regression Fixed Point Clustering, Hennig (2003).

flexmixedruns This fits a latent class model to data with mixed type continuous/nominal variables. Actually it calls a method for flexmix.

mergenormals Clustering by merging components of a Gaussian mixture, see Hennig (2010).

regmix ML-fit of a mixture of linear regression models, see DeSarbo and Cron (1988).

Cluster validity indexes and estimation of the number of clusters

cluster.stats This computes several cluster validity statistics from a clustering and a dissimilarity matrix including the Calinski-Harabasz index, the adjusted Rand index and other statistics explained in Gordon (1999) as well as several characterising measures such as average between cluster and within cluster dissimilarity and separation. See also calinhara, dudahart2 for specific indexes, and a new version cqcluster.stats that computes some more indexes and statistics used for computing them. There's also distrsimilarity, which computes within-cluster dissimilarity to the Gaussian and uniform distribution.

prediction.strength Estimates the number of clusters by computing the prediction strength of a clustering of a dataset into different numbers of components for various clustering methods, see Tibshirani and Walther (2005). In fact, this is more flexible than what is in the original paper, because it can use point classification schemes that work better with clustering methods other than k-means.

nselectboot Estimates the number of clusters by bootstrap stability selection, see Fang and Wang (2012). This is quite flexible regarding clustering methods and point classification schemes and also allows for dissimilarity data.

clusterbenchstats This runs many clustering methods (to be specifed by the user) with many numbers of clusters on a dataset and produces standardised and comparable versions of many cluster validity indexes (see Hennig 2019, Akhanli and Hennig 2020). This is done by means of producing random clusterings on the given data, see stupidkcentroids and stupidknn. It allows to compare many clusterings based on many different potential desirable features of a clustering. print.valstat allows to compute an aggregated index with user-specified weights.

fpc-package 5

Cluster visualisation and validation

clucols Sets of colours and symbols useful for cluster plotting.

clusterboot Cluster-wise stability assessment of a clustering. Clusterings are performed on resampled data to see for every cluster of the original dataset how well this is reproduced. See Hennig (2007) for details.

cluster.varstats Extracts variable-wise information for every cluster in order to help with cluster interpretation.

plotcluster Visualisation of a clustering or grouping in data by various linear projection methods that optimise the separation between clusters, or between a single cluster and the rest of the data according to Hennig (2004) including classical methods such as discriminant coordinates. This calls the function discrproj, which is a bit more flexible but doesn't produce a plot itself.

ridgeline.diagnosis Plots and diagnostics for assessing modality of Gaussian mixtures, see Ray and Lindsay (2005).

weightplots Plots to diagnose component separation in Gaussian mixtures, see Hennig (2010).

localshape Local shape matrix, can be used for finding clusters in connection with function ics in package ICS, see Hennig's discussion and rejoinder of Tyler et al. (2009).

Useful wrapper functions for clustering methods

kmeansCBI This and other "CBI"-functions (see the kmeansCBI-help page) are unified wrappers for various clustering methods in R that may be useful because they do in one step for what you normally may need to do a bit more in R (for example fitting a Gaussian mixture with noise component in package mclust).

kmeansruns This calls kmeans for the k-means clustering method and includes estimation of the number of clusters and finding an optimal solution from several starting points.

pamk This calls pam and clara for the partitioning around medoids clustering method (Kaufman and Rouseeuw, 1990) and includes two different ways of estimating the number of clusters.

Author(s)

Christian Hennig <christian.hennig@unibo.it>https://www.unibo.it/sitoweb/christian.hennig/en/

References

Akhanli, S. and Hennig, C. (2020) Calibrating and aggregating cluster validity indexes for context-adapted comparison of clusterings. *Statistics and Computing*, 30, 1523-1544, https://link.springer.com/article/10.1007/s11222-020-09958-2, https://arxiv.org/abs/2002.01822

DeSarbo, W. S. and Cron, W. L. (1988) A maximum likelihood methodology for clusterwise linear regression, *Journal of Classification* 5, 249-282.

Ester, M., Kriegel, H.-P., Sander, J. and Xu, X. (1996). A Density-Based Algorithm for Discovering Clusters in Large Spatial Databases with Noise. *Proceedings of 2nd International Conference on Knowledge Discovery and Data Mining (KDD-96)*.

Fang, Y. and Wang, J. (2012) Selection of the number of clusters via the bootstrap method. *Computational Statistics and Data Analysis*, 56, 468-477.

6 adcoord

Gordon, A. D. (1999) Classification, 2nd ed. Chapman and Hall.

Hennig, C. (2003) Clusters, outliers and regression: fixed point clusters, *Journal of Multivariate Analysis* 86, 183-212.

Hennig, C. (2004) Asymmetric linear dimension reduction for classification. *Journal of Computational and Graphical Statistics*, 13, 930-945.

Hennig, C. (2005) Fuzzy and Crisp Mahalanobis Fixed Point Clusters, in Baier, D., Decker, R., and Schmidt-Thieme, L. (eds.): *Data Analysis and Decision Support*. Springer, Heidelberg, 47-56.

Hennig, C. (2007) Cluster-wise assessment of cluster stability. *Computational Statistics and Data Analysis*, 52, 258-271.

Hennig, C. (2010) Methods for merging Gaussian mixture components, *Advances in Data Analysis and Classification*, 4, 3-34.

Hennig, C. (2019) Cluster validation by measurement of clustering characteristics relevant to the user. In C. H. Skiadas (ed.) *Data Analysis and Applications 1: Clustering and Regression, Modeling-estimating, Forecasting and Data Mining, Volume 2*, Wiley, New York 1-24, https://arxiv.org/abs/1703.09282

Hennig, C. and Christlieb, N. (2002) Validating visual clusters in large datasets: Fixed point clusters of spectral features, *Computational Statistics and Data Analysis* 40, 723-739.

Kaufman, L. and Rousseeuw, P.J. (1990). "Finding Groups in Data: An Introduction to Cluster Analysis". Wiley, New York.

Ray, S. and Lindsay, B. G. (2005) The Topography of Multivariate Normal Mixtures, *Annals of Statistics*, 33, 2042-2065.

Tibshirani, R. and Walther, G. (2005) Cluster Validation by Prediction Strength, *Journal of Computational and Graphical Statistics*, 14, 511-528.

adcoord

Asymmetric discriminant coordinates

Description

Asymmetric discriminant coordinates as defined in Hennig (2003). Asymmetric discriminant projection means that there are two classes, one of which is treated as the homogeneous class (i.e., it should appear homogeneous and separated in the resulting projection) while the other may be heterogeneous. The principle is to maximize the ratio between the projection of a between classes separation matrix and the projection of the covariance matrix within the homogeneous class.

Usage

```
adcoord(xd, clvecd, clnum=1)
```

Arguments

xd the data matrix; a numerical object which can be coerced to a matrix.

clvecd integer vector of class numbers; length must equal nrow(xd).

clnum integer. Number of the homogeneous class.

adcoord 7

Details

The square root of the homogeneous classes covariance matrix is inverted by use of tdecomp, which can be expected to give reasonable results for singular within-class covariance matrices.

Value

List with the following components

ev eigenvalues in descending order.

units columns are coordinates of projection basis vectors. New points x can be pro-

jected onto the projection basis vectors by x %*% units

proj projections of xd onto units.

Author(s)

Christian Hennig <christian.hennig@unibo.it>https://www.unibo.it/sitoweb/christian.hennig/en/

References

Hennig, C. (2004) Asymmetric linear dimension reduction for classification. Journal of Computational and Graphical Statistics 13, 930-945.

Hennig, C. (2005) A method for visual cluster validation. In: Weihs, C. and Gaul, W. (eds.): Classification - The Ubiquitous Challenge. Springer, Heidelberg 2005, 153-160.

See Also

plotcluster for straight forward discriminant plots. discrproj for alternatives. rFace for generation of the example data used below.

Examples

```
set.seed(4634)
face <- rFace(600,dMoNo=2,dNoEy=0)
grface <- as.integer(attr(face,"grouping"))
adcf <- adcoord(face,grface==2)
adcf2 <- adcoord(face,grface==4)
plot(adcf$proj,col=1+(grface==2))
plot(adcf2$proj,col=1+(grface==4))
# ...done in one step by function plotcluster.</pre>
```

8 ancoord

ancoord	Asymmetric neighborhood based discriminant coordinates
ancoord	Asymmetric neighborhood based discriminant coordinates

Description

Asymmetric neighborhood based discriminant coordinates as defined in Hennig (2003). Asymmetric discriminant projection means that there are two classes, one of which is treated as the homogeneous class (i.e., it should appear homogeneous and separated in the resulting projection) while the other may be heterogeneous. The principle is to maximize the ratio between the projection of a between classes covariance matrix, which is defined by averaging the between classes covariance matrices in the neighborhoods of the points of the homogeneous class and the projection of the covariance matrix within the homogeneous class.

Usage

```
ancoord(xd, clvecd, clnum=1, nn=50, method="mcd", countmode=1000, ...)
```

Arguments

xd	the data matrix; a numerical object which can be coerced to a matrix.
clvecd	integer vector of class numbers; length must equal nrow(xd).
clnum	integer. Number of the homogeneous class.
nn	integer. Number of points which belong to the neighborhood of each point (including the point itself).
method	one of "mve", "mcd" or "classical". Covariance matrix used within the homogeneous class. "mcd" and "mve" are robust covariance matrices as implemented in cov.rob. "classical" refers to the classical covariance matrix.
countmode	optional positive integer. Every count mode algorithm runs ancoord shows a message. $ \\$

Details

The square root of the homogeneous classes covariance matrix is inverted by use of tdecomp, which can be expected to give reasonable results for singular within-class covariance matrices.

Value

List with the following components

no effect

ev	eigenvalues in descending order.
units	columns are coordinates of projection basis vectors. New points x can be projected onto the projection basis vectors by x $\%$ units
proi	projections of xd onto units.

awcoord 9

Author(s)

Christian Hennig <christian.hennig@unibo.it>https://www.unibo.it/sitoweb/christian.hennig/en/

References

Hennig, C. (2004) Asymmetric linear dimension reduction for classification. Journal of Computational and Graphical Statistics 13, 930-945.

Hennig, C. (2005) A method for visual cluster validation. In: Weihs, C. and Gaul, W. (eds.): Classification - The Ubiquitous Challenge. Springer, Heidelberg 2005, 153-160.

See Also

plotcluster for straight forward discriminant plots. discrproj for alternatives. rFace for generation of the example data used below.

Examples

```
set.seed(4634)
face <- rFace(600,dMoNo=2,dNoEy=0)
grface <- as.integer(attr(face,"grouping"))
ancf2 <- ancoord(face,grface==4)
plot(ancf2$proj,col=1+(grface==4))
# ...done in one step by function plotcluster.</pre>
```

awcoord

Asymmetric weighted discriminant coordinates

Description

Asymmetric weighted discriminant coordinates as defined in Hennig (2003). Asymmetric discriminant projection means that there are two classes, one of which is treated as the homogeneous class (i.e., it should appear homogeneous and separated in the resulting projection) while the other may be heterogeneous. The principle is to maximize the ratio between the projection of a between classes separation matrix and the projection of the covariance matrix within the homogeneous class. Points are weighted according to their (robust) Mahalanobis distance to the homogeneous class.

Usage

10 awcoord

Arguments

xd the data matrix; a numerical object which can be coerced to a matrix.

clvecd integer vector of class numbers; length must equal nrow(xd).

clnum integer. Number of the homogeneous class.

mahal "md" or "square". If "md", the points are weighted by the square root of the

alpha-quantile of the corresponding chi squared distribution over the roots of their Mahalanobis distance to the homogeneous class, unless this is smaller than 1. If "square" (which is recommended), the (originally squared) Mahalanobis

distance and the unrooted quantile is used.

method one of "mve", "mcd" or "classical". Covariance matrix used within the homoge-

neous class and for the computation of the Mahalanobis distances. "mcd" and "mve" are robust covariance matrices as implemented in cov.rob. "classical"

refers to the classical covariance matrix.

clweight logical. If FALSE, only the points of the heterogeneous class are weighted.

This, together with method="classical", computes AWC as defined in Hennig (2003). If TRUE, all points are weighted. This, together with method="mcd",

computes ARC as defined in Hennig (2003).

alpha numeric between 0 and 1. The corresponding quantile of the chi squared dis-

tribution is used for the downweighting of points. Points with a smaller Maha-

lanobis distance to the homogeneous class get full weight.

subsample integer. If 0, all points are used. Else, only a subsample of subsample of the

points is used.

countmode optional positive integer. Every countmode algorithm runs awcoord shows a

message.

... no effect

Details

The square root of the homogeneous classes covariance matrix is inverted by use of tdecomp, which can be expected to give reasonable results for singular within-class covariance matrices.

Value

List with the following components

ev eigenvalues in descending order.

units columns are coordinates of projection basis vectors. New points x can be pro-

jected onto the projection basis vectors by x %*% units

proj projections of xd onto units.

Author(s)

Christian Hennig <christian.hennig@unibo.it>https://www.unibo.it/sitoweb/christian.hennig/en/

batcoord 11

References

Hennig, C. (2004) Asymmetric linear dimension reduction for classification. Journal of Computational and Graphical Statistics 13, 930-945.

Hennig, C. (2005) A method for visual cluster validation. In: Weihs, C. and Gaul, W. (eds.): Classification - The Ubiquitous Challenge. Springer, Heidelberg 2005, 153-160.

See Also

plotcluster for straight forward discriminant plots. discrproj for alternatives. rFace for generation of the example data used below.

Examples

```
set.seed(4634)
face <- rFace(600,dMoNo=2,dNoEy=0)
grface <- as.integer(attr(face,"grouping"))
awcf <- awcoord(face,grface==1)
# awcf2 <- ancoord(face,grface==1, method="mcd")
plot(awcf$proj,col=1+(grface==1))
# plot(awcf2$proj,col=1+(grface==1))
# ...done in one step by function plotcluster.</pre>
```

batcoord

Bhattacharyya discriminant projection

Description

Computes Bhattacharyya discriminant projection coordinates as described in Fukunaga (1990), p. 455 ff

Usage

```
batcoord(xd, clvecd, clnum=1, dom="mean")
batvarcoord(xd, clvecd, clnum=1)
```

Arguments

xd the data matrix; a numerical object which can be coerced to a matrix.

clvecd integer or logical vector of class numbers; length must equal nrow(xd).

clnum integer, one of the values of clvecd, if this is an integer vector. Bhattacharyya

projections can only be computed if there are only two classes in the dataset. clnum is the number of one of the two classes. All the points indicated by other

values of clvecd are interpreted as the second class.

12 batcoord

dom

string. dom="mean" means that the discriminant coordinate for the group means is computed as the first projection direction by discroord (option pool="equal"; both classes have the same weight for computing the within-class covariance matrix). Then the data is projected into a subspace orthogonal (w.r.t. the within-class covariance) to the discriminant coordinate, and the projection coordinates to maximize the differences in variance are computed.

dom="variance" means that the projection coordinates maximizing the difference in variances are computed. Then they are ordered with respect to the Bhattacharyya distance, which takes also the mean differences into account. Both procedures are implemented as described in Fukunaga (1990).

Details

batvarcoord computes the optimal projection coordinates with respect to the difference in variances. batcoord combines the differences in mean and variance as explained for the argument dom.

Value

batcoord returns a list with the components ev, rev, units, proj. batvarcoord returns a list with the components ev, rev, units, proj, W, S1, S2.

ev	vector of eigenvalues. If dom="mean", then first eigenvalue from discroord. Further eigenvalues are of $S_1^{-1}S_2$, where S_i is the covariance matrix of class i. For batvarcoord or if dom="variance", all eigenvalues come from $S_1^{-1}S_2$ and are ordered by rev.
rev	for batcoord: vector of projected Bhattacharyya distances (Fukunaga (1990), p. 99). Determine quality of the projection coordinates. For batvarcoord: vector of amount of projected difference in variances.
units	columns are coordinates of projection basis vectors. New points x can be projected onto the projection basis vectors by $x \%\%$ units.
proj	projections of xd onto units.
W	matrix $S_1^{-1}S_2$.
S1	covariance matrix of the first class.
S2	covariance matrix of the second class.

Author(s)

Christian Hennig <christian.hennig@unibo.it>https://www.unibo.it/sitoweb/christian.hennig/en/

References

Fukunaga, K. (1990). *Introduction to Statistical Pattern Recognition* (2nd ed.). Boston: Academic Press.

bhattacharyya.dist 13

See Also

```
plotcluster for straight forward discriminant plots.
discrecord for discriminant coordinates.
rFace for generation of the example data used below.
```

Examples

```
set.seed(4634)
face <- rFace(600,dMoNo=2,dNoEy=0)
grface <- as.integer(attr(face,"grouping"))
bcf2 <- batcoord(face,grface==2)
plot(bcf2$proj,col=1+(grface==2))
bcfv2 <- batcoord(face,grface==2,dom="variance")
plot(bcfv2$proj,col=1+(grface==2))
bcfvv2 <- batvarcoord(face,grface==2)
plot(bcfvv2$proj,col=1+(grface==2))</pre>
```

bhattacharyya.dist

Bhattacharyya distance between Gaussian distributions

Description

Computes Bhattacharyya distance between two multivariate Gaussian distributions. See Fukunaga (1990).

Usage

```
bhattacharyya.dist(mu1, mu2, Sigma1, Sigma2)
```

Arguments

mu1	mean vector of component 1.
mu2	mean vector of component 2.
Sigma1	covariance matrix of component 1.
Sigma2	covariance matrix of component 2.

Value

The Bhattacharyya distance between the two Gaussian distributions.

Note

Thanks to David Pinto for improving this function.

Author(s)

```
Christian Hennig <christian.hennig@unibo.it>https://www.unibo.it/sitoweb/christian.hennig/en/
```

14 bhattacharyya.matrix

References

Fukunaga, K. (1990) Introduction to Statistical Pattern Recognition, 2nd edition, Academic Press, New York.

Hennig, C. (2010) Methods for merging Gaussian mixture components, *Advances in Data Analysis and Classification*, 4, 3-34.

Examples

```
round(bhattacharyya.dist(c(1,1),c(2,5),diag(2),diag(2)),digits=2)
```

bhattacharyya.matrix Matrix of pairwise Bhattacharyya distances

Description

Computes Bhattachryya distances for pairs of components given the parameters of a Gaussian mixture.

Usage

Arguments

muarray matrix of component means (different components are in different columns).

Sigmaarray three dimensional array with component covariance matrices (the third dimension refers to components).

ipairs "all" or list of vectors of two integers. If ipairs="all", computations are carried out for all pairs of components. Otherwise, ipairs gives the pairs of components for which computations are carried out.

misclassification.bound

logical. If TRUE, upper bounds for misclassification probabilities exp(-b) are given out instead of the original Bhattacharyya distances b.

Value

A matrix with Bhattacharyya distances (or derived misclassification bounds, see above) between pairs of Gaussian distributions with the provided parameters. If ipairs!="all", the Bhattacharyya distance and the misclassification bound are given as NA for pairs not included in ipairs.

Author(s)

Christian Hennig <christian.hennig@unibo.it>https://www.unibo.it/sitoweb/christian.hennig/en/

calinhara 15

References

Fukunaga, K. (1990) Introduction to Statistical Pattern Recognition, 2nd edition, Academic Press, New York.

Hennig, C. (2010) Methods for merging Gaussian mixture components, *Advances in Data Analysis and Classification*, 4, 3-34.

See Also

bhattacharyya.dist

Examples

```
\label{eq:muarray} $$\operatorname{muarray} <-\operatorname{cbind}(c(0,0),c(0,0.1),c(10,10))$$ sigmaarray <- array(c(\operatorname{diag}(2),\operatorname{diag}(2),\operatorname{diag}(2)),\operatorname{dim}=c(2,2,3))$$ bhattacharyya.matrix(muarray,sigmaarray,ipairs=list(c(1,2),c(2,3)))$$
```

calinhara

Calinski-Harabasz index

Description

Calinski-Harabasz index for estimating the number of clusters, based on an observations/variables-matrix here. A distance based version is available through cluster.stats.

Usage

```
calinhara(x,clustering,cn=max(clustering))
```

Arguments

data matrix or data frame.
 clustering vector of integers. Clustering.
 cn integer. Number of clusters.

Value

Calinski-Harabasz statistic, which is (n-cn)*sum(diag(B))/((cn-1)*sum(diag(W))). B being the between-cluster means, and W being the within-clusters covariance matrix.

Author(s)

Christian Hennig <christian.hennig@unibo.it>https://www.unibo.it/sitoweb/christian.hennig/en

16 can

References

Calinski, T., and Harabasz, J. (1974) A Dendrite Method for Cluster Analysis, *Communications in Statistics*, 3, 1-27.

See Also

```
cluster.stats
```

Examples

```
set.seed(98765)
iriss <- iris[sample(150,20),-5]
km <- kmeans(iriss,3)
round(calinhara(iriss,km$cluster),digits=2)</pre>
```

can

Generation of the tuning constant for regression fixed point clusters

Description

Generates tuning constants ca for fixreg dependent on the number of points and variables of the dataset.

Only thought for use in fixreg.

Usage

```
can(n, p)
```

Arguments

n positive integer. Number of points.

p positive integer. Number of independent variables.

Details

```
The formula is 3+33/(n*2^{-(p-1)/2})^{1/3}+2900000/(n*2^{-(p-1)/2})^3. For justification cf. Hennig (2002).
```

Value

A number.

Author(s)

Christian Hennig <christian.hennig@unibo.it>https://www.unibo.it/sitoweb/christian.hennig/en/

cat2bin 17

References

Hennig, C. (2002) Fixed point clusters for linear regression: computation and comparison, *Journal of Classification* 19, 249-276.

See Also

fixreg

Examples

can(429,3)

cat2bin

Recode nominal variables to binary variables

Description

Recodes a dataset with nominal variables so that the nominal variables are replaced by binary variables for the categories.

Usage

cat2bin(x,categorical=NULL)

Arguments

Х

data matrix or data frame. The data need to be organised case-wise, i.e., if there are categorical variables only, and 15 cases with values c(1,1,2) on the 3 variables, the data matrix needs 15 rows with values 1 1 2. (Categorical variables could take numbers or strings or anything that can be coerced to factor levels as values.)

. .

categorical

vector of numbers of variables to be recoded.

Value

A list with components

data

data matrix with variables specified in categorical replaced by 0-1 variables, one for each category.

variableinfo

list of lists. One list for every variable in the original dataset, with four components each, namely type ("categorical" or "not recoded"), levels (levels of nominal recoded variables in order of binary variable in output dataset), ncat (number of categories for recoded variables), varnum (number of variables in output dataset belonging to this original variable).

18 cdbw

Author(s)

Christian Hennig <christian.hennig@unibo.it>https://www.unibo.it/sitoweb/christian.hennig/en

See Also

```
discrete.recode
```

Examples

```
set.seed(776655)
v1 <- rnorm(20)
v2 <- rnorm(20)
d1 <- sample(1:5,20,replace=TRUE)
d2 <- sample(1:4,20,replace=TRUE)
ldata <-cbind(v1,v2,d1,d2)
lc <- cat2bin(ldata,categorical=3:4)</pre>
```

cdbw

CDbw-index for cluster validation

Description

CDbw-index for cluster validation, as defined in Halkidi and Vazirgiannis (2008), Halkidi et al. (2015).

Usage

Arguments

X	something that can be coerced into a numerical matrix. Euclidean dataset.
clustering	vector of integers with length $=nrow(x)$; indicating the cluster for each observation.
r	integer. Number of cluster border representatives.
S	numerical vector of shrinking factors (between 0 and 1).
clusterstdev	logical. If TRUE, the neighborhood radius for intra-cluster density is the within- cluster estimated squared distance from the mean of the cluster; otherwise it is the average of these over all clusters.
trace	logical. If TRUE, results are printed for the steps to compute the index.

cgrestandard 19

Value

List with components (see Halkidi and Vazirgiannis (2008), Halkidi et al. (2015) for details)

cdbw value of CDbw index (the higher the better).

cohesion cohesion.

compactness compactness.

sep separation.

Author(s)

Christian Hennig <christian.hennig@unibo.it>https://www.unibo.it/sitoweb/christian.hennig/en/

References

Halkidi, M. and Vazirgiannis, M. (2008) A density-based cluster validity approach using multi-representatives. *Pattern Recognition Letters* 29, 773-786.

Halkidi, M., Vazirgiannis, M. and Hennig, C. (2015) Method-independent indices for cluster validation. In C. Hennig, M. Meila, F. Murtagh, R. Rocci (eds.) *Handbook of Cluster Analysis*, CRC Press/Taylor & Francis, Boca Raton.

Examples

```
options(digits=3)
iriss <- as.matrix(iris[c(1:5,51:55,101:105),-5])
irisc <- as.numeric(iris[c(1:5,51:55,101:105),5])
cdbw(iriss,irisc)</pre>
```

cgrestandard

Standardise cluster validation statistics by random clustering results

Description

Standardises cluster validity statistics as produced by clustatsum relative to results that were achieved by random clusterings on the same data by randomclustersim. The aim is to make differences between values comparable between indexes, see Hennig (2019), Akhanli and Hennig (2020).

This is mainly for use within clusterbenchstats.

Usage

20 cgrestandard

Arguments

clusum object of class "valstat", see clusterbenchstats.
clusim list; output object of randomclustersim, see there.
G vector of integers. Numbers of clusters to consider.

percentage logical. If FALSE, standardisation is done to mean zero and standard deviation 1

using the random clusterings. If TRUE, the output is the percentage of simulated values below the result (more precisely, this number plus one divided by the

total plus one).

useallmethods logical. If FALSE, only random clustering results from clusim are used for

standardisation. If TRUE, also clustering results from other methods as given

in clusum are used.

useallg logical. If TRUE, standardisation uses results from all numbers of clusters in G.

If FALSE, standardisation of results for a specific number of cluster only uses

results from that number of clusters.

othernc list of integer vectors of length 2. This allows the incorporation of methods that

bring forth other numbers of clusters than those in G, for example because a method may have automatically estimated a number of clusters. The first number is the number of the clustering method (the order is determined by argument clustermethod in clusterbenchstats), the second number is the number of

clusters. Results specified here are only standardised in useallg=TRUE.

Details

cgrestandard will add a statistic named dmode to the input set of validation statistics, which is defined as 0.75*dindex+0.25*highdgap, aggregating these two closely related statistics, see clustatsum.

Value

List of class "valstat", see valstat.object, with standardised results as explained above.

Author(s)

Christian Hennig <christian.hennig@unibo.it>https://www.unibo.it/sitoweb/christian.hennig/en/

References

Hennig, C. (2019) Cluster validation by measurement of clustering characteristics relevant to the user. In C. H. Skiadas (ed.) *Data Analysis and Applications 1: Clustering and Regression, Modeling-estimating, Forecasting and Data Mining, Volume 2*, Wiley, New York 1-24, https://arxiv.org/abs/1703.09282

Akhanli, S. and Hennig, C. (2020) Calibrating and aggregating cluster validity indexes for context-adapted comparison of clusterings. *Statistics and Computing*, 30, 1523-1544, https://link.springer.com/article/10.1007/s11222-020-09958-2, https://arxiv.org/abs/2002.01822

classifdist 21

See Also

Examples

```
set.seed(20000)
options(digits=3)
face <- rFace(10,dMoNo=2,dNoEy=0,p=2)</pre>
dif <- dist(face)</pre>
clusum <- list()</pre>
clusum[[2]] <- list()</pre>
cl12 <- kmeansCBI(face,2)</pre>
cl13 <- kmeansCBI(face,3)</pre>
cl22 <- claraCBI(face,2)</pre>
cl23 <- claraCBI(face,2)</pre>
ccl12 <- clustatsum(dif,cl12$partition)</pre>
ccl13 <- clustatsum(dif,cl13$partition)</pre>
ccl22 <- clustatsum(dif,cl22$partition)</pre>
ccl23 <- clustatsum(dif,cl23$partition)</pre>
clusum[[1]] <- list()</pre>
clusum[[1]][[2]] <- ccl12</pre>
clusum[[1]][[3]] <- ccl13
clusum[[2]][[2]] <- ccl22
clusum[[2]][[3]] <- ccl23
clusum$maxG <- 3</pre>
clusum$minG <- 2</pre>
clusum$method <- c("kmeansCBI","claraCBI")</pre>
clusum$name <- c("kmeansCBI","claraCBI")</pre>
clusim <- randomclustersim(dist(face),G=2:3,nnruns=1,kmruns=1,</pre>
  fnruns=1, avenruns=1, monitor=FALSE)
cgr <- cgrestandard(clusum,clusim,2:3)</pre>
cgr2 <- cgrestandard(clusum,clusim,2:3,useallg=TRUE)</pre>
cgr3 <- cgrestandard(clusum,clusim,2:3,percentage=TRUE)</pre>
print(str(cgr))
print(str(cgr2))
print(cgr3[[1]][[2]])
```

classifdist

Classification of unclustered points

Description

Various methods for classification of unclustered points from clustered points for use within functions nselectboot and prediction.strength.

22 classifdist

Usage

Arguments

cdist dissimilarity matrix or dist-object. Necessary for classifdist but optional

for classifup and there only used if method="averagedist" (if not provided,

dist is applied to data).

data something that can be coerced into a an n*p-data matrix.

clustering integer vector. Gives the cluster number (between 1 and k for k clusters) for

clustered points and should be -1 for points to be classified.

method one of "averagedist", "centroid", "qda", "knn". See details.

centroids for classifup a k times p matrix of cluster centroids. For classifdist a vector

of numbers of centroid objects as provided by pam. Only used if method="centroid"; in that case mandatory for classifdist but optional for classifnp, where

cluster mean vectors are computed if centroids=NULL.

nnk number of nearest neighbours if method="knn".

Details

classifdist is for data given as dissimilarity matrix, classifnp is for data given as n times p data matrix. The following methods are supported:

- "centroid" assigns observations to the cluster with closest cluster centroid as specified in argument centroids (this is associated to k-means and pam/clara-clustering).
- "qda" only in classifnp. Classifies by quadratic discriminant analysis (this is associated to Gaussian clusters with flexible covariance matrices), calling qda with default settings. If qda gives an error (usually because a class was too small), lda is used.
- "lda" only in classifing. Classifies by linear discriminant analysis (this is associated to Gaussian clusters with equal covariance matrices), calling lda with default settings.
- "averagedist" assigns to the cluster to which an observation has the minimum average dissimilarity to all points in the cluster (this is associated with average linkage clustering).
- "knn" classifies by nnk nearest neighbours (for nnk=1, this is associated with single linkage clustering). Calls knn in classifnp.
- "fn" classifies by the minimum distance to the farthest neighbour. This is associated with complete linkage clustering).

Value

An integer vector giving cluster numbers for all observations; those for the observations already clustered in the input are the same as in the input.

clucols 23

Author(s)

Christian Hennig <christian.hennig@unibo.it>https://www.unibo.it/sitoweb/christian.hennig/en/

See Also

```
prediction.strength, nselectboot
```

Examples

```
set.seed(20000)
x1 <- rnorm(50)
y <- rnorm(100)
x2 <- rnorm(40,mean=20)
x3 <- rnorm(10,mean=25,sd=100)
x <-cbind(c(x1,x2,x3),y)
truec <- c(rep(1,50),rep(2,40),rep(3,10))
topredict <- c(1,2,51,52,91)
clumin <- truec
clumin[topredict] <- -1

classifnp(x,clumin, method="averagedist")
classifdist(dist(x),clumin, centroids=c(3,53,93),method="centroid")
classifdist(dist(x),clumin,method="knn")</pre>
```

clucols

Sets of colours and symbols for cluster plotting

Description

clucols gives out a vector of different random colours. clugrey gives out a vector of equidistant grey scales. clusym is a vector of different symbols starting from "1", "2",...

Usage

```
clucols(i, seed=NULL)
clugrey(i,max=0.9)
clusym
```

Arguments

i integer. Length of output vector (number of clusters).

seed integer. Random seed.

max between 0 and 1. Maximum grey scale value, see grey (close to 1 is bright).

24 clujaccard

Value

clucols gives out a vector of different random colours. clugrey gives out a vector of equidistant grey scales. clusym is a vector of different characters starting from "1", "2",...

Author(s)

Christian Hennig <christian.hennig@unibo.it>https://www.unibo.it/sitoweb/christian.hennig/en

Examples

```
set.seed(112233)
require(MASS)
require(flexmix)
data(Cars93)
Cars934 <- Cars93[,c(3,5,8,10)]
cc <-
    discrete.recode(Cars934,xvarsorted=FALSE,continuous=c(2,3),discrete=c(1,4))
fcc <- flexmix(cc$data~1,k=3,
model=lcmixed(continuous=2,discrete=2,ppdim=c(6,3),diagonal=TRUE))
plot(Cars934[,c(2,3)],col=clucols(3)[fcc@cluster],pch=clusym[fcc@cluster])</pre>
```

clujaccard

Jaccard similarity between logical vectors

Description

Jaccard similarity between logical or 0-1 vectors: sum(c1 & c2)/sum(c1 | c2).

Usage

```
clujaccard(c1,c2,zerobyzero=NA)
```

Arguments

c1 logical or 0-1-vector.

c2 logical or 0-1-vector (same length).

zerobyzero result if sum(c1 | c2)=0.

Value

Numeric between 0 and 1.

Author(s)

Christian Hennig <christian.hennig@unibo.it>https://www.unibo.it/sitoweb/christian.hennig/en/

clusexpect 25

Examples

```
c1 <- rep(TRUE,10)
c2 <- c(FALSE,rep(TRUE,9))
clujaccard(c1,c2)</pre>
```

clusexpect

Expected value of the number of times a fixed point cluster is found

Description

A rough approximation of the expectation of the number of times a well separated fixed point cluster (FPC) of size n is found in ir fixed point iterations of fixreg.

Usage

```
clusexpect(n, p, cn, ir)
```

Arguments

n positive integer. Total number of points.

p positive integer. Number of independent variables.

cn positive integer smaller or equal to n. Size of the FPC.

ir positive integer. Number of fixed point iterations.

Details

The approximation is based on the assumption that a well separated FPC is found iff all p+2 points of the initial coinfiguration come from the FPC. The value is ir times the probability for this. For a discussion of this assumption cf. Hennig (2002).

Value

A number.

Author(s)

Christian Hennig <christian.hennig@unibo.it>https://www.unibo.it/sitoweb/christian.hennig/en/

References

Hennig, C. (2002) Fixed point clusters for linear regression: computation and comparison, *Journal of Classification* 19, 249-276.

See Also

fixreg

26 clustatsum

Examples

```
round(clusexpect(500,4,150,2000),digits=2)
```

clustatsum

Compute and format cluster validation statistics

Description

clustatsum computes cluster validation statistics by running cqcluster.stats, and potentially distrsimilarity, and collecting some key statistics values with a somewhat different nomenclature.

This was implemented as a helper function for use inside of clusterbenchstats and cgrestandard.

Usage

Arguments

datadist	distances on which validation-measures are based, dist object or distance matrix. If NULL, this is computed from datanp; at least one of datadist and datanp must be specified.
clustering	an integer vector of length of the number of cases, which indicates a clustering. The clusters have to be numbered from 1 to the number of clusters.
noisecluster	logical. If TRUE, it is assumed that the largest cluster number in clustering denotes a 'noise class', i.e. points that do not belong to any cluster. These points are not taken into account for the computation of all functions of within and between cluster distances including the validation indexes.
datanp	optional observations times variables data matrix, see npstats.
npstats	logical. If TRUE, distrsimilarity is called and the two statistics computed there are added to the output. These are based on datanp and require datanp to be specified.
useboot	logical. If TRUE, a stability index (either nselectboot or prediction. strength) will be involved.
bootclassif	If useboot=TRUE, a string indicating the classification method to be used with the stability index, see the classification argument of nselectboot and prediction.strength.

clustatsum 27

bootmethod either "nselectboot" or "prediction.strength"; stability index to be used

 $if \ useboot \verb== TRUE.$

bootruns integer. Number of resampling runs. If useboot=TRUE, passed on as B to

nselectboot or M to prediction. strength.

cbmethod CBI-function (see kmeansCBI); clustering method to be used for stability assess-

ment if useboot=TRUE.

methodpars parameters to be passed on to cbmethod.

distmethod logical. In case of useboot=TRUE indicates whether cbmethod will interpret

data as distances.

Value

clustatsum returns a list. The components, as listed below, are outputs of summary.cquality with default parameters, which means that they are partly transformed versions of those given out by cqcluster.stats, i.e., their range is between 0 and 1 and large values are good. Those from distrsimilarity are computed with largeisgood=TRUE, correspondingly.

avewithin average distance within clusters (reweighted so that every observation, rather

than every distance, has the same weight).

mnnd average distance to nnkth nearest neighbour within cluster.

cvnnd coefficient of variation of dissimilarities to nnkth nearest wthin-cluster neigh-

bour, measuring uniformity of within-cluster densities, weighted over all clus-

ters, see Sec. 3.7 of Hennig (2019).

maxdiameter maximum cluster diameter.

widest gap widest within-cluster gap or average of cluster-wise widest within-cluster gap,

depending on parameter averagegap.

sindex separation index, see argument sepindex.

minsep minimum cluster separation.

asw average silhouette width. See silhouette.

dindex this index measures to what extent the density decreases from the cluster mode

to the outskirts; I-densdec in Sec. 3.6 of Hennig (2019); low values are good.

denscut this index measures whether cluster boundaries run through density valleys; I-

densbound in Sec. 3.6 of Hennig (2019); low values are good.

highdgap this measures whether there is a large within-cluster gap with high density on

both sides; I-highdgap in Sec. 3.6 of Hennig (2019); low values are good.

pearsongamma correlation between distances and a 0-1-vector where 0 means same cluster, 1

means different clusters. "Normalized gamma" in Halkidi et al. (2001).

withinss a generalisation of the within clusters sum of squares (k-means objective func-

tion), which is obtained if d is a Euclidean distance matrix. For general distance measures, this is half the sum of the within cluster squared dissimilarities di-

vided by the cluster size.

28 clustatsum

entropy entropy of the distribution of cluster memberships, see Meila(2007).

pame average distance to cluster centroid.

kdnorm Kolmogorov distance between distribution of within-cluster Mahalanobis dis-

tances and appropriate chi-squared distribution, aggregated over clusters (I am

grateful to Agustin Mayo-Iscar for the idea).

kdunif Kolmogorov distance between distribution of distances to nnkth nearest within-

cluster neighbor and appropriate Gamma-distribution, see Byers and Raftery

(1998), aggregated over clusters.

boot if useboot=TRUE, stability value; stabk for method nselectboot; mean.pred

for method prediction.strength.

Author(s)

Christian Hennig <christian.hennig@unibo.it>https://www.unibo.it/sitoweb/christian.hennig/en/

References

Akhanli, S. and Hennig, C. (2020) Calibrating and aggregating cluster validity indexes for context-adapted comparison of clusterings. *Statistics and Computing*, 30, 1523-1544, https://link.springer.com/article/10.1007/s11222-020-09958-2, https://arxiv.org/abs/2002.01822

Halkidi, M., Batistakis, Y., Vazirgiannis, M. (2001) On Clustering Validation Techniques, *Journal of Intelligent Information Systems*, 17, 107-145.

Hennig, C. (2019) Cluster validation by measurement of clustering characteristics relevant to the user. In C. H. Skiadas (ed.) *Data Analysis and Applications 1: Clustering and Regression, Modeling-estimating, Forecasting and Data Mining, Volume 2*, Wiley, New York 1-24, https://arxiv.org/abs/1703.09282

Kaufman, L. and Rousseeuw, P.J. (1990). "Finding Groups in Data: An Introduction to Cluster Analysis". Wiley, New York.

Meila, M. (2007) Comparing clusterings?an information based distance, *Journal of Multivariate Analysis*, 98, 873-895.

See Also

```
cqcluster.stats, distrsimilarity
```

Examples

```
set.seed(20000)
options(digits=3)
face <- rFace(20,dMoNo=2,dNoEy=0,p=2)
dface <- dist(face)
complete3 <- cutree(hclust(dface),3)
clustatsum(dface,complete3)</pre>
```

cluster.magazine 29

cluster.magazine Run many clustering methods on many numbers of clusters	
--	--

Description

Runs a user-specified set of clustering methods (CBI-functions, see kmeansCBI with several numbers of clusters on a dataset with unified output.

Usage

Arguments

data	data matrix or dist-object.	
G	vector of integers. Numbers of clusters to consider.	
diss	logical. If TRUE, the data matrix is assumed to be a distance/dissimilariy matrix, otherwise it's observations times variables.	
scaling	either a logical or a numeric vector of length equal to the number of columns of data. If FALSE, data won't be scaled, otherwise scaling is passed on to scale as argumentscale.	
clustermethod	vector of strings specifying names of CBI-functions (see kmeansCBI). These are the clustering methods to be applied.	
distmethod	vector of logicals, of the same length as clustermethod. TRUE means that the clustering method operates on distances. If diss=TRUE, all entries have to be TRUE. Otherwise, if an entry is true, the corresponding method will be applied on dist(data).	
ncinput	vector of logicals, of the same length as clustermethod. TRUE indicates that the corresponding clustering method requires the number of clusters as input and will not estimate the number of clusters itself.	
clustermethodpars		
	list of the same length as clustermethod. Specifies parameters for all involved clustering methods. Its jth entry is passed to clustermethod number k. Can be an empty entry in case all defaults are used for a clustering method. The number of clusters does not need to be specified here.	
trace	logical. If TRUE, some runtime information is printed.	

30 cluster.magazine

Value

List of lists comprising

output Two-dimensional list. The first list index i is the number of the clustering method

(ordering as specified in clustermethod), the second list index j is the number of clusters. This stores the full output of clustermethod i run on number of

clusters j.

clustering Two-dimensional list. The first list index i is the number of the clustering method

(ordering as specified in clustermethod), the second list index j is the number of clusters. This stores the clustering integer vector (i.e., the partition-component of the CBI-function, see kmeansCBI) of clustermethod i run on num-

ber of clusters j.

noise Two-dimensional list. The first list index i is the number of the clustering method

(ordering as specified in clustermethod), the second list index j is the number of clusters. List entries are single logicals. If TRUE, the clustering method estimated some noise, i.e., points not belonging to any cluster, which in the clustering vector are indicated by the highest number (number of clusters plus one in

case that the number of clusters was fixed).

othernc list of integer vectors of length 2. The first number is the number of the cluster-

ing method (the order is determined by argument clustermethod), the second number is the number of clusters for those methods that estimate the number of clusters themselves and estimate a number that is smaller than min(G) or larger

than max(G).

Author(s)

Christian Hennig <christian.hennig@unibo.it>https://www.unibo.it/sitoweb/christian.hennig/en/

References

Hennig, C. (2017) Cluster validation by measurement of clustering characteristics relevant to the user. In C. H. Skiadas (ed.) *Proceedings of ASMDA 2017*, 501-520, https://arxiv.org/abs/1703.09282

See Also

clusterbenchstats, kmeansCBI

Examples

```
set.seed(20000)
options(digits=3)
face <- rFace(10,dMoNo=2,dNoEy=0,p=2)
clustermethod=c("kmeansCBI","hclustCBI","hclustCBI")
# A clustering method can be used more than once, with different
# parameters
clustermethodpars <- list()</pre>
```

cluster.stats

Cluster validation statistics

Description

Computes a number of distance based statistics, which can be used for cluster validation, comparison between clusterings and decision about the number of clusters: cluster sizes, cluster diameters, average distances within and between clusters, cluster separation, biggest within cluster gap, average silhouette widths, the Calinski and Harabasz index, a Pearson version of Hubert's gamma coefficient, the Dunn index and two indexes to assess the similarity of two clusterings, namely the corrected Rand index and Meila's VI.

Usage

Arguments

d	a distance object (as generated by dist) or a distance matrix between cases.
clustering	an integer vector of length of the number of cases, which indicates a clustering. The clusters have to be numbered from 1 to the number of clusters.
alt.clustering	an integer vector such as for clustering, indicating an alternative clustering. If provided, the corrected Rand index and Meila's VI for clustering vs. alt.clustering are computed.
noisecluster	logical. If TRUE, it is assumed that the largest cluster number in clustering denotes a 'noise class', i.e. points that do not belong to any cluster. These points are not taken into account for the computation of all functions of within and between cluster distances including the validation indexes.
silhouette	logical. If TRUE, the silhouette statistics are computed, which requires package cluster.
G2	logical. If TRUE, Goodman and Kruskal's index G2 (cf. Gordon (1999), p. 62) is computed. This executes lots of sorting algorithms and can be very slow (it has been improved by R. Francois - thanks!)

G3 logical. If TRUE, the index G3 (cf. Gordon (1999), p. 62) is computed. This

executes sort on all distances and can be extremely slow.

wgap logical. If TRUE, the widest within-cluster gaps (largest link in within-cluster

minimum spanning tree) are computed. This is used for finding a good number

of clusters in Hennig (2013).

sepindex logical. If TRUE, a separation index is computed, defined based on the distances

for every point to the closest point not in the same cluster. The separation index is then the mean of the smallest proportion sepprob of these. This allows to formalise separation less sensitive to a single or a few ambiguous points. The output component corresponding to this is sindex, not separation! This is

used for finding a good number of clusters in Hennig (2013).

sepprob numerical between 0 and 1, see sepindex.

sepwithnoise logical. If TRUE and sepindex and noisecluster are both TRUE, the noise

points are incorporated as cluster in the separation index (sepindex) computation. Also they are taken into account for the computation for the minimum

cluster separation.

compareonly logical. If TRUE, only the corrected Rand index and Meila's VI are computed

and given out (this requires alt.clustering to be specified).

aggregateonly logical. If TRUE (and not compareonly), no clusterwise but only aggregated

information is given out (this cuts the size of the output down a bit).

Value

cluster.stats returns a list containing the components n, cluster.number, cluster.size, min.cluster.size, noisen, except if compareonly=TRUE, in which case only the last two components are computed.

n number of cases.

cluster.number number of clusters.

cluster.size vector of cluster sizes (number of points).

min.cluster.size

size of smallest cluster.

noisen number of noise points, see argument noisecluster (noisen=0 if noisecluster=FALSE).

diameter vector of cluster diameters (maximum within cluster distances).

average.distance

vector of clusterwise within cluster average distances.

median.distance

vector of clusterwise within cluster distance medians.

separation vector of clusterwise minimum distances of a point in the cluster to a point of

another cluster.

average.toother

vector of clusterwise average distances of a point in the cluster to the points of

other clusters.

separation.matrix

matrix of separation values between all pairs of clusters.

ave.between.matrix

matrix of mean dissimilarities between points of every pair of clusters.

average.between

average distance between clusters.

average within average distance within clusters (reweighted so that every observation, rather

than every distance, has the same weight).

n.between number of distances between clusters.
n.within number of distances within clusters.

max.diameter maximum cluster diameter.
min.separation minimum cluster separation.

within.cluster.ss

a generalisation of the within clusters sum of squares (k-means objective function), which is obtained if d is a Euclidean distance matrix. For general distance measures, this is half the sum of the within cluster squared dissimilarities divided by the cluster size.

clus.avg.silwidths

vector of cluster average silhouette widths. See silhouette.

avg.silwidth average silhouette width. See silhouette.

g2 Goodman and Kruskal's Gamma coefficient. See Milligan and Cooper (1985),

Gordon (1999, p. 62).

g3 G3 coefficient. See Gordon (1999, p. 62).

pearsongamma correlation between distances and a 0-1-vector where 0 means same cluster, 1

means different clusters. "Normalized gamma" in Halkidi et al. (2001).

dunn minimum separation / maximum diameter. Dunn index, see Halkidi et al. (2002).

dunn2 minimum average dissimilarity between two cluster / maximum average within

cluster dissimilarity, another version of the family of Dunn indexes.

entropy entropy of the distribution of cluster memberships, see Meila(2007).

wb.ratio average.within/average.between.

ch Calinski and Harabasz index (Calinski and Harabasz 1974, optimal in Milligan

and Cooper 1985; generalised for dissimilarities in Hennig and Liao 2013).

cwidegap vector of widest within-cluster gaps.

widestgap widest within-cluster gap.

sindex separation index, see argument sepindex.

corrected.rand corrected Rand index (if alt.clustering has been specified), see Gordon (1999,

p. 198).

vi variation of information (VI) index (if alt.clustering has been specified), see

Meila (2007).

Note

Because cluster.stats processes a full dissimilarity matrix, it isn't suitable for large data sets. You may consider distcritmulti in that case.

Author(s)

Christian Hennig <christian.hennig@unibo.it>https://www.unibo.it/sitoweb/christian.hennig/en/

References

Calinski, T., and Harabasz, J. (1974) A Dendrite Method for Cluster Analysis, *Communications in Statistics*, 3, 1-27.

Gordon, A. D. (1999) Classification, 2nd ed. Chapman and Hall.

Halkidi, M., Batistakis, Y., Vazirgiannis, M. (2001) On Clustering Validation Techniques, *Journal of Intelligent Information Systems*, 17, 107-145.

Hennig, C. and Liao, T. (2013) How to find an appropriate clustering for mixed-type variables with application to socio-economic stratification, *Journal of the Royal Statistical Society, Series C Applied Statistics*, 62, 309-369.

Hennig, C. (2013) How many bee species? A case study in determining the number of clusters. In: Spiliopoulou, L. Schmidt-Thieme, R. Janning (eds.): "Data Analysis, Machine Learning and Knowledge Discovery", Springer, Berlin, 41-49.

Kaufman, L. and Rousseeuw, P.J. (1990). "Finding Groups in Data: An Introduction to Cluster Analysis". Wiley, New York.

Meila, M. (2007) Comparing clusterings?an information based distance, *Journal of Multivariate Analysis*, 98, 873-895.

Milligan, G. W. and Cooper, M. C. (1985) An examination of procedures for determining the number of clusters. *Psychometrika*, 50, 159-179.

See Also

cqcluster.stats is a more sophisticated version of cluster.stats with more options. silhouette, dist, calinhara, distcritmulti. clusterboot computes clusterwise stability statistics by resampling.

Examples

cluster.varstats 35

Description

This function gives some helpful variable-wise information for cluster interpretation, given a clustering and a data set. The output object contains some tables. For categorical variables, tables compare clusterwise distributions with overall distributions. Continuous variables are categorised for this.

If desired, tables, histograms, some standard statistics of continuous variables and validation plots as available through discrproj (Hennig 2004) are given out on the fly.

Usage

Arguments

clustering	vector of integers. Clustering (needs to be in standard coding, 1,2,).
vardata	data matrix or data frame of which variables are summarised.
contdata	variable matrix or data frame, normally all or some variables from vardata, on which cluster visualisation by projection methods is performed unless projmethod="none". It should make sense to interpret these variables in a quantitative (intervalscaled) way.
clusterwise	logical. If FALSE, only the output tables are computed but no more detail and graphs are given on the fly.
tablevar	vector of integers. Numbers of variables treated as categorical (i.e., no histograms and statistics, just tables) if clusterwise=TRUE. Note that an error will be produced by factor type variables unless they are declared as categorical here.
catvar	vector of integers. Numbers of variables to be categorised by proportional quantiles for table computation. Recommended for all continuous variables.
quantvar	vector of integers. Variables for which means, standard deviations and quantiles should be given out if clusterwise=TRUE.
catvarcats	integer. Number of categories used for categorisation of variables specified in quantvar.

36 cluster.varstats

proportions	logical. If TRUE, output tables contain proportions, otherwise numbers of observations.
projmethod	one of "none", "dc", "bc", "vbc", "mvdc", "adc", "awc" (recommended if not "none"), "arc", "nc", "wnc", "anc". Cluster validation projection method introduced in Hennig (2004), passed on as method argument in discrproj.
minsize	integer. Projection is not carried out for clusters with fewer points than this. (If this is chosen smaller, it may lead to errors with some projection methods.)
ask	logical. If TRUE, par(ask=TRUE) is set in the beginning to prompt the user before plots and par(ask=FALSE) in the end.
rangefactor	numeric. Factor by which to multiply the range for projection plot ranges.
x	an object of class "varwisetables", output object of cluster.varstats.
digits	integer. Number of digits after the decimal point to print out.
	not used.

Value

An object of class "varwisetables", which is a list with a table for each variable, giving (categorised) marginal distributions by cluster.

Author(s)

Christian Hennig <christian.hennig@unibo.it>https://www.unibo.it/sitoweb/christian.hennig/en

References

Hennig, C. (2004) Asymmetric linear dimension reduction for classification. Journal of Computational and Graphical Statistics 13, 930-945.

Examples

```
set.seed(112233)
options(digits=3)
require(MASS)
require(flexmix)
data(Cars93)
Cars934 <- Cars93[,c(3,5,8,10)]
cc <-
    discrete.recode(Cars934,xvarsorted=FALSE,continuous=c(2,3),discrete=c(1,4))
fcc <- flexmix(cc$data~1,k=2,
model=lcmixed(continuous=2,discrete=2,ppdim=c(6,3),diagonal=TRUE))
cv <-
    cluster.varstats(fcc@cluster,Cars934, contdata=Cars934[,c(2,3)],
    tablevar=c(1,4),catvar=c(2,3),quantvar=c(2,3),projmethod="awc",
    ask=FALSE)
print(cv)</pre>
```

clusterbenchstats

Run and validate many clusterings

Description

This runs the methodology explained in Hennig (2019), Akhanli and Hennig (2020). It runs a user-specified set of clustering methods (CBI-functions, see kmeansCBI) with several numbers of clusters on a dataset, and computes many cluster validation indexes. In order to explore the variation of these indexes, random clusterings on the data are generated, and validation indexes are standardised by use of the random clusterings in order to make them comparable and differences between values interpretable.

The function print.valstat can be used to provide weights for the cluster validation statistics, and will then compute a weighted validation index that can be used to compare all clusterings.

See the examples for how to get the indexes A1 and A2 from Akhanli and Hennig (2020).

Usage

```
clusterbenchstats(data, G, diss = inherits(data, "dist"),
                                   scaling=TRUE, clustermethod,
                                   methodnames=clustermethod,
                               distmethod=rep(TRUE,length(clustermethod)),
                               ncinput=rep(TRUE,length(clustermethod)),
                               clustermethodpars,
                               npstats=FALSE,
                               useboot=FALSE,
                               bootclassif=NULL,
                               bootmethod="nselectboot",
                               bootruns=25,
                               trace=TRUE,
                               pamcrit=TRUE,snnk=2,
                               dnnk=2,
                               nnruns=100, kmruns=100, fnruns=100, avenruns=100,
                               multicore=FALSE,cores=detectCores()-1,
                               useallmethods=TRUE,
                               useallg=FALSE,...)
## S3 method for class 'clusterbenchstats'
print(x,...)
```

Arguments

data	data matrix or dist-object.
G	vector of integers. Numbers of clusters to consider.
diss	logical. If TRUE, the data matrix is assumed to be a distance/dissimilariy matrix,
	otherwise it's observations times variables.

scaling either a logical or a numeric vector of length equal to the number of columns of

data. If FALSE, data won't be scaled, otherwise scaling is passed on to scale

as argumentscale.

clustermethod vector of strings specifying names of CBI-functions (see kmeansCBI). These are

the clustering methods to be applied.

methodnames vector of strings with user-chosen names for clustering methods, one for every

method in clustermethod. These can be used to distinguish different methods run by the same CBI-function but with different parameter values such as

complete and average linkage for hclustCBI.

distmethod vector of logicals, of the same length as clustermethod. TRUE means that the

clustering method operates on distances. If diss=TRUE, all entries have to be TRUE. Otherwise, if an entry is true, the corresponding method will be applied

on dist(data).

ncinput vector of logicals, of the same length as clustermethod. TRUE indicates that

the corresponding clustering method requires the number of clusters as input and will not estimate the number of clusters itself. Only methods for which this

is TRUE can be used with useboot=TRUE.

clustermethodpars

list of the same length as clustermethod. Specifies parameters for all involved clustering methods. Its jth entry is passed to clustermethod number k. Can be an empty entry in case all defaults are used for a clustering method. However, the last entry is not allowed to be empty (you may just set a parameter of the last clustering method to its default value if you don't want to specify anything

else)! The number of clusters does not need to be specified here.

npstats logical. If TRUE, distrsimilarity is called and the two validity statistics com-

puted there are added. These require diss=FALSE.

useboot logical. If TRUE, a stability index (either nselectboot or prediction. strength)

will be involved.

bootclassif If useboot=TRUE, a vector of strings indicating the classification methods to be

used with the stability index for the different methods indicated in clustermethods, see the classification argument of nselectboot and prediction.strength.

bootmethod either "nselectboot" or "prediction.strength"; stability index to be used

if useboot=TRUE.

bootruns integer. Number of resampling runs. If useboot=TRUE, passed on as B to

nselectboot or M to prediction.strength. Note that these are applied to all kmruns+nnruns+avenruns+fnruns random clusterings on top of the regular ones, which may take a lot of time if bootruns and these values are chosen

large.

trace logical. If TRUE, some runtime information is printed.

pamcrit logical. If TRUE, the average distance of points to their respective cluster cen-

troids is computed (criterion of the PAM clustering method, validation criterion pamc); centroids are chosen so that they minimise this criterion for the given

clustering. Passed on to cqcluster.stats.

snnk integer. Number of neighbours used in coefficient of variation of distance to

nearest within cluster neighbour, the cvnnd-statistic (clusters with snnk or fewer points are ignored for this). Passed on to cqcluster.stats as argument nnk.

dnnk	integer. Number of nearest neighbors to use for dissimilarity to the uniform in case that npstats=TRUE; nnk-argument to be passed on to distrsimilarity.
nnruns	integer. Number of runs of stupidknn (random clusterings). With useboot=TRUE one may want to choose this lower than the default for reasons of computation time.
kmruns	integer. Number of runs of stupidkcentroids (random clusterings). With useboot=TRUE one may want to choose this lower than the default for reasons of computation time.
fnruns	integer. Number of runs of stupidkfn (random clusterings). With useboot=TRUE one may want to choose this lower than the default for reasons of computation time.
avenruns	integer. Number of runs of stupidkaven (random clusterings). With useboot=TRUE one may want to choose this lower than the default for reasons of computation time.
multicore	logical. If TRUE, parallel computing is used through the function mclapply from package parallel; read warnings there if you intend to use this; it won't work on Windows.
cores	integer. Number of cores for parallelisation.
useallmethods	logical, to be passed on to cgrestandard. If FALSE, only random clustering results are used for standardisation. If TRUE, clustering results from all methods are used.
useallg	logical to be passed on to cgrestandard. If TRUE, standardisation uses results from all numbers of clusters in G. If FALSE, standardisation of results for a specific number of cluster only uses results from that number of clusters.
• • •	further arguments to be passed on to cqcluster.stats through clustatsum (no effect in print.clusterbenchstats).
X	object of class "clusterbenchstats".

Value

The output of clusterbenchstats is a big list of lists comprising lists cm, stat, sim, qstat, sstat

CM	output object of cluster.magazine, see there for details. Clustering of all
	methods and numbers of clusters on the dataset data.

stat	object of class	"valstat", see	valstat.object	for details.	Unstandardised
	3	,	•		

cluster validation statistics.

sim output object of randomclustersim, see there. validity indexes from random

clusterings used for standardisation of validation statistics on data.

qstat object of class "valstat", see valstat.object for details. Cluster validation

statistics standardised by random clusterings, output of cgrestandard based on

percentages, i.e., with percentage=TRUE.

sstat object of class "valstat", see valstat.object for details. Cluster validation

statistics standardised by random clusterings, output of cgrestandard based on mean and standard deviation (called Z-score standardisation in Akhanli and

Hennig (2020), i.e., with percentage=FALSE.

Note

This may require a lot of computing time and also memory for datasets that are not small, as most indexes require computation and storage of distances.

Author(s)

Christian Hennig <christian.hennig@unibo.it>https://www.unibo.it/sitoweb/christian.hennig/en/

References

Hennig, C. (2019) Cluster validation by measurement of clustering characteristics relevant to the user. In C. H. Skiadas (ed.) *Data Analysis and Applications 1: Clustering and Regression, Modeling-estimating, Forecasting and Data Mining, Volume 2*, Wiley, New York 1-24, https://arxiv.org/abs/1703.09282

Akhanli, S. and Hennig, C. (2020) Calibrating and aggregating cluster validity indexes for context-adapted comparison of clusterings. *Statistics and Computing*, 30, 1523-1544, https://link.springer.com/article/10.1007/s11222-020-09958-2, https://arxiv.org/abs/2002.01822

See Also

valstat.object.cluster.magazine,kmeansCBI.cqcluster.stats,clustatsum,cgrestandard

Examples

```
set.seed(20000)
 options(digits=3)
 face <- rFace(10,dMoNo=2,dNoEy=0.p=2)</pre>
 clustermethod=c("kmeansCBI", "hclustCBI")
# A clustering method can be used more than once, with different
# parameters
 clustermethodpars <- list()</pre>
 clustermethodpars[[2]] <- list()</pre>
 clustermethodpars[[2]]$method <- "average"</pre>
# Last element of clustermethodpars needs to have an entry!
 methodname <- c("kmeans", "average")</pre>
 cbs <- clusterbenchstats(face,G=2:3,clustermethod=clustermethod,</pre>
   methodname=methodname, distmethod=rep(FALSE, 2),
   clustermethodpars=clustermethodpars,nnruns=1,kmruns=1,fnruns=1,avenruns=1)
 print(cbs)
 print(cbs$qstat,aggregate=TRUE,weights=c(1,0,0,0,0,1,0,1,0,1,0,1,0,0,1,1))
# The weights are weights for the validation statistics ordered as in
# cbs$qstat$statistics for computation of an aggregated index, see
# ?print.valstat.
# Now using bootstrap stability assessment as in Akhanli and Hennig (2020):
 bootclassif <- c("centroid", "averagedist")</pre>
 cbsboot <- clusterbenchstats(face,G=2:3,clustermethod=clustermethod,</pre>
   methodname=methodname, distmethod=rep(FALSE, 2),
   clustermethodpars=clustermethodpars,
```

```
useboot=TRUE,bootclassif=bootclassif,bootmethod="nselectboot",
   bootruns=2,nnruns=1,kmruns=1,fnruns=1,avenruns=1,useallg=TRUE)
   print(cbsboot)
## Not run:
# Index A1 in Akhanli and Hennig (2020) (need these weights choices):
   print(cbsboot$sstat,aggregate=TRUE,weights=c(1,0,0,0,0,0,0,0,0,0,0,0,0,0,0,1,0))
# Index A2 in Akhanli and Hennig (2020) (need these weights choices):
   print(cbsboot$sstat,aggregate=TRUE,weights=c(0,0,0,0,1,1,0,0,0,0,0,0,0,0,1,0))
## End(Not run)
# Results from nselectboot:
   plot(cbsboot$stat,cbsboot$sim,statistic="boot")
```

clusterboot

Clusterwise cluster stability assessment by resampling

Description

Assessment of the clusterwise stability of a clustering of data, which can be cases*variables or dissimilarity data. The data is resampled using several schemes (bootstrap, subsetting, jittering, replacement of points by noise) and the Jaccard similarities of the original clusters to the most similar clusters in the resampled data are computed. The mean over these similarities is used as an index of the stability of a cluster (other statistics can be computed as well). The methods are described in Hennig (2007).

clusterboot is an integrated function that computes the clustering as well, using interface functions for various clustering methods implemented in R (several interface functions are provided, but you can implement further ones for your favourite clustering method). See the documentation of the input parameter clustermethod below.

Quite general clustering methods are possible, i.e. methods estimating or fixing the number of clusters, methods producing overlapping clusters or not assigning all cases to clusters (but declaring them as "noise"). Fuzzy clusterings cannot be processed and have to be transformed to crisp clusterings by the interface function.

Usage

```
print(x,statistics=c("mean","dissolution","recovery"),...)
## S3 method for class 'clboot'
plot(x,xlim=c(0,1),breaks=seq(0,1,by=0.05),...)
```

Arguments

data

by default something that can be coerced into a (numerical) matrix (data frames with non-numerical data are allowed when using datatomatrix=FALSE, see below). The data matrix - either an n*p-data matrix (or data frame) or an n*ndissimilarity matrix (or dist-object).

В

integer. Number of resampling runs for each scheme, see bootmethod.

distances

logical. If TRUE, the data is interpreted as dissimilarity matrix. If data is a dist-object, distances=TRUE automatically, otherwise distances=FALSE by default. This means that you have to set it to TRUE manually if data is a dissimilarity matrix.

bootmethod

vector of strings, defining the methods used for resampling. Possible methods:

"boot": nonparametric bootstrap (precise behaviour is controlled by parameters bscompare and multipleboot).

"subset": selecting random subsets from the dataset. Size determined by subtuning.

"noise": replacing a certain percentage of the points by random noise, see noisetuning.

"jitter" add random noise to all points, see jittertuning. (This didn't perform well in Hennig (2007), but you may want to get your own experience.)

"bojit" nonparametric bootstrap first, and then adding noise to the points, see jittertuning.

Important: only the methods "boot" and "subset" work with dissimilarity data, or if datatomatrix=FALSE!

The results in Hennig (2007) indicate that "boot" is generally informative and often quite similar to "subset" and "bojit", while "noise" sometimes provides different information. Therefore the default (for distances=FALSE) is to use "boot" and "noise". However, some clustering methods may have problems with multiple points, which can be solved by using "bojit" or "subset" instead of "boot" or by multipleboot=FALSE below.

logical. If TRUE, multiple points in the bootstrap sample are taken into account to compute the Jaccard similarity to the original clusters (which are represented by their "bootstrap versions", i.e., the points of the original cluster which also occur in the bootstrap sample). If a point was drawn more than once, it is in the "bootstrap version" of the original cluster more than once, too, if bscompare=TRUE. Otherwise multiple points are ignored for the computation of the Jaccard similarities. If multipleboot=FALSE, it doesn't make a difference.

multipleboot

logical. If FALSE, all points drawn more than once in the bootstrap draw are only used once in the bootstrap samples.

jittertuning

positive numeric. Tuning for the "jitter"-method. The noise distribution for jittering is a normal distribution with zero mean. The covariance matrix has the

bscompare

same Eigenvectors as that of the original data set, but the standard deviation along the principal directions is determined by the jittertuning-quantile of the distances between neighboring points projected along these directions.

noisetuning

A vector of two positive numerics. Tuning for the "noise"-method. The first component determines the probability that a point is replaced by noise. Noise is generated by a uniform distribution on a hyperrectangle along the principal directions of the original data set, ranging from -noisetuning[2] to noisetuning[2] times the standard deviation of the data set along the respective direction. Note that only points not replaced by noise are considered for the computation of Jaccard similarities.

subtuning

integer. Size of subsets for "subset".

clustermethod

an interface function (the function name, not a string containing the name, has to be provided!). This defines the clustering method. See the "Details"-section for a list of available interface functions and guidelines how to write your own ones.

noisemethod

logical. If TRUE, the last cluster is regarded as "noise cluster", which means that for computing the Jaccard similarity, it is not treated as a cluster. The noise cluster of the original clustering is only compared with the noise cluster of the clustering of the resampled data. This means that in the clusterboot-output (and plot), if points were assigned to the noise cluster, the last cluster number refers to it, and its Jaccard similarity values refer to comparisons with estimated noise components in resampled datasets only. (Some cluster methods such as tclust and mclustBIC produce such noise components.)

count

logical. If TRUE, the resampling runs are counted on the screen.

showplots

logical. If TRUE, a plot of the first two dimensions of the resampled data set (or the classical MDS solution for dissimilarity data) is shown for every resampling run. The last plot shows the original data set. Ignored if datatomatrix=FALSE.

dissolution

numeric between 0 and 1. If the Jaccard similarity between the resampling version of the original cluster and the most similar cluster on the resampled data is smaller or equal to this value, the cluster is considered as "dissolved". Numbers of dissolved clusters are recorded.

recover

numeric between 0 and 1. If the Jaccard similarity between the resampling version of the original cluster and the most similar cluster on the resampled data is larger than this value, the cluster is considered as "successfully recovered". Numbers of recovered clusters are recorded.

seed

integer. Seed for random generator (fed into set.seed) to make results reproducible. If NULL, results depend on chance.

datatomatrix

logical. If TRUE, data is coerced into a (numerical) matrix at the start of clusterboot. FALSE may be chosen for mixed type data including e.g. categorical factors (assuming that the chosen clustermethod allows for this). This disables some features of clusterboot, see parameters bootmethod and showplots.

. . .

additional parameters for the clustermethods called by clusterboot. No effect in print.clboot and plot.clboot.

Χ

object of class clboot.

statistics specifies in print.clboot, which of the three clusterwise Jaccard similarity

statistics "mean", "dissolution" (number of times the cluster has been dissolved) and "recovery" (number of times a cluster has been successfully re-

covered) is printed.

xlim transferred to hist. breaks transferred to hist.

Details

Here are some guidelines for interpretation. There is some theoretical justification to consider a Jaccard similarity value smaller or equal to 0.5 as an indication of a "dissolved cluster", see Hennig (2008). Generally, a valid, stable cluster should yield a mean Jaccard similarity value of 0.75 or more. Between 0.6 and 0.75, clusters may be considered as indicating patterns in the data, but which points exactly should belong to these clusters is highly doubtful. Below average Jaccard values of 0.6, clusters should not be trusted. "Highly stable" clusters should yield average Jaccard similarities of 0.85 and above. All of this refers to bootstrap; for the other resampling schemes it depends on the tuning constants, though their default values should grant similar interpretations in most cases.

While B=100 is recommended, smaller run numbers could give quite informative results as well, if computation times become too high.

Note that the stability of a cluster is assessed, but stability is not the only important validity criterion - clusters obtained by very inflexible clustering methods may be stable but not valid, as discussed in Hennig (2007). See plotcluster for graphical cluster validation.

Information about interface functions for clustering methods:

The following interface functions are currently implemented (in the present package; note that almost all of these functions require the specification of some control parameters, so if you use one of them, look up their common help page kmeansCBI) first:

- **kmeansCBI** an interface to the function kmeans for k-means clustering. This assumes a cases*variables matrix as input.
- **hclustCBI** an interface to the function hclust for agglomerative hierarchical clustering with optional noise cluster. This function produces a partition and assumes a cases*variables matrix as input.
- hclusttreeCBI an interface to the function hclust for agglomerative hierarchical clustering. This function produces a tree (not only a partition; therefore the number of clusters can be huge!) and assumes a cases*variables matrix as input.
- **disthclustCBI** an interface to the function hclust for agglomerative hierarchical clustering with optional noise cluster. This function produces a partition and assumes a dissimilarity matrix as input.
- **noisemclustCBI** an interface to the function mclustBIC for normal mixture model based clustering. This assumes a cases*variables matrix as input. Warning: mclustBIC sometimes has problems with multiple points. It is recommended to use this only together with multipleboot=FALSE.
- distnoisemclustCBI an interface to the function mclustBIC for normal mixture model based clustering. This assumes a dissimilarity matrix as input and generates a data matrix by multidimensional scaling first. Warning: mclustBIC sometimes has problems with multiple points. It is recommended to use this only together with multipleboot=FALSE.

claraCBI an interface to the functions pam and clara for partitioning around medoids. This can be used with cases*variables as well as dissimilarity matrices as input.

- pamkCBI an interface to the function pamk for partitioning around medoids. The number of cluster is estimated by the average silhouette width. This can be used with cases*variables as well as dissimilarity matrices as input.
- **tclustCBI** an interface to the function tclust in the tclust library for trimmed Gaussian clustering. This assumes a cases*variables matrix as input. Note that this function is not currently provided because the tclust package is only available in the CRAN archives, but the code is in the Examples-section of the kmeansCBI-help page.
- **dbscanCBI** an interface to the function dbscan for density based clustering. This can be used with cases*variables as well as dissimilarity matrices as input..
- **mahalCBI** an interface to the function fixmahal for fixed point clustering. This assumes a cases*variables matrix as input.
- **mergenormCBI** an interface to the function mergenormals for clustering by merging Gaussian mixture components.
- **speccCBI** an interface to the function specc for spectral clustering.

You can write your own interface function. The first argument of an interface function should preferably be a data matrix (of class "matrix", but it may be a symmetrical dissimilarity matrix). It can be a data frame, but this restricts some of the functionality of clusterboot, see above. Further arguments can be tuning constants for the clustering method. The output of an interface function should be a list containing (at least) the following components:

- **result** clustering result, usually a list with the full output of the clustering method (the precise format doesn't matter); whatever you want to use later.
- nc number of clusters. If some points don't belong to any cluster but are declared as "noise", nc includes the noise cluster, and there should be another component nccl, being the number of clusters not including the noise cluster (note that it is not mandatory to define a noise component if not all points are assigned to clusters, but if you do it, the stability of the noise cluster is assessed as well.)
- **clusterlist** this is a list consisting of a logical vectors of length of the number of data points (n) for each cluster, indicating whether a point is a member of this cluster (TRUE) or not. If a noise cluster is included, it should always be the last vector in this list.
- partition an integer vector of length n, partitioning the data. If the method produces a partition, it should be the clustering. This component is only used for plots, so you could do something like rep(1,n) for non-partitioning methods. If a noise cluster is included, nc=nccl+1 and the noise cluster is cluster no. nc.

clustermethod a string indicating the clustering method.

Value

clusterboot returns an object of class "clboot", which is a list with components result, partition, nc, clustermethod,

result clustering result; full output of the selected clustermethod for the original data

set.

partition parameter of the selected clustermethod (note that this is only mean-

ingful for partitioning clustering methods).

number of clusters in original data (including noise component if noisemethod=TRUE). nc number of clusters in original data (not including noise component if noisemethod=TRUE). nccl clustermethod, B, noisemethod, bootmethod, multipleboot, dissolution, recover input parameters, see above. matrix of Jaccard similarities for bootmethod="boot". Rows correspond to bootresult clusters in the original data set. Columns correspond to bootstrap runs. bootmean clusterwise means of the bootresult. bootbrd clusterwise number of times a cluster has been dissolved. bootrecover clusterwise number of times a cluster has been successfully recovered.

subsetresult, subsetmean, etc.

same as bootresult, bootmean, etc., but for the other resampling methods.

Author(s)

hennig/en/

References

Hennig, C. (2007) Cluster-wise assessment of cluster stability. Computational Statistics and Data Analysis, 52, 258-271.

Hennig, C. (2008) Dissolution point and isolation robustness: robustness criteria for general cluster analysis methods. Journal of Multivariate Analysis 99, 1154-1176.

See Also

dist, interface functions: kmeansCBI, hclustCBI, hclusttreeCBI, disthclustCBI, noisemclustCBI, distnoisemclustCBI, claraCBI, pamkCBI, dbscanCBI, mahalCBI

Examples

```
options(digits=3)
set.seed(20000)
face <- rFace(50,dMoNo=2,dNoEy=0,p=2)</pre>
cf1 <- clusterboot(face, B=3, bootmethod=
        c("boot", "noise", "jitter"), clustermethod=kmeansCBI,
        krange=5, seed=15555)
print(cf1)
plot(cf1)
cf2 <- clusterboot(dist(face), B=3, bootmethod=
        "subset", clustermethod=disthclustCBI,
        k=5, cut="number", method="average", showplots=TRUE, seed=15555)
print(cf2)
d1 <- c("a","b","a","c")
d2 <- c("a","a","a","b")
dx <- as.data.frame(cbind(d1,d2))</pre>
```

cmahal 47

```
\label{eq:cpx} \begin{split} &\text{cpx} <\text{-} &\text{clusterboot}(\text{dx}, \text{k=2}, \text{B=10}, \text{clustermethod=claraCBI}, \\ &\text{multipleboot=TRUE}, \text{usepam=TRUE}, \text{datatomatrix=FALSE}) \\ &\text{print}(\text{cpx}) \end{split}
```

cmahal

Generation of tuning constant for Mahalanobis fixed point clusters.

Description

Generates tuning constants ca for fixmahal dependent on the number of points and variables of the current fixed point cluster (FPC).

This is experimental and only thought for use in fixmahal.

Usage

```
cmahal(n, p, nmin, cmin, nc1, c1 = cmin, q = 1)
```

Arguments

n	positive integer. Number of points.
р	positive integer. Number of variables.
nmin	integer larger than 1. Smallest number of points for which ca is computed. For smaller FPC sizes, ca is set to the value for nmin.
cmin	positive number. Minimum value for ca.
nc1	positive integer. Number of points at which ca=c1.
c1	positive numeric. Tuning constant for cmahal. Value for ca for FPC size equal to ${\sf nc1}$.
q	numeric between 0 and 1. 1 for steepest possible descent of ca as function of the FPC size. Should presumably always be 1.

Details

Some experiments suggest that the tuning constant ca should decrease with increasing FPC size and increase with increasing p in fixmahal. This is to prevent too small meaningless FPCs while maintaining the significant larger ones. cmahal with q=1 computes ca in such a way that as long as ca>cmin, the decrease in n is as steep as possible in order to maintain the validity of the convergence theorem in Hennig and Christlieb (2002).

Value

A numeric vector of length n, giving the values for ca for all FPC sizes smaller or equal to n.

Author(s)

Christian Hennig <christian.hennig@unibo.it>https://www.unibo.it/sitoweb/christian.hennig/en/

48 con.comp

References

Hennig, C. and Christlieb, N. (2002) Validating visual clusters in large datasets: Fixed point clusters of spectral features, *Computational Statistics and Data Analysis* 40, 723-739.

See Also

fixmahal

Examples

con.comp

Connectivity components of an undirected graph

Description

Computes the connectivity components of an undirected graph from a matrix giving the edges.

Usage

```
con.comp(comat)
```

Arguments

comat

a symmetric logical or 0-1 matrix, where comat[i,j]=TRUE means that there is an edge between vertices i and j. The diagonal is ignored.

Details

The "depth-first search" algorithm of Cormen, Leiserson and Rivest (1990, p. 477) is used.

Value

An integer vector, giving the number of the connectivity component for each vertice.

Author(s)

```
Christian Hennig <christian.hennig@unibo.it>https://www.unibo.it/sitoweb/christian.hennig/en/
```

References

Cormen, T. H., Leiserson, C. E. and Rivest, R. L. (1990), *Introduction to Algorithms*, Cambridge: MIT Press.

confusion 49

See Also

hclust, cutree for cutted single linkage trees (often equivalent).

Examples

```
set.seed(1000)
x <- rnorm(20)
m <- matrix(0,nrow=20,ncol=20)
for(i in 1:20)
    for(j in 1:20)
    m[i,j] <- abs(x[i]-x[j])
d <- m<0.2
cc <- con.comp(d)
max(cc) # number of connectivity components
plot(x,cc)
# The same should be produced by
# cutree(hclust(as.dist(m),method="single"),h=0.2).</pre>
```

confusion

Misclassification probabilities in mixtures

Description

Estimates a misclassification probability in a mixture distribution between two mixture components from estimated posterior probabilities regardless of component parameters, see Hennig (2010).

Usage

```
confusion(z,pro,i,j,adjustprobs=FALSE)
```

Arguments

Z	matrix of posterior probabilities for observations (rows) to belong to mixture components (columns), so entries need to sum up to 1 for each row.
pro	vector of component proportions, need to sum up to 1.
i	integer. Component number.
j	integer. Component number.
adjustprobs	logical. If TRUE, probabilities are initially standardised so that those for components i and j add up to one (i.e., if they were the only components).

Value

Estimated probability that an observation generated by component j is classified to component i by maximum a posteriori rule.

50 cov.wml

Author(s)

Christian Hennig <christian.hennig@unibo.it>https://www.unibo.it/sitoweb/christian.hennig/en/

References

Hennig, C. (2010) Methods for merging Gaussian mixture components, *Advances in Data Analysis and Classification*, 4, 3-34.

Examples

```
set.seed(12345)
m <- rpois(20,lambda=5)
dim(m) <- c(5,4)
pro <- apply(m,2,sum)
pro <- pro/sum(pro)
m <- m/apply(m,1,sum)
round(confusion(m,pro,1,2),digits=2)</pre>
```

cov.wml

Weighted Covariance Matrices (Maximum Likelihood)

Description

Returns a list containing estimates of the weighted covariance matrix and the mean of the data, and optionally of the (weighted) correlation matrix. The covariance matrix is divided by the sum of the weights, corresponding to n and the ML-estimator in the case of equal weights, as opposed to n-1 for cov.wt.

Usage

```
cov.wml(x, wt = rep(1/nrow(x), nrow(x)), cor = FALSE, center = TRUE)
```

Arguments

X	a matrix or data frame. As usual, rows are observations and columns are variables.
wt	a non-negative and non-zero vector of weights for each observation. Its length must equal the number of rows of x.
cor	A logical indicating whether the estimated correlation weighted matrix will be returned as well.
center	Either a logical or a numeric vector specifying the centers to be used when computing covariances. If TRUE, the (weighted) mean of each variable is used, if 'FALSE, zero is used. If center is numeric, its length must equal the number of columns of x.

Value

A list containing the following named components:

cov the estimated (weighted) covariance matrix.

center an estimate for the center (mean) of the data.

n.obs the number of observations (rows) in x.

wt the weights used in the estimation. Only returned if given as an argument.

cor the estimated correlation matrix. Only returned if 'cor' is 'TRUE'.

Author(s)

Christian Hennig <christian.hennig@unibo.it>https://www.unibo.it/sitoweb/christian.hennig/en/

See Also

```
cov.wt, cov, var
```

Examples

```
x \leftarrow c(1,2,3,4,5,6,7,8,9,10)

y \leftarrow c(1,2,3,8,7,6,5,8,9,10)

cov.wml(cbind(x,y),wt=c(0,0,0,1,1,1,1,1,0,0))

cov.wt(cbind(x,y),wt=c(0,0,0,1,1,1,1,1,0,0))
```

cqcluster.stats

Cluster validation statistics (version for use with clusterbenchstats

Description

This is a more sophisticated version of cluster.stats for use with clusterbenchstats, see Hennig (2017). Computes a number of distance-based statistics, which can be used for cluster validation, comparison between clusterings and decision about the number of clusters: cluster sizes, cluster diameters, average distances within and between clusters, cluster separation, biggest within cluster gap, average silhouette widths, the Calinski and Harabasz index, a Pearson version of Hubert's gamma coefficient, the Dunn index, further statistics introduced in Hennig (2017) and two indexes to assess the similarity of two clusterings, namely the corrected Rand index and Meila's VI.

Usage

```
dquantile=0.1,
  nndist=TRUE, nnk=2, standardisation="max", sepall=TRUE, maxk=10,
  cvstan=sqrt(length(clustering)))

## S3 method for class 'cquality'
summary(object, stanbound=TRUE, largeisgood=TRUE, ...)

## S3 method for class 'summary.cquality'
print(x, ...)
```

Arguments

d a distance object (as generated by dist) or a distance matrix between cases.

clustering an integer vector of length of the number of cases, which indicates a clustering.

The clusters have to be numbered from 1 to the number of clusters.

alt.clustering an integer vector such as for clustering, indicating an alternative cluster-

ing. If provided, the corrected Rand index and Meila's VI for clustering vs.

alt.clustering are computed.

noisecluster logical. If TRUE, it is assumed that the largest cluster number in clustering

denotes a 'noise class', i.e. points that do not belong to any cluster. These points are not taken into account for the computation of all functions of within and

between cluster distances including the validation indexes.

silhouette logical. If TRUE, the silhouette statistics are computed, which requires package

cluster.

logical. If TRUE, Goodman and Kruskal's index G2 (cf. Gordon (1999), p. 62)

is computed. This executes lots of sorting algorithms and can be very slow (it

has been improved by R. Francois - thanks!)

G3 logical. If TRUE, the index G3 (cf. Gordon (1999), p. 62) is computed. This

executes sort on all distances and can be extremely slow.

wgap logical. If TRUE, the widest within-cluster gaps (largest link in within-cluster

minimum spanning tree) are computed. This is used for finding a good number

of clusters in Hennig (2013). See also parameter averagegap.

sepindex logical. If TRUE, a separation index is computed, defined based on the distances

for every point to the closest point not in the same cluster. The separation index is then the mean of the smallest proportion sepprob of these. This allows to formalise separation less sensitive to a single or a few ambiguous points. The output component corresponding to this is sindex, not separation! This is used for finding a good number of clusters in Hennig (2013). See also parameter

sepall.

sepprob numerical between 0 and 1, see sepindex.

sepwithnoise logical. If TRUE and sepindex and noisecluster are both TRUE, the noise

points are incorporated as cluster in the separation index (sepindex) computation. Also they are taken into account for the computation for the minimum

cluster separation.

compareonly logical. If TRUE, only the corrected Rand index and Meila's VI are computed

and given out (this requires alt.clustering to be specified).

aggregateonly logical. If TRUE (and not compareonly), no clusterwise but only aggregated

information is given out (this cuts the size of the output down a bit).

averagegap logical. If TRUE, the average of the widest within-cluster gaps over all clusters is

given out; if FALSE, the maximum is given out.

pamcrit logical. If TRUE, the average distance of points to their respective cluster cen-

troids is computed (criterion of the PAM clustering method); centroids are cho-

sen so that they minimise this criterion for the given clustering.

dquantile numerical between 0 and 1; quantile used for kernel density estimator for density

indexes, see Hennig (2019), Sec. 3.6.

nndist logical. If TRUE, average distance to nnkth nearest neighbour within cluster is

computed.

nnk integer. Number of neighbours used in average and coefficient of variation of

distance to nearest within cluster neighbour (clusters with nnk or fewer points

are ignored for this).

standardisation

"none", "max", "ave", "q90", or a number. See details.

sepall logical. If TRUE, a fraction of smallest sepprob distances to other clusters is

used from every cluster. Otherwise, a fraction of smallest sepprob distances

overall is used in the computation of sindex.

maxk numeric. Parsimony is defined as the number of clusters divided by maxk.

cvstan numeric. cvnnd is standardised by cvstan if there is standardisation, see De-

tails.

object of class equality, output of eqcluster.stats.

x object of class equality, output of eqcluster.stats.

stanbound logical. If TRUE, all index values larger than 1 will be set to 1, and all values

smaller than 0 will be set to 0. This is for preparation in case of largeisgood=TRUE (if values are already suitably standardised within cqcluster.stats, it won't

do harm and can do good).

largeisgood logical. If TRUE, indexes x are transformed to 1-x in case that before transforma-

tion smaller values indicate a better clustering (that's average.within, mnnd, widestgap, within.clust

For this to make sense, cqcluster.stats should be run with standardisation="max"

and summary.cquality with stanbound=TRUE.

... no effect.

Details

The standardisation-parameter governs the standardisation of the index values. standardisation="none" means that unstandardised raw values of indexes are given out. Otherwise, entropy will be standardised by the maximum possible value for the given number of clusters; within.cluster.ss and between.cluster.ss will be standardised by the overall sum of squares; mnnd will be standardised by the maximum distance to the nnkth nearest neighbour within cluster; pearsongamma will be standardised by adding 1 and dividing by 2; cvnn will be standardised by cvstan (the default is the possible maximum).

standardisation allows options for the standardisation of average.within, sindex, wgap, pamcrit, max.diameter, min. and can be "max" (maximum distance), "ave" (average distance), q90 (0.9-quantile of distances), or a positive number. "max" is the default and standardises all the listed indexes into the range [0,1].

Value

cqcluster.stats with compareonly=FALSE and aggregateonly=FALSE returns a list of type cquality containing the components n, cluster.number, cluster.size, min.cluster.size, noisen, diameter, averag Some of these are standardised, see Details. If compareonly=TRUE, only corrected.rand, vi are given out. If aggregateonly=TRUE, only n, cluster.number, min.cluster.size, noisen, diameter, average.between, are given out.

summary.cquality returns a list of type summary.cquality with components average.within,nnk,mnnd,avg.silwidth These are as documented below for cqcluster.stats, but after transformation by stanbound and largeisgood, see arguments.

n number of points.

cluster.number number of clusters.

cluster.size vector of cluster sizes (number of points).

min.cluster.size

size of smallest cluster.

noisen number of noise points, see argument noisecluster (noisen=0 if noisecluster=FALSE).

diameter vector of cluster diameters (maximum within cluster distances).

average.distance

vector of clusterwise within cluster average distances.

median.distance

vector of clusterwise within cluster distance medians.

separation vector of clusterwise minimum distances of a point in the cluster to a point of

another cluster.

average.toother

vector of clusterwise average distances of a point in the cluster to the points of

other clusters.

separation.matrix

matrix of separation values between all pairs of clusters.

ave.between.matrix

matrix of mean dissimilarities between points of every pair of clusters.

avebetween average distance between clusters.

avewithin average distance within clusters (reweighted so that every observation, rather

than every distance, has the same weight).

n.between number of distances between clusters.n.within number of distances within clusters.

maxdiameter maximum cluster diameter.
minsep minimum cluster separation.

withinss a generalisation of the within clusters sum of squares (k-means objective func-

tion), which is obtained if d is a Euclidean distance matrix. For general distance measures, this is half the sum of the within cluster squared dissimilarities di-

vided by the cluster size.

clus.avg.silwidths

vector of cluster average silhouette widths. See silhouette.

asw average silhouette width. See silhouette.

g2 Goodman and Kruskal's Gamma coefficient. See Milligan and Cooper (1985),

Gordon (1999, p. 62).

g3 G3 coefficient. See Gordon (1999, p. 62).

pearsongamma correlation between distances and a 0-1-vector where 0 means same cluster, 1

means different clusters. "Normalized gamma" in Halkidi et al. (2001).

dunn minimum separation / maximum diameter. Dunn index, see Halkidi et al. (2002).

dunn2 minimum average dissimilarity between two cluster / maximum average within

cluster dissimilarity, another version of the family of Dunn indexes.

entropy entropy of the distribution of cluster memberships, see Meila(2007).

wb.ratio average.within/average.between.

ch Calinski and Harabasz index (Calinski and Harabasz 1974, optimal in Milligan

and Cooper 1985; generalised for dissimilarities in Hennig and Liao 2013).

cwidegap vector of widest within-cluster gaps.

widest gap widest within-cluster gap or average of cluster-wise widest within-cluster gap,

depending on parameter averagegap.

corrected.rand corrected Rand index (if alt.clustering has been specified), see Gordon (1999,

p. 198).

vi variation of information (VI) index (if alt.clustering has been specified), see

Meila (2007).

sindex separation index, see argument sepindex.

svec vector of smallest closest distances of points to next cluster that are used in the

computation of sindex if sepall=TRUE.

psep vector of all closest distances of points to next cluster.

stan value by which som statistics were standardised, see Details.

nnk value of input parameter nnk.

mnnd average distance to nnkth nearest neighbour within cluster.

pamc average distance to cluster centroid.
pamcentroids index numbers of cluster centroids.

dindex this index measures to what extent the density decreases from the cluster mode

to the outskirts; I-densdec in Sec. 3.6 of Hennig (2019); low values are good.

denscut this index measures whether cluster boundaries run through density valleys; I-

densbound in Sec. 3.6 of Hennig (2019); low values are good.

highdgap this measures whether there is a large within-cluster gap with high density on

both sides; I-highdgap in Sec. 3.6 of Hennig (2019); low values are good.

npenalty vector of penalties for all clusters that are used in the computation of denscut, see Hennig (2019) (these are sums of penalties over all points in the cluster). depenalty vector of penalties for all clusters that are used in the computation of dindex, see Hennig (2019) (these are sums of several penalties for density increase when going from the mode outward in the cluster). withindensp distance-based kernel density values for all points as computed in Sec. 3.6 of Hennig (2019). densoc contribution of points from other clusters than the one to which a point is assigned to the density, for all points; called h_o in Sec. 3.6 of Hennig (2019). pdistto list that for all clusters has a sequence of point numbers. These are the points already incorporated in the sequence of points constructed in the algorithm in Sec. 3.6 of Hennig (2019) to which the next point to be joined is connected. list that for all clusters has a sequence of point numbers. Sequence of points to pclosetomode be incorporated in the sequence of points constructed in the algorithm in Sec. 3.6 of Hennig (2019). distto list that for all clusters has a sequence of differences between the standardised densities (see percwdens) at the new point added and the point to which it is connected (if this is positive, the penalty is this to the square), in the algorithm in Sec. 3.6 of Hennig (2019). percwdens this is withindensp divided by its maximum. percdensoc this is densoc divided by the maximum of withindensp, called h_o^* in Sec. 3.6 of Hennig (2019). parsimony number of clusters divided by maxk. cvnnd coefficient of variation of dissimilarities to nnkth nearest within-cluster neighbour, measuring uniformity of within-cluster densities, weighted over all clusters, see Sec. 3.7 of Hennig (2019). cvnndc vector of cluster-wise coefficients of variation of dissimilarities to nnkth nearest wthin-cluster neighbour as required in computation of cvnnd.

Note

Because cqcluster.stats processes a full dissimilarity matrix, it isn't suitable for large data sets. You may consider distcritmulti in that case.

Author(s)

Christian Hennig <christian.hennig@unibo.it>https://www.unibo.it/sitoweb/christian.hennig/en/

References

Akhanli, S. and Hennig, C. (2020) Calibrating and aggregating cluster validity indexes for context-adapted comparison of clusterings. *Statistics and Computing*, 30, 1523-1544, https://link.springer.com/article/10.1007/s11222-020-09958-2, https://arxiv.org/abs/2002.01822

Calinski, T., and Harabasz, J. (1974) A Dendrite Method for Cluster Analysis, *Communications in Statistics*, 3, 1-27.

cvnn 57

Gordon, A. D. (1999) Classification, 2nd ed. Chapman and Hall.

Halkidi, M., Batistakis, Y., Vazirgiannis, M. (2001) On Clustering Validation Techniques, *Journal of Intelligent Information Systems*, 17, 107-145.

Hennig, C. and Liao, T. (2013) How to find an appropriate clustering for mixed-type variables with application to socio-economic stratification, *Journal of the Royal Statistical Society, Series C Applied Statistics*, 62, 309-369.

Hennig, C. (2013) How many bee species? A case study in determining the number of clusters. In: Spiliopoulou, L. Schmidt-Thieme, R. Janning (eds.): "Data Analysis, Machine Learning and Knowledge Discovery", Springer, Berlin, 41-49.

Hennig, C. (2019) Cluster validation by measurement of clustering characteristics relevant to the user. In C. H. Skiadas (ed.) *Data Analysis and Applications 1: Clustering and Regression, Modeling-estimating, Forecasting and Data Mining, Volume 2*, Wiley, New York 1-24, https://arxiv.org/abs/1703.09282

Kaufman, L. and Rousseeuw, P.J. (1990). "Finding Groups in Data: An Introduction to Cluster Analysis". Wiley, New York.

Meila, M. (2007) Comparing clusterings?an information based distance, *Journal of Multivariate Analysis*, 98, 873-895.

Milligan, G. W. and Cooper, M. C. (1985) An examination of procedures for determining the number of clusters. *Psychometrika*, 50, 159-179.

See Also

cluster.stats, silhouette, dist, calinhara, distcritmulti. clusterboot computes clusterwise stability statistics by resampling.

Examples

cvnn

Cluster validation based on nearest neighbours

Description

Cluster validity index based on nearest neighbours as defined in Liu et al. (2013) with a correction explained in Halkidi et al. (2015).

58 cvnn

Usage

```
cvnn(d=NULL,clusterings,k=5)
```

Arguments

d dissimilarity matrix or dist-object.

clusterings list of vectors of integers with length =nrow(d); indicating the cluster for each

observation for several clusterings (list elements) to be compared.

k integer. Number of nearest neighbours.

Value

List with components (see Liu et al. (2013), Halkidi et al. (2015) for details)

cvnnindex vector of index values for the various clusterings, see Liu et al. (2013), the lower

the better.

sep vector of separation values.

comp vector of compactness values.

Author(s)

Christian Hennig <christian.hennig@unibo.it>https://www.unibo.it/sitoweb/christian.hennig/en/

References

Halkidi, M., Vazirgiannis, M. and Hennig, C. (2015) Method-independent indices for cluster validation. In C. Hennig, M. Meila, F. Murtagh, R. Rocci (eds.) *Handbook of Cluster Analysis*, CRC Press/Taylor & Francis, Boca Raton.

Liu, Y, Li, Z., Xiong, H., Gao, X., Wu, J. and Wu, S. (2013) Understanding and enhancement of internal clustering validation measures. *IEEE Transactions on Cybernetics* 43, 982-994.

Examples

```
options(digits=3)
iriss <- as.matrix(iris[c(1:10,51:55,101:105),-5])
irisc <- as.numeric(iris[c(1:10,51:55,101:105),5])
print(cvnn(dist(iriss),list(irisc,rep(1:4,5))))</pre>
```

cweight 59

cweight

Weight function for AWC

Description

For use in awcoord only.

Usage

```
cweight(x, ca)
```

Arguments

x numerical.
ca numerical.

Value

```
ca/x if smaller than 1, else 1.
```

Author(s)

Christian Hennig <christian.hennig@unibo.it>https://www.unibo.it/sitoweb/christian.hennig/en/

See Also

awcoord

Examples

```
cweight(4,1)
```

dbscan

DBSCAN density reachability and connectivity clustering

Description

Generates a density based clustering of arbitrary shape as introduced in Ester et al. (1996).

60 dbscan

Usage

```
dbscan(data, eps, MinPts = 5, scale = FALSE, method = c("hybrid", "raw",
    "dist"), seeds = TRUE, showplot = FALSE, countmode = NULL)
    ## S3 method for class 'dbscan'
print(x, ...)
    ## S3 method for class 'dbscan'
plot(x, data, ...)
    ## S3 method for class 'dbscan'
predict(object, data, newdata = NULL,
predict.max=1000, ...)
```

Arguments

data matrix, data.frame, dissimilarity matrix or dist-object. Specify method="dist"

if the data should be interpreted as dissimilarity matrix or object. Otherwise Eu-

clidean distances will be used.

eps Reachability distance, see Ester et al. (1996).

MinPts Reachability minimum no. of points, see Ester et al. (1996).

scale scale the data if TRUE.

method "dist" treats data as distance matrix (relatively fast but memory expensive),

"raw" treats data as raw data and avoids calculating a distance matrix (saves memory but may be slow), "hybrid" expects also raw data, but calculates partial

distance matrices (very fast with moderate memory requirements).

seeds FALSE to not include the isseed-vector in the dbscan-object.

showplot 0 = no plot, 1 = plot per iteration, 2 = plot per subiteration.

countmode NULL or vector of point numbers at which to report progress.

x object of class dbscan.
object object of class dbscan.

newdata matrix or data.frame with raw data to predict.

predict.max max. batch size for predictions.

... Further arguments transferred to plot methods.

Details

Clusters require a minimum no of points (MinPts) within a maximum distance (eps) around one of its members (the seed). Any point within eps around any point which satisfies the seed condition is a cluster member (recursively). Some points may not belong to any clusters (noise).

We have clustered a 100.000 x 2 dataset in 40 minutes on a Pentium M 1600 MHz.

print.dbscan shows a statistic of the number of points belonging to the clusters that are seeds and border points.

plot.dbscan distinguishes between seed and border points by plot symbol.

dbscan 61

Value

predict.dbscan gives out a vector of predicted clusters for the points in newdata. dbscan gives out an object of class 'dbscan' which is a LIST with components

cluster integer vector coding cluster membership with noise observations (singletons)

coded as 0

isseed logical vector indicating whether a point is a seed (not border, not noise)

eps parameter eps MinPts parameter MinPts

Note

this is a simplified version of the original algorithm (no K-D-trees used), thus we have $o(n^2)$ instead of o(n*log(n))

Author(s)

Jens Oehlschlaegel, based on a draft by Christian Hennig.

References

Martin Ester, Hans-Peter Kriegel, Joerg Sander, Xiaowei Xu (1996). A Density-Based Algorithm for Discovering Clusters in Large Spatial Databases with Noise. Institute for Computer Science, University of Munich. Proceedings of 2nd International Conference on Knowledge Discovery and Data Mining (KDD-96).

Examples

```
set.seed(665544)
 n <- 600
 x \leftarrow cbind(runif(10, 0, 10) + rnorm(n, sd=0.2), runif(10, 0, 10) + rnorm(n, sd=0.2))
    sd=0.2))
 par(bg="grey40")
 ds \leftarrow dbscan(x, 0.2)
# run with showplot=1 to see how dbscan works.
 ds
 plot(ds, x)
 x2 <- matrix(0,nrow=4,ncol=2)</pre>
 x2[1,] <- c(5,2)
 x2[2,] <- c(8,3)
 x2[3,] <- c(4,4)
 x2[4,] \leftarrow c(9,9)
 predict(ds, x, x2)
 x \leftarrow cbind((1:3)+rnorm(n, sd=0.2), (1:3)+rnorm(n, sd=0.2))
# Not run, but results from my machine are 0.105 - 0.068 - 0.255:
# system.time(ds <- dbscan(x, 0.3, countmode=NULL, method="raw"))[3]</pre>
```

62 dipp.tantrum

```
# system.time(dsb <- dbscan(x, 0.3, countmode=NULL, method="hybrid"))[3]
# system.time(dsc <- dbscan(dist(x), 0.3, countmode=NULL,
# method="dist"))[3]</pre>
```

dipp.tantrum

Simulates p-value for dip test

Description

Simulates p-value for dip test (see dip) in the way suggested by Tantrum, Murua and Stuetzle (2003) from the clostest unimodal distribution determined by kernel density estimation with bandwith chosen so that the density just becomes unimodal. This is less conservative (and in fact sometimes anti-conservative) than the values from dip.test.

Usage

```
dipp.tantrum(xdata,d,M=100)
```

Arguments

xdata numeric vector. One-dimensional dataset.

d numeric. Value of dip statistic.

M integer. Number of artificial datasets generated in order to estimate the p-value.

Value

List with components

p. value approximated p-value.

bw borderline unimodality bandwith in density with default settings.

dv vector of dip statistic values from simulated artificial data.

Author(s)

Christian Hennig <christian.hennig@unibo.it>https://www.unibo.it/sitoweb/christian.hennig/en/

References

J. A. Hartigan and P. M. Hartigan (1985) The Dip Test of Unimodality, *Annals of Statistics*, 13, 70-84.

Tantrum, J., Murua, A. and Stuetzle, W. (2003) Assessment and Pruning of Hierarchical Model Based Clustering, *Proceedings of the ninth ACM SIGKDD international conference on Knowledge discovery and data mining*, Washington, D.C., 197-205.

diptest.multi 63

Examples

```
# not run, requires package diptest
# x <- runif(100)
# d <- dip(x)
# dt <- dipp.tantrum(x,d,M=10)</pre>
```

diptest.multi

Diptest for discriminant coordinate projection

Description

Diptest (Hartigan and Hartigan, 1985, see dip) for data projected in discriminant coordinate separating optimally two class means (see discroord) as suggested by Tantrum, Murua and Stuetzle (2003).

Usage

```
diptest.multi(xdata,class,pvalue="uniform",M=100)
```

Arguments

xdata matrix. Potentially multidimensional dataset.

class vector of integers giving class numbers for observations.

pvalue "uniform" or "tantrum". Defines whether the p-value is computed from a uni-

form null model as suggested in Hartigan and Hartigan (1985, using dip. test)

or as suggested in Tantrum et al. (2003, using dipp.tantrum).

M integer. Number of artificial datasets generated in order to estimate the p-value

if pvalue="tantrum".

Value

The resulting p-value.

Author(s)

Christian Hennig <christian.hennig@unibo.it>https://www.unibo.it/sitoweb/christian.hennig/en/

References

J. A. Hartigan and P. M. Hartigan (1985) The Dip Test of Unimodality, *Annals of Statistics*, 13, 70-84.

Tantrum, J., Murua, A. and Stuetzle, W. (2003) Assessment and Pruning of Hierarchical Model Based Clustering, *Proceedings of the ninth ACM SIGKDD international conference on Knowledge discovery and data mining*, Washington, D.C., 197-205.

64 discreoord

Examples

```
require(diptest)
x <- cbind(runif(100),runif(100))
partition <- 1+(x[,1]<0.5)
d1 <- diptest.multi(x,partition)
d2 <- diptest.multi(x,partition,pvalue="tantrum",M=10)</pre>
```

discrcoord

Discriminant coordinates/canonical variates

Description

Computes discriminant coordinates, sometimes referred to as "canonical variates" as described in Seber (1984).

Usage

```
discrcoord(xd, clvecd, pool = "n", ...)
```

Arguments

xd the data matrix; a numerical object which can be coerced to a matrix.

clvecd integer vector of class numbers; length must equal nrow(xd).

pool string. Determines how the within classes covariance is pooled. "n" means that

the class covariances are weighted corresponding to the number of points in each

class (default). "equal" means that all classes get equal weight.

... no effect

Details

The matrix T (see Seber (1984), p. 270) is inverted by use of tdecomp, which can be expected to give reasonable results for singular within-class covariance matrices.

Value

List with the following components

ev eigenvalues in descending order.

units columns are coordinates of projection basis vectors. New points x can be pro-

jected onto the projection basis vectors by x %*% units

proj projections of xd onto units.

Author(s)

Christian Hennig <christian.hennig@unibo.it>https://www.unibo.it/sitoweb/christian.hennig/en/

discrete.recode 65

References

Seber, G. A. F. (1984). Multivariate Observations. New York: Wiley.

See Also

plotcluster for straight forward discriminant plots.

batcoord for discriminating projections for two classes, so that also the differences in variance are shown (discrecord is based only on differences in mean).

rFace for generation of the example data used below.

Examples

```
set.seed(4634)
face <- rFace(600,dMoNo=2,dNoEy=0)
grface <- as.integer(attr(face,"grouping"))
dcf <- discrcoord(face,grface)
plot(dcf$proj,col=grface)
# ...done in one step by function plotcluster.</pre>
```

discrete.recode

Recodes mixed variables dataset

Description

Recodes a dataset with mixed continuous and categorical variables so that the continuous variables come first and the categorical variables have standard coding 1, 2, 3,... (in lexicographical ordering of values coerced to strings).

Usage

discrete.recode(x,xvarsorted=TRUE,continuous=0,discrete)

Arguments

х	data matrix or data frame. The data need to be organised case-wise, i.e., if there are categorical variables only, and 15 cases with values c(1,1,2) on the 3 variables, the data matrix needs 15 rows with values 1 1 2. (Categorical variables could take numbers or strings or anything that can be coerced to factor levels as values.)
xvarsorted	logical. If TRUE, the continuous variables are assumed to be the first ones, and the categorical variables to be behind them.
continuous	vector of integers giving positions of the continuous variables. If xvarsorted=TRUE, a single integer, number of continuous variables.
discrete	vector of integers giving positions of the categorical variables (the variables need to be coded in such a way that data.matrix converts them to something numeric). If xvarsorted=TRUE, a single integer, number of categorical variables.

66 discrproj

Value

A list with components

data matrix with continuous variables first and categorical variables in standard

coding behind them.

ppdim vector of categorical variable-wise numbers of categories.

discretelevels list of levels of the categorical variables belonging to what is treated by flexmixedruns

as category 1, 2, 3 etc.

continuous number of continuous variables.
discrete number of categorical variables.

Author(s)

```
Christian Hennig <christian.hennig@unibo.it>https://www.unibo.it/sitoweb/christian.hennig/en
```

See Also

1cmixed

Examples

```
set.seed(776655)
v1 <- rnorm(20)
v2 <- rnorm(20)
d1 <- sample(c(2,4,6,8),20,replace=TRUE)
d2 <- sample(1:4,20,replace=TRUE)
ldata <- cbind(v1,d1,v2,d2)
lc <-
discrete.recode(ldata,xvarsorted=FALSE,continuous=c(1,3),discrete=c(2,4))
require(MASS)
data(Cars93)
Cars934 <- Cars93[,c(3,5,8,10)]
cc <- discrete.recode(Cars934,xvarsorted=FALSE,continuous=c(2,3),discrete=c(1,4))</pre>
```

discrproj

Linear dimension reduction for classification

Description

An interface for ten methods of linear dimension reduction in order to separate the groups optimally in the projected data. Includes classical discriminant coordinates, methods to project differences in mean and covariance structure, asymmetric methods (separation of a homogeneous class from a heterogeneous one), local neighborhood-based methods and methods based on robust covariance matrices.

discrproj 67

Usage

Arguments

x the data matrix; a numerical object which can be coerced to a matrix.

clvecd vector of class numbers which can be coerced into integers; length must equal

nrow(xd).

method one of

"dc" usual discriminant coordinates, see discrecord,

"bc" Bhattacharyya coordinates, first coordinate showing mean differences, second showing covariance matrix differences, see batcoord,

"vbc" variance dominated Bhattacharyya coordinates, see batcoord,

"mvdc" added meana and variance differences optimizing coordinates, see mvdcoord,

"adc" asymmetric discriminant coordinates, see adcoord,

"awc" asymmetric discriminant coordinates with weighted observations, see awcoord,

"arc" asymmetric discriminant coordinates with weighted observations and robust MCD-covariance matrix, see awcoord,

"nc" neighborhood based coordinates, see ncoord,

"wnc" neighborhood based coordinates with weighted neighborhoods, see ncoord,

"anc" asymmetric neighborhood based coordinates, see ancoord.

Note that "bc", "vbc", "adc", "awc", "arc" and "anc" assume that there are only

two classes.

clnum integer. Number of the class which is attempted to plot homogeneously by

"asymmetric methods", which are the methods assuming that there are only two

classes, as indicated above.

ignorepoints logical. If TRUE, points with label ignorenum in clvecd are ignored in the com-

putation for method and are only projected afterwards onto the resulting units.

If pch=NULL, the plot symbol for these points is "N".

ignorenum one of the potential values of the components of clvecd. Only has effect if

ignorepoints=TRUE, see above.

... additional parameters passed to the projection methods.

Value

discrproj returns the output of the chosen projection method, which is a list with at least the components ev, units, proj. For detailed informations see the help pages of the projection methods.

ev eigenvalues in descending order, usually indicating portion of information in the

corresponding direction.

units columns are coordinates of projection basis vectors. New points x can be pro-

jected onto the projection basis vectors by x %*% units

proj projections of xd onto units.

68 distancefactor

Author(s)

Christian Hennig <christian.hennig@unibo.it>https://www.unibo.it/sitoweb/christian.hennig/en/

References

Hennig, C. (2004) Asymmetric linear dimension reduction for classification. Journal of Computational and Graphical Statistics 13, 930-945.

Hennig, C. (2005) A method for visual cluster validation. In: Weihs, C. and Gaul, W. (eds.): Classification - The Ubiquitous Challenge. Springer, Heidelberg 2005, 153-160.

Seber, G. A. F. (1984). Multivariate Observations. New York: Wiley.

Fukunaga (1990). Introduction to Statistical Pattern Recognition (2nd ed.). Boston: Academic Press.

See Also

```
discrcoord, batcoord, mvdcoord, adcoord, awcoord, ncoord, ancoord. rFace for generation of the example data used below.
```

Examples

```
set.seed(4634)
face <- rFace(300,dMoNo=2,dNoEy=0,p=3)
grface <- as.integer(attr(face,"grouping"))

# The abs in the following is there to unify the output,
# because eigenvectors are defined only up to their sign.
# Statistically it doesn't make sense to compute absolute values.
round(abs(discrproj(face,grface, method="nc")$units),digits=2)
round(abs(discrproj(face,grface, method="wnc")$units),digits=2)
round(abs(discrproj(face,grface, clnum=1, method="arc")$units),digits=2)</pre>
```

distancefactor

Factor for dissimilarity of mixed type data

Description

Computes a factor that can be used to standardise ordinal categorical variables and binary dummy variables coding categories of nominal scaled variables for Euclidean dissimilarity computation in mixed type data. See Hennig and Liao (2013).

Usage

distancefactor 69

Arguments

cat	integer. Number of categories of the variable to be standardised. Note that for type="categorical" the number of categories of the original variable is required, although the distancefactor is used to standardise dummy variables for the categories.
n	integer. Number of data points.
catsizes	vector of integers giving numbers of observations per category. One of n and catsizes must be supplied. If catsizes=NULL, rep(round(n/cat),cat) is used (this may be appropriate as well if numbers of observations of categories are unequal, if the researcher decides that the dissimilarity measure should not be influenced by empirical category sizes.
type	"categorical" if the factor is used for dummy variables belonging to a nominal variable, "ordinal" if the factor is used for an ordinal variable ind standard Likert coding.
normfactor	numeric. Factor on which standardisation is based. As a default, this is $E(X_1-X_2)^2=0$ for independent unit variance variables.
qfactor	numeric. Factor q in Hennig and Liao (2013) to adjust for clumping effects due

Value

A factor by which to multiply the variable in order to make it comparable to a unit variance continuous variable when aggregated in Euclidean fashion for dissimilarity computation, so that expected effective difference between two realisations of the variable equals qfactor*normfactor.

Author(s)

Christian Hennig <christian.hennig@unibo.it>https://www.unibo.it/sitoweb/christian.hennig/en

References

Hennig, C. and Liao, T. (2013) How to find an appropriate clustering for mixed-type variables with application to socio-economic stratification, *Journal of the Royal Statistical Society, Series C Applied Statistics*, 62, 309-369.

See Also

```
1cmixed, pam
```

Examples

```
set.seed(776655)
d1 <- sample(1:5,20,replace=TRUE)
d2 <- sample(1:4,20,replace=TRUE)
ldata <- cbind(d1,d2)
lc <- cat2bin(ldata,categorical=1)$data
lc[,1:5] <- lc[,1:5]*distancefactor(5,20,type="categorical")
lc[,6] <- lc[,6]*distancefactor(4,20,type="ordinal")</pre>
```

to discreteness.

70 distcritmulti

distcritmulti	Distance based validity criteria for large data sets
	·

Description

Approximates average silhouette width or the Pearson version of Hubert's gamma criterion by hacking the dataset into pieces and averaging the subset-wise values, see Hennig and Liao (2013).

Usage

Arguments

X	cases times variables data matrix.
clustering	vector of integers indicating the clustering.
part	vector of integer subset sizes; sum should be smaller or equal to the number of cases of x. If NULL, subset sizes are chosen approximately equal.
ns	integer. Number of subsets, only used if part==NULL.
criterion	"asw" or "pearsongamma", specifies whether the average silhouette width or the Pearson version of Hubert's gamma is computed.
fun	" ${\tt dist}$ " or " ${\tt daisy}$ ", specifies which function is used for computing dissimilarities.
metric	passed on to \mbox{dist} (as argument method) or \mbox{daisy} to determine which dissimilarity is used.
count	logical. if TRUE, the subset number just processed is printed.
seed	integer, random seed. (If NULL, result depends on random numbers.)
	further arguments to be passed on to dist or daisy.

Value

A list with components crit.overall, crit.sub, crit.sd, part.

```
crit.overall value of criterion.
crit.sub vector of subset-wise criterion values.
crit.sd standard deviation of crit.sub, can be used to assess stability.
subsets list of case indexes in subsets.
```

Author(s)

Christian Hennig <christian.hennig@unibo.it>https://www.unibo.it/sitoweb/christian.hennig/en

distrsimilarity 71

References

Halkidi, M., Batistakis, Y., Vazirgiannis, M. (2001) On Clustering Validation Techniques, *Journal of Intelligent Information Systems*, 17, 107-145.

Hennig, C. and Liao, T. (2013) How to find an appropriate clustering for mixed-type variables with application to socio-economic stratification, *Journal of the Royal Statistical Society, Series C Applied Statistics*, 62, 309-369.

Kaufman, L. and Rousseeuw, P.J. (1990). "Finding Groups in Data: An Introduction to Cluster Analysis". Wiley, New York.

See Also

```
cluster.stats, silhouette
```

Examples

```
set.seed(20000)
options(digits=3)
face <- rFace(50,dMoNo=2,dNoEy=0,p=2)
clustering <- as.integer(attr(face,"grouping"))
distcritmulti(face,clustering,ns=3,seed=100000,criterion="pearsongamma")</pre>
```

distrsimilarity

Similarity of within-cluster distributions to normal and uniform

Description

Two measures of dissimilarity between the within-cluster distributions of a dataset and normal or uniform distribution. For the normal it's the Kolmogorov dissimilarity between the Mahalanobis distances to the center and a chi-squared distribution. For the uniform it is the Kolmogorov distance between the distance to the kth nearest neighbour and a Gamma distribution (this is based on Byers and Raftery (1998)). The clusterwise values are aggregated by weighting with the cluster sizes.

Usage

```
distrsimilarity(x,clustering,noisecluster = FALSE,
distribution=c("normal","uniform"),nnk=2,
largeisgood=FALSE,messages=FALSE)
```

Arguments

x the data matrix; a numerical object which can be coerced to a matrix.

clustering integer vector of class numbers; length must equal nrow(x), numbers must go

from 1 to the number of clusters.

noisecluster logical. If TRUE, the cluster with the largest number is ignored for the computa-

tions.

72 distrsimilarity

distribution vector of "normal", "uniform" or both. Indicates which of the two dissimilar-

ities is/are computed.

nnk integer. Number of nearest neighbors to use for dissimilarity to the uniform.

largeisgood logical. If TRUE, dissimilarities are transformed to 1-d (this means that larger

values indicate a better fit).

messages logical. If TRUE, warnings are given if within-cluster covariance matrices are

not invertible (in which case all within-cluster Mahalanobis distances are set to

zero).

Value

List with the following components

kdnorm Kolmogorov distance between distribution of within-cluster Mahalanobis dis-

tances and appropriate chi-squared distribution, aggregated over clusters (I am

grateful to Agustin Mayo-Iscar for the idea).

kdunif Kolmogorov distance between distribution of distances to nnkth nearest within-

cluster neighbor and appropriate Gamma-distribution, see Byers and Raftery

(1998), aggregated over clusters.

kdnormc vector of cluster-wise Kolmogorov distances between distribution of within-

cluster Mahalanobis distances and appropriate chi-squared distribution.

kdunifc vector of cluster-wise Kolmogorov distances between distribution of distances

to nnkth nearest within-cluster neighbor and appropriate Gamma-distribution.

xmahal vector of Mahalanobs distances to the respective cluster center.
xdknn vector of distance to nnkth nearest within-cluster neighbor.

Note

It is very hard to capture similarity to a multivariate normal or uniform in a single value, and both used here have their shortcomings. Particularly, the dissimilarity to the uniform can still indicate a good fit if there are holes or it's a uniform distribution concentrated on several not connected sets.

Author(s)

Christian Hennig <christian.hennig@unibo.it>https://www.unibo.it/sitoweb/christian.hennig/en/

References

Byers, S. and Raftery, A. E. (1998) Nearest-Neighbor Clutter Removal for Estimating Features in Spatial Point Processes, *Journal of the American Statistical Association*, 93, 577-584.

Hennig, C. (2017) Cluster validation by measurement of clustering characteristics relevant to the user. In C. H. Skiadas (ed.) *Proceedings of ASMDA 2017*, 501-520, https://arxiv.org/abs/1703.09282

See Also

cqcluster.stats,cluster.stats for more cluster validity statistics.

dridgeline 73

Examples

```
set.seed(20000)
options(digits=3)
face <- rFace(200,dMoNo=2,dNoEy=0,p=2)
km3 <- kmeans(face,3)
distrsimilarity(face,km3$cluster)</pre>
```

dridgeline

Density along the ridgeline

Description

Computes the density of a two-component Gaussian mixture along the ridgeline (Ray and Lindsay, 2005), along which all its density extrema are located.

Usage

Arguments

alpha	sequence of values between 0 and 1 for which the density is computed.
prop	mixture proportion of first component.
mu1	mean vector of component 1.
mu2	mean vector of component 2.
Sigma1	covariance matrix of component 1.
Sigma2	covariance matrix of component 2.
showplot	logical. If TRUE, the density is plotted against alpha.
	further arguments to be passed on to plot.

Value

Vector of density values for values of alpha.

Author(s)

```
Christian Hennig <christian.hennig@unibo.it>https://www.unibo.it/sitoweb/christian.hennig/en/
```

References

Ray, S. and Lindsay, B. G. (2005) The Topography of Multivariate Normal Mixtures, *Annals of Statistics*, 33, 2042-2065.

```
q \leftarrow dridgeline(seq(0,1,0.1),0.5,c(1,1),c(2,5),diag(2),diag(2))
```

74 dudahart2

dudahart2 Dud	da-Hart test for splitting
---------------	----------------------------

Description

Duda-Hart test for whether a data set should be split into two clusters.

Usage

```
dudahart2(x,clustering,alpha=0.001)
```

Arguments

x data matrix or data frame.

clustering vector of integers. Clustering into two clusters.

alpha numeric between 0 and 1. Significance level (recommended to be small if this

is used for estimating the number of clusters).

Value

A list with components

p.value p-value against null hypothesis of homogemeity.

dh ratio of within-cluster sum of squares for two clusters and overall sum of squares.

compare critical value for dh at level alpha.

cluster1 FALSE if the null hypothesis of homogemeity is rejected.

alpha see above.

z 1-alpha-quantile of a standard Gaussian.

Author(s)

Christian Hennig <christian.hennig@unibo.it>https://www.unibo.it/sitoweb/christian.hennig/en

References

Duda, R. O. and Hart, P. E. (1973) Pattern Classification and Scene Analysis. Wiley, New York.

See Also

```
cluster.stats
```

extract.mixturepars 75

Examples

```
options(digits=2)
set.seed(98765)
iriss <- iris[sample(150,20),-5]
km <- kmeans(iriss,2)
dudahart2(iriss,km$cluster)</pre>
```

extract.mixturepars

Extract parameters for certain components from mclust

Description

Extracts parameters of certain mixture components from the output of summary.mclustBIC and updates proportions so that they sum up to 1.

Usage

```
extract.mixturepars(mclustsum,compnumbers,noise=FALSE)
```

Arguments

mclustsum output object of summary.mclustBIC.

compnumbers vector of integers. Numbers of mixture components.

noise logical. Should be TRUE if a noise component was fitted by mclustBIC.

Value

Object as component parameters of summary.mclustBIC-output, but for specified components only. (Orientation information from all components is kept.)

Author(s)

```
Christian Hennig <christian.hennig@unibo.it>https://www.unibo.it/sitoweb/christian.hennig/en/
```

```
set.seed(98765)
require(mclust)
iriss <- iris[sample(150,20),-5]
irisBIC <- mclustBIC(iriss,G=5,modelNames="VEV")
siris <- summary(irisBIC,iriss)
emp <- extract.mixturepars(siris,2)
emp$pro
round(emp$mean,digits=1)
emp$variance$modelName
round(emp$variance$scale,digits=2)</pre>
```

76 findrep

findrep	Finding representatives for cluster border

Description

Finds representative objects for the border of a cluster and the within-cluster variance as defined in the framework of the cdbw cluster validation index (and meant to be used in that context).

Usage

Arguments

x	matrix. Euclidean dataset.
xcen	mean vector of cluster.
clustering	vector of integers with length $= nrow(x)$; indicating the cluster for each observation.
cluster	integer. Number of cluster to be treated.
r	integer. Number of representatives.
р	integer. Number of dimensions.
n	integer. Number of observations.
nc	integer. Number of observations in cluster.

Value

List with components

repc	vector of index of representatives (out of all observations).
repx	vector of index of representatives (out of only the observations in cluster).
maxr	number of representatives (this can be smaller than ${\tt r}$ if fewer pairwise different observations are in cluster.
wvar	estimated average within-cluster squared distance to mean.

Author(s)

Christian Hennig <christian.hennig@unibo.it>https://www.unibo.it/sitoweb/christian.hennig/en/

References

Halkidi, M. and Vazirgiannis, M. (2008) A density-based cluster validity approach using multi-representatives. *Pattern Recognition Letters* 29, 773-786.

Halkidi, M., Vazirgiannis, M. and Hennig, C. (2015) Method-independent indices for cluster validation. In C. Hennig, M. Meila, F. Murtagh, R. Rocci (eds.) *Handbook of Cluster Analysis*, CRC Press/Taylor & Francis, Boca Raton.

See Also

cdbw

Examples

```
options(digits=3)
iriss <- as.matrix(iris[c(1:5,51:55,101:105),-5])
irisc <- as.numeric(iris[c(1:5,51:55,101:105),5])
findrep(iriss,colMeans(iriss),irisc,cluster=1,r=2)</pre>
```

fixmahal

Mahalanobis Fixed Point Clusters

Description

Computes Mahalanobis fixed point clusters (FPCs), i.e., subsets of the data, which consist exactly of the non-outliers w.r.t. themselves, and may be interpreted as generated from a homogeneous normal population. FPCs may overlap, are not necessarily exhausting and do not need a specification of the number of clusters.

Note that while fixmahal has lots of parameters, only one (or few) of them have usually to be specified, cf. the examples. The philosophy is to allow much flexibility, but to always provide sensible defaults.

Usage

Arguments

dat something that can be coerced to a numerical matrix or vector. Data matrix, rows

are points, columns are variables. fpclusters.rfpc does not need specification

of dat if fixmahal has been run with ind.storage=TRUE.

n optional positive integer. Number of cases.

p optional positive integer. Number of independent variables.

method a string. method="classical" means 0-1 weighting of observations by Maha-

lanobis distances and use of the classical normal covariance estimator. method="ml" uses the ML-covariance estimator (division by n instead of n-1) This is used in Hennig and Christlieb (2002). method can also be "mcd" or "mve", to enforce the use of robust centers and covariance matrices, see cov.rob. This is experimental, not recommended at the moment, may be very slowly and requires library lqs. The default is method="fuzzy", where weighted means and covariance matrices are used (Hennig, 2005). The weights are computed by wfu, i.e., a function that is constant 1 for arguments smaller than ca, 0 for arguments larger than ca2 and continuously linear in between. Convergence is only proven

for method="ml" up to now.

cgen optional string. "fixed" means that the same tuning constant ca is used for all

iterations. "auto" means that ca is generated dependently on the size of the

current data subset in each iteration by cmahal. This is experimental.

ca optional positive number. Tuning constant, specifying required cluster separa-

tion. By default determined as calpha-quantile of the chisquared distribution

with p degrees of freedom.

ca2 optional positive number. Second tuning constant needed if method="fuzzy".

By default determined as calpha2-quantile of the chisquared distribution with

p degrees of freedom.

calpha number between 0 and 1. See ca.

calpha2 number between 0 and 1, larger than calpha. See ca2.

pointit optional logical. If TRUE, subset fixed point algorithms are started from initial

configurations, which are built around single points of the dataset, cf. mahalconf.

Otherwise, initial configurations are only specified by init.group.

subset optional positive integer smaller or equal than n. Initial configurations for the

fixed point algorithm (cf. mahalconf) are built from a subset of subset points

from the data. No effect if pointit=FALSE. Default: all points.

nc1 optional positive integer. Tuning constant needed by cmahal to generate ca

automatically. Only needed for cgen="auto".

startn optional positive integer. Size of the initial configurations. The default value

is chosen to prevent that small meaningless FPCs are found, but it should be decreased if clusters of size smaller than the default value are of interest.

mnc optional positive integer. Minimum size of clusters to be reported.

mer optional nonnegative number. FPCs (groups of them, respectively, see details)

are only reported as stable if the ratio of the number of their findings to their number of points exceeds mer. This holds under pointit=TRUE and subset=n. For subset<n, the ratio is adjusted, but for small subset, the results may ex-

tremely vary and have to be taken with care.

distcut optional value between 0 and 1. A similarity measure between FPCs, given

in Hennig (2002), and the corresponding Single Linkage groups of FPCs with similarity larger than distcut are computed. A single representative FPC is

selected for each group.

maxit optional integer. Maximum number of iterations per algorithm run (usually an

FPC is found much earlier).

iter positive number. Algorithm stops when difference between subsequent weight

vectors is smaller than iter. Only needed for method="fuzzy".

init.group optional list of logical vectors of length n. Every vector indicates a starting con-

figuration for the fixed point algorithm. This can be used for datasets with high dimension, where the vectors of init.group indicate cluster candidates found by graphical inspection or background knowledge, as in Hennig and Christlieb

(2002).

ind.storage optional logical. If TRUE, then all indicator vectors of found FPCs are given in

the value of fixmahal. May need lots of memory, but is a bit faster.

countmode optional positive integer. Every countmode algorithm runs fixmahal shows a

message.

plot optional string. If "start", you get a scatterplot of the first two variables to

highlight the initial configuration, "iteration" generates such a plot at each iteration, "both" does both (this may be very time consuming). The default is

"none".

object of class mfpc, output of fixmahal.

x object of class mfpc, output of fixmahal.

maxnc positive integer. Maximum number of FPCs to be reported.

no positive integer. Number of the representative FPC to be plotted.

bw	optional logical. If TRUE, plot is black/white, FPC is indicated by different symbol. Else FPC is indicated red.
main	plot title.
xlab	label for x-axis. If NULL, a default text is used.
ylab	label for y-axis. If NULL, a default text is used.
pch	plotting symbol, see par. If NULL, the default is used.
col	plotting color, see par. If NULL, the default is used.
gv	logical vector (or, with method="fuzzy", vector of weights between 0 and 1) of length n. Indicates the initial configuration for the fixed point algorithm.
	additional parameters to be passed to plot (no effects elsewhere).

Details

A (crisp) Mahalanobis FPC is a data subset that reproduces itself under the following operation: Compute mean and covariance matrix estimator for the data subset, and compute all points of the dataset for which the squared Mahalanobis distance is smaller than ca.

Fixed points of this operation can be considered as clusters, because they contain only non-outliers (as defined by the above mentioned procedure) and all other points are outliers w.r.t. the subset.

The current default is to compute fuzzy Mahalanobis FPCs, where the points in the subset have a membership weight between 0 and 1 and give rise to weighted means and covariance matrices. The new weights are then obtained by computing the weight function wfu of the squared Mahalanobis distances, i.e., full weight for squared distances smaller than ca, zero weight for squared distances larger than ca2 and decreasing weights (linear function of squared distances) in between.

A fixed point algorithm is started from the whole dataset, algorithms are started from the subsets specified in init.group, and further algorithms are started from further initial configurations as explained under subset and in the function mahalconf.

Usually some of the FPCs are unstable, and more than one FPC may correspond to the same significant pattern in the data. Therefore the number of FPCs is reduced: A similarity matrix is computed between FPCs. Similarity between sets is defined as the ratio between 2 times size of intersection and the sum of sizes of both sets. The Single Linkage clusters (groups) of level distcut are computed, i.e. the connectivity components of the graph where edges are drawn between FPCs with similarity larger than distcut. Groups of FPCs whose members are found often enough (cf. parameter mer) are considered as stable enough. A representative FPC is chosen for every Single Linkage cluster of FPCs according to the maximum expectation ratio ser. ser is the ratio between the number of findings of an FPC and the number of points of an FPC, adjusted suitably if subset<n. Usually only the representative FPCs of stable groups are of interest.

Default tuning constants are taken from Hennig (2005).

Generally, the default settings are recommended for fixmahal. For large datasets, the use of init.group together with pointit=FALSE is useful. Occasionally, mnc and startn may be chosen smaller than the default, if smaller clusters are of interest, but this may lead to too many clusters. Decrease of ca will often lead to too many clusters, even for homogeneous data. Increase of ca will produce only very strongly separated clusters. Both may be of interest occasionally.

Singular covariance matrices during the iterations are handled by solvecov.

summary.mfpc gives a summary about the representative FPCs of stable groups.

plot.mfpc is a plot method for the representative FPC of stable group no. no. It produces a scatterplot, where the points belonging to the FPC are highlighted, the mean is and for p<3 also the

region of the FPC is shown. For p>=3, the optimal separating projection computed by batcoord is shown.

fpclusters.mfpc produces a list of indicator vectors for the representative FPCs of stable groups. fpmi is called by fixmahal for a single fixed point algorithm and will usually not be executed alone.

Value

sto

fixmahal returns an object of class mfpc. This is a list containing the components nc,g,means,covs,nfound,er,tsc,ncol summary.mfpc returns an object of class summary.mfpc. This is a list containing the components means,covs,stn,stfound,sn,ser,tskip,skc,tsc,sim,ca,ca2,calpha,mer,method,cgen,pointit.

fpclusters.mfpc returns a list of indicator vectors for the representative FPCs of stable groups.

fpmi returns a list with the components mg, covg, md, gv, coll, method, ca.

nc	integer. Number of FPCs.
g	list of logical vectors. Indicator vectors of FPCs. FALSE if ind.storage=FALSE.
means	list of numerical vectors. Means of FPCs. In summary.mfpc, only for representative FPCs of stable groups and sorted according to ser.
covs	list of numerical matrices. Covariance matrices of FPCs. In summary.mfpc, only for representative FPCs of stable groups and sorted according to ser.
nfound	vector of integers. Number of findings for the FPCs.
er	numerical vector. Ratio of number of findings of FPCs to their size. Under pointit=TRUE, this can be taken as a measure of stability of FPCs.
tsc	integer. Number of algorithm runs leading to too small or too seldom found FPCs.
ncoll	integer. Number of algorithm runs where collinear covariance matrices occurred.
skc	integer. Number of skipped clusters.
grto	vector of integers. Numbers of FPCs to which algorithm runs led, which were started by init.group.
imatrix	vector of integers. Size of intersection between FPCs. See sseg.
smatrix	numerical vector. Similarities between FPCs. See sseg.
stn	integer. Number of representative FPCs of stable groups. In summary.mfpc, sorted according to ser.
stfound	vector of integers. Number of findings of members of all groups of FPCs. In summary.mfpc, sorted according to ser.
ser	numerical vector. Ratio of number of findings of groups of FPCs to their size. Under pointit=TRUE, this can be taken as a measure of stability of FPCs. In summary.mfpc, sorted from largest to smallest.
sfpc	vector of integers. Numbers of representative FPCs of all groups.
ssig	vector of integers of length stn. Numbers of representative FPCs of the stable groups.

vector of integers. Numbers of groups ordered according to largest ser.

struc vector of integers. Number of group an FPC belongs to.

n see arguments.
p see arguments.
method see arguments.
cgen see arguments.

ca see arguments, if cgen has been "fixed". Else numerical vector of length nc

(see below), giving the final values of ca for all FPC. In fpmi, tuning constant

for the iterated FPC.

ca2 see arguments.

cvec numerical vector of length n for cgen="auto". The values for the tuning con-

stant ca corresponding to the cluster sizes from 1 to n.

calpha see arguments.

pointit see arguments.

subset see arguments.

mnc see arguments.

startn see arguments.

mer see arguments.

distcut see arguments.

sn vector of integers. Number of points of representative FPCs. tskip integer. Number of algorithm runs leading to skipped FPCs.

sim vector of integers. Size of intersections between representative FPCs of stable

groups. See sseg.

mg mean vector.

covg covariance matrix.

md Mahalanobis distances.

gv logical (numerical, respectively, if method="fuzzy") indicator vector of iterated

FPC.

coll logical. TRUE means that singular covariance matrices occurred during the itera-

tions.

Author(s)

Christian Hennig <christian.hennig@unibo.it>https://www.unibo.it/sitoweb/christian.hennig/en/

References

Hennig, C. (2002) Fixed point clusters for linear regression: computation and comparison, *Journal of Classification* 19, 249-276.

Hennig, C. (2005) Fuzzy and Crisp Mahalanobis Fixed Point Clusters, in Baier, D., Decker, R., and Schmidt-Thieme, L. (eds.): *Data Analysis and Decision Support*. Springer, Heidelberg, 47-56.

Hennig, C. and Christlieb, N. (2002) Validating visual clusters in large datasets: Fixed point clusters of spectral features, *Computational Statistics and Data Analysis* 40, 723-739.

See Also

```
fixreg for linear regression fixed point clusters.

mahalconf, wfu, cmahal for computation of initial configurations, weights, tuning constants.

sseg for indexing the similarity/intersection vectors computed by fixmahal.

batcoord, cov.rob, solvecov, cov.wml, plotcluster for computation of projections, (inverted) covariance matrices, plotting.

rFace for generation of example data, see below.
```

```
options(digits=2)
set.seed(20000)
face <- rFace(400,dMoNo=2,dNoEy=0, p=3)
# The first example uses grouping information via init.group.
initg <- list()</pre>
grface <- as.integer(attr(face, "grouping"))</pre>
for (i in 1:5) initg[[i]] <- (grface==i)</pre>
ff0 <- fixmahal(face, pointit=FALSE, init.group=initg)</pre>
summary(ff0)
cff0 <- fpclusters(ff0)</pre>
plot(face, col=1+cff0[[1]])
plot(face, col=1+cff0[[4]]) # Why does this come out as a cluster?
plot(ff0, face, 4) # A bit clearer...
# Without grouping information, examples need more time:
# ff1 <- fixmahal(face)</pre>
# summary(ff1)
# cff1 <- fpclusters(ff1)</pre>
# plot(face, col=1+cff1[[1]])
# plot(face, col=1+cff1[[6]]) # Why does this come out as a cluster?
# plot(ff1, face, 6) # A bit clearer...
# ff2 <- fixmahal(face,method="ml")</pre>
# summary(ff2)
# ff3 <- fixmahal(face,method="ml",calpha=0.95,subset=50)</pre>
# summary(ff3)
## ...fast, but lots of clusters. mer=0.3 may be useful here.
# set.seed(3000)
# face2 <- rFace(400,dMoNo=2,dNoEy=0)</pre>
# ff5 <- fixmahal(face2)</pre>
# summary(ff5)
## misses right eye of face data; with p=6,
## initial configurations are too large for 40 point clusters
# ff6 <- fixmahal(face2, startn=30)</pre>
# summary(ff6)
# cff6 <- fpclusters(ff6)</pre>
# plot(face2, col=1+cff6[[3]])
# plot(ff6, face2, 3)
\# x \leftarrow c(1,2,3,6,6,7,8,120)
# ff8 <- fixmahal(x)</pre>
# summary(ff8)
# ...dataset a bit too small for the defaults...
```

```
# ff9 <- fixmahal(x, mnc=3, startn=3)
# summary(ff9)</pre>
```

fixreg

Linear Regression Fixed Point Clusters

Description

Computes linear regression fixed point clusters (FPCs), i.e., subsets of the data, which consist exactly of the non-outliers w.r.t. themselves, and may be interpreted as generated from a homogeneous linear regression relation between independent and dependent variable. FPCs may overlap, are not necessarily exhausting and do not need a specification of the number of clusters.

Note that while fixreg has lots of parameters, only one (or few) of them have usually to be specified, cf. the examples. The philosophy is to allow much flexibility, but to always provide sensible defaults.

Usage

```
fixreg(indep=rep(1,n), dep, n=length(dep),
                    p=ncol(as.matrix(indep)),
                    ca=NA, mnc=NA, mtf=3, ir=NA, irnc=NA,
                    irprob=0.95, mncprob=0.5, maxir=20000, maxit=5*n,
                    distcut=0.85, init.group=list(),
                    ind.storage=FALSE, countmode=100,
                    plot=FALSE)
## S3 method for class 'rfpc'
summary(object, ...)
## S3 method for class 'summary.rfpc'
print(x, maxnc=30, ...)
## S3 method for class 'rfpc'
plot(x, indep=rep(1,n), dep, no, bw=TRUE,
                      main=c("Representative FPC No. ",no),
                      xlab="Linear combination of independents",
                      ylab=deparse(substitute(indep)),
                      xlim=NULL, ylim=range(dep),
                      pch=NULL, col=NULL,...)
## S3 method for class 'rfpc'
fpclusters(object, indep=NA, dep=NA, ca=object$ca, ...)
rfpi(indep, dep, p, gv, ca, maxit, plot)
```

Arguments

8	
indep	numerical matrix or vector. Independent variables. Leave out for clustering one-dimensional data. fpclusters.rfpc does not need specification of indep if fixreg was run with ind.storage=TRUE.
dep	numerical vector. Dependent variable. fpclusters.rfpc does not need specification of dep if fixreg was run with ind.storage=TRUE.
n	optional positive integer. Number of cases.
р	optional positive integer. Number of independent variables.
ca	optional positive number. Tuning constant, specifying required cluster separation. By default determined automatically as a function of n and p, see function can, Hennig (2002a).
mnc	optional positive integer. Minimum size of clusters to be reported. By default determined automatically as a function of mncprob. See Hennig (2002a).
mtf	optional positive integer. FPCs must be found at least mtf times to be reported by summary.rfpc.
ir	optional positive integer. Number of algorithm runs. By default determined automatically as a function of n, p, irnc, irprob, mtf, maxir. See function itnumber and Hennig (2002a).
irnc	optional positive integer. Size of the smallest cluster to be found with approximated probability irprob.
irprob	optional value between 0 and 1. Approximated probability for a cluster of size irnc to be found.
mncprob	optional value between 0 amd 1. Approximated probability for a cluster of size $$ mnc to be found.
maxir	optional integer. Maximum number of algorithm runs.
maxit	optional integer. Maximum number of iterations per algorithm run (usually an FPC is found much earlier).
distcut	optional value between 0 and 1. A similarity measure between FPCs, given in Hennig (2002a), and the corresponding Single Linkage groups of FPCs with similarity larger than distcut are computed. A single representative FPC is selected for each group.
init.group	optional list of logical vectors of length n. Every vector indicates a starting configuration for the fixed point algorithm. This can be used for datasets with high dimension, where the vectors of init.group indicate cluster candidates found by graphical inspection or background knowledge.
ind.storage	optional logical. If TRUE, then all indicator vectors of found FPCs are given in the value of fixreg. May need lots of memory, but is a bit faster.
countmode	optional positive integer. Every count mode algorithm runs fixreg shows a message.
plot	optional logical. If TRUE, you get a scatterplot of first independent vs. dependent variable at each iteration.
object	object of class rfpc, output of fixreg.

x	object of class rfpc, output of fixreg.
maxnc	positive integer. Maximum number of FPCs to be reported.
no	positive integer. Number of the representative FPC to be plotted.
bw	optional logical. If TRUE, plot is black/white, FPC is indicated by different symbol. Else FPC is indicated red.
main	plot title.
xlab	label for x-axis.
ylab	label for y-axis.
xlim	plotted range of x-axis. If NULL, the range of the plotted linear combination of independent variables is used.
ylim	plotted range of y-axis.
pch	plotting symbol, see par. If NULL, the default is used.
col	plotting color, see par. If NULL, the default is used.
gv	logical vector of length n . Indicates the initial configuration for the fixed point algorithm.
	additional parameters to be passed to plot (no effects elsewhere).

Details

A linear regression FPC is a data subset that reproduces itself under the following operation:

Compute linear regression and error variance estimator for the data subset, and compute all points of the dataset for which the squared residual is smaller than ca times the error variance.

Fixed points of this operation can be considered as clusters, because they contain only non-outliers (as defined by the above mentioned procedure) and all other points are outliers w.r.t. the subset.

fixreg performs ir fixed point algorithms started from random subsets of size p+2 to look for FPCs. Additionally an algorithm is started from the whole dataset, and algorithms are started from the subsets specified in init.group.

Usually some of the FPCs are unstable, and more than one FPC may correspond to the same significant pattern in the data. Therefore the number of FPCs is reduced: FPCs with less than mnc points are ignored. Then a similarity matrix is computed between the remaining FPCs. Similarity between sets is defined as the ratio between 2 times size of intersection and the sum of sizes of both sets. The Single Linkage clusters (groups) of level distcut are computed, i.e. the connectivity components of the graph where edges are drawn between FPCs with similarity larger than distcut. Groups of FPCs whose members are found mtf times or more are considered as stable enough. A representative FPC is chosen for every Single Linkage cluster of FPCs according to the maximum expectation ratio ser. ser is the ratio between the number of findings of an FPC and the estimated expectation of the number of findings of an FPC of this size, called *expectation ratio* and computed by clusexpect.

Usually only the representative FPCs of stable groups are of interest.

The choice of the involved tuning constants such as ca and ir is discussed in detail in Hennig (2002a). Statistical theory is presented in Hennig (2003).

Generally, the default settings are recommended for fixreg. In cases where they lead to a too large number of algorithm runs (e.g., always for p>4), the use of init.group together with mtf=1 and ir=0 is useful. Occasionally, irnc may be chosen smaller than the default, if smaller clusters are of interest, but this may lead to too many clusters and too many algorithm runs. Decrease of ca will

often lead to too many clusters, even for homogeneous data. Increase of ca will produce only very strongly separated clusters. Both may be of interest occasionally.

rfpi is called by fixreg for a single fixed point algorithm and will usually not be executed alone.

summary.rfpc gives a summary about the representative FPCs of stable groups.

plot.rfpc is a plot method for the representative FPC of stable group no. no. It produces a scatterplot of the linear combination of independent variables determined by the regression coefficients of the FPC vs. the dependent variable. The regression line and the region of non-outliers determined by ca are plotted as well.

fpclusters.rfpc produces a list of indicator vectors for the representative FPCs of stable groups.

Value

nc

fixreg returns an object of class rfpc. This is a list containing the components nc,g,coefs,vars,nfound,er,tsc,ncoll,g summary.rfpc returns an object of class summary.rfpc. This is a list containing the components coefs,vars,stfound,stn,sn,ser,tsc,sim,ca,ir,mnc,mtf.

 ${\tt fpclusters.rfpc}\ returns\ a\ list\ of\ indicator\ vectors\ for\ the\ representative\ FPCs\ of\ stable\ groups.$

rfpi returns a list with the components coef, var, g, coll, ca.

integer. Number of FPCs.

110	megen rumber of 11 es.
g	list of logical vectors. Indicator vectors of FPCs. FALSE if ind. storage=FALSE.
coefs	list of numerical vectors. Regression coefficients of FPCs. In summary.rfpc, only for representative FPCs of stable groups and sorted according to stfound.
vars	list of numbers. Error variances of FPCs. In summary.rfpc, only for representative FPCs of stable groups and sorted according to stfound.
nfound	vector of integers. Number of findings for the FPCs.
er	numerical vector. Expectation ratios of FPCs. Can be taken as a stability measure.
tsc	integer. Number of algorithm runs leading to too small or too seldom found \ensuremath{FPCs} .
ncoll	integer. Number of algorithm runs where collinear regressor matrices occurred.
grto	vector of integers. Numbers of FPCs to which algorithm runs led, which were started by ${\tt init.group}$.
imatrix	vector of integers. Size of intersection between FPCs. See sseg.
smatrix	numerical vector. Similarities between FPCs. See sseg.
stn	integer. Number of representative FPCs of stable groups. In summary.rfpc sorted according to stfound.
stfound	vector of integers. Number of findings of members of all groups of FPCs. In summary.rfpc sorted according to stfound.
sfpc	vector of integers. Numbers of representative FPCs.
ssig	vector of integers. As sfpc, but only for stable groups.
sto	vector of integers. Number of representative FPC of most, 2nd most,, often found group of FPCs.

struc	vector of integers. Number of group an FPC belongs to.
n	see arguments.
р	see arguments.
ca	see arguments.
ir	see arguments.
mnc	see arguments.
mtf	see arguments.
distcut	see arguments.
sn	vector of integers. Number of points of representative FPCs.
ser	numerical vector. Expectation ratio for stable groups.
sim	vector of integers. Size of intersections between representative FPCs of stable groups. See sseg.
coef	vector of regression coefficients.
var	error variance.
g	logical indicator vector of iterated FPC.
coll	logical. TRUE means that singular covariance matrices occurred during the itera-

Author(s)

Christian Hennig <christian.hennig@unibo.it>https://www.unibo.it/sitoweb/christian.hennig/en/

References

Hennig, C. (2002) Fixed point clusters for linear regression: computation and comparison, *Journal of Classification* 19, 249-276.

Hennig, C. (2003) Clusters, outliers and regression: fixed point clusters, *Journal of Multivariate Analysis* 86, 183-212.

See Also

fixmahal for fixed point clusters in the usual setup (non-regression).

regmix for clusterwiese linear regression by mixture modeling ML.

can, itnumber for computation of the default settings.

tions.

clusexpect for estimation of the expected number of findings of an FPC of given size.

itnumber for the generation of the number of fixed point algorithms.

minsize for the smallest FPC size to be found with a given probability..

sseg for indexing the similarity/intersection vectors computed by fixreg.

flexmixedruns 89

Examples

```
set.seed(190000)
options(digits=3)
data(tonedata)
attach(tonedata)
tonefix <- fixreg(stretchratio,tuned,mtf=1,ir=20)</pre>
summary(tonefix)
# This is designed to have a fast example; default setting would be better.
# If you want to see more (and you have a bit more time),
# try out the following:
## Not run:
 set.seed(1000)
 tonefix <- fixreg(stretchratio,tuned)</pre>
# Default - good for these data
 summary(tonefix)
 plot(tonefix,stretchratio,tuned,1)
 plot(tonefix,stretchratio,tuned,2)
 plot(tonefix, stretchratio, tuned, 3, bw=FALSE, pch=5)
 toneclus <- fpclusters(tonefix,stretchratio,tuned)</pre>
 plot(stretchratio, tuned, col=1+toneclus[[2]])
 tonefix2 <- fixreg(stretchratio,tuned,distcut=1,mtf=1,countmode=50)</pre>
# Every found fixed point cluster is reported,
# no matter how instable it may be.
 summary(tonefix2)
 tonefix3 <- fixreg(stretchratio,tuned,ca=7)</pre>
# ca defaults to 10.07 for these data.
 summary(tonefix3)
 subset <- c(rep(FALSE,5),rep(TRUE,24),rep(FALSE,121))</pre>
 tonefix4 <- fixreg(stretchratio, tuned,</pre>
                     mtf=1,ir=0,init.group=list(subset))
 summary(tonefix4)
## End(Not run)
```

flexmixedruns

Fitting mixed Gaussian/multinomial mixtures with flexmix

Description

flexmixedruns fits a latent class mixture (clustering) model where some variables are continuous and modelled within the mixture components by Gaussian distributions and some variables are categorical and modelled within components by independent multinomial distributions. The fit is by maximum likelihood estimation computed with the EM-algorithm. The number of components can be estimated by the BIC.

Note that at least one categorical variable is needed, but it is possible to use data without continuous variable.

90 flexmixedruns

Usage

flexmixedruns(x,diagonal=TRUE,xvarsorted=TRUE,

continuous, discrete, ppdim=NULL, initial.cluster=NULL, simruns=20, n.cluster=1:20, verbose=TRUE, recode=TRUE, allout=TRUE, control=list(minprior=0.001), silent=TRUE)

Arguments

x data matrix or data frame. The data need to be organised case-wise, i.e., if there are categorical variables only, and 15 cases with values c(1,1,2) on the 3 variables, the data matrix needs 15 rows with values 1 1 2. (Categorical variables could take numbers or strings or anything that can be coerced to factor levels as

values.)

diagonal logical. If TRUE, Gaussian models are fitted restricted to diagonal covariance

matrices. Otherwise, covariance matrices are unrestricted. TRUE is consistent with the "within class independence" assumption for the multinomial variables.

xvarsorted logical. If TRUE, the continuous variables are assumed to be the first ones, and

the categorical variables to be behind them.

continuous vector of integers giving positions of the continuous variables. If xvarsorted=TRUE,

a single integer, number of continuous variables.

discrete vector of integers giving positions of the categorical variables. If xvarsorted=TRUE,

a single integer, number of categorical variables.

ppdim vector of integers specifying the number of (in the data) existing categories for

each categorical variable. If recode=TRUE, this can be omitted and is computed

automatically.

initial.cluster

this corresponds to the cluster parameter in flexmix and should only be specified if simruns=1 and n.cluster is a single number. Either a matrix with n.cluster columns of initial cluster membership probabilities for each observation; or a factor or integer vector with the initial cluster assignments of observations at the start of the EM algorithm. Default is random assignment into

n.cluster clusters.

simruns integer. Number of starts of the EM algorithm with random initialisation in order

to find a good global optimum.

n.cluster vector of integers, numbers of components (the optimum one is found by min-

imising the BIC).

verbose logical. If TRUE, some information about the different runs of the EM algorithm

is given out.

recode logical. If TRUE, the function discrete.recode is applied in order to recode

categorical data so that the 1cmixed-method can use it. Only set this to FALSE if your data already has that format (even it that case, TRUE doesn't do harm). If

recode=FALSE, the categorical variables are assumed to be coded 1,2,3,...

allout logical. If TRUE, the regular flexmix-output is given out for every single number

of clusters, which can create a huge output object.

control list of control parameters for flexmix, for details see the help page of FLXcontrol-class.

flexmixedruns 91

silent logical. This is passed on to the try-function. If FALSE, error messages from

failed runs of flexmix are suppressed. (The information that a flexmix-error

occurred is still given out if verbose=TRUE).

Details

Sometimes flexmix produces errors because of degenerating covariance matrices, too small clusters etc. flexmixedruns tolerates these and treats them as non-optimal runs. (Higher simruns or different control may be required to get a valid solution.)

General documentation on flexmix can be found in Friedrich Leisch's "FlexMix: A General Framework for Finite Mixture Models and Latent Class Regression in R", https://CRAN.R-project.org/package=flexmix

Value

A list with components

optsummary summary object for flexmix object with optimal number of components.

optimalk optimal number of components.

errcount vector with numbers of EM runs for each number of components that led to

flexmix errors.

flexout if allout=TRUE, list of flexmix output objects for all numbers of components,

for details see the help page of flexmix-class. Slots that can be used include for example cluster and components. So if fo is the flexmixedruns-output object, fo\$flexout[[fo\$optimalk]]@cluster gives a component number vec-

tor for the observations (maximum posterior rule), and fo\$flexout[[fo\$optimalk]]@components

gives the estimated model parameters, which for lcmixed and therefore flexmixedruns

are called

center mean vector
cov covariance matrix

pp list of categorical variable-wise category probabilities

If allout=FALSE, only the flexmix output object for the optimal number of com-

ponents, i.e., the [[fo\$optimalk]] indexing above can then be omitted.

bicvals vector of values of the BIC for each number of components.

ppdim vector of categorical variable-wise numbers of categories.

discretelevels list of levels of the categorical variables belonging to what is treated by flexmixedruns

as category 1, 2, 3 etc.

Author(s)

Christian Hennig <christian.hennig@unibo.it>https://www.unibo.it/sitoweb/christian.hennig/en

References

Hennig, C. and Liao, T. (2013) How to find an appropriate clustering for mixed-type variables with application to socio-economic stratification, *Journal of the Royal Statistical Society, Series C Applied Statistics*, 62, 309-369.

92 fpclusters

See Also

lcmixed, flexmix, FLXcontrol-class, flexmix-class, discrete.recode.

Examples

fpclusters

Extracting clusters from fixed point cluster objects

Description

fpclusters is a generic function which extracts the representative fixed point clusters (FPCs) from FPC objects generated by fixmahal and fixreg. For documentation and examples see fixmahal and fixreg.

Usage

```
fpclusters(object, ...)
```

Arguments

```
object of class rfpc or mfpc.... further arguments depending on the method.
```

Value

a list of logical or numerical vectors indicating or giving the weights of the cluster memberships.

Author(s)

```
Christian Hennig <christian.hennig@unibo.it>https://www.unibo.it/sitoweb/christian.hennig/en/
```

See Also

```
fixmahal, fixreg
```

itnumber 93

itnumber	Number of regression fixed point cluster iterations
----------	---

Description

Computes the number of fixed point iterations needed by fixreg to find mtf times a fixed point cluster (FPC) of size cn with an approximated probability of prob.

Thought for use within fixreg.

Usage

```
itnumber(n, p, cn, mtf, prob = 0.95, maxir = 20000)
```

Arguments

n	positive integer. Total number of points.
р	positive integer. Number of independent variables.
cn	positive integer smaller or equal to n. Size of the FPC.
mtf	positive integer.
prob	number between 0 and 1.
maxir	positive integer. itnumber is set to this value if it would otherwise be larger.

Details

The computation is based on the binomial distribution with probability given by clusexpect with ir=1.

Value

An integer.

Author(s)

Christian Hennig <christian.hennig@unibo.it>https://www.unibo.it/sitoweb/christian.hennig/en/

References

Hennig, C. (2002) Fixed point clusters for linear regression: computation and comparison, *Journal of Classification* 19, 249-276.

See Also

```
fixreg, clusexpect
```

```
itnumber(500,4,150,2)
```

94 jittervar

jittervar

Jitter variables in a data matrix

Description

Jitters some variables in a data matrix.

Usage

```
jittervar(x,jitterv=NULL,factor=1)
```

Arguments

x data matrix or data frame.

jitterv vector of numbers of variables to be jittered.

factor numeric. Passed on to jitter. See the documentation there. The higher, the

more jittering.

Value

data matrix or data frame with jittered variables.

Author(s)

Christian Hennig <christian.hennig@unibo.it>https://www.unibo.it/sitoweb/christian.hennig/en

See Also

```
jitter
```

```
set.seed(776655)
v1 <- rnorm(20)
v2 <- rnorm(20)
d1 <- sample(1:5,20,replace=TRUE)
d2 <- sample(1:4,20,replace=TRUE)
ldata <- cbind(v1,v2,d1,d2)
jv <- jittervar(ldata,jitterv=3:4)</pre>
```

kmeansCBI

Interface functions for clustering methods

Description

These functions provide an interface to several clustering methods implemented in R, for use together with the cluster stability assessment in clusterboot (as parameter clustermethod; "CBI" stands for "clusterboot interface"). In some situations it could make sense to use them to compute a clustering even if you don't want to run clusterboot, because some of the functions contain some additional features (e.g., normal mixture model based clustering of dissimilarity matrices projected into the Euclidean space by MDS or partitioning around medoids with estimated number of clusters, noise/outlier identification in hierarchical clustering).

Usage

```
kmeansCBI(data,krange,k,scaling=FALSE,runs=1,criterion="ch",...)
hclustCBI(data,k,cut="number",method,scaling=TRUE,noisecut=0,...)
hclusttreeCBI(data,minlevel=2,method,scaling=TRUE,...)
disthclustCBI(dmatrix,k,cut="number",method,noisecut=0,...)
noisemclustCBI(data,G,k,modelNames,nnk,hcmodel=NULL,Vinv=NULL,
                        summary.out=FALSE,...)
distnoisemclustCBI(dmatrix,G,k,modelNames,nnk,
                        hcmodel=NULL, Vinv=NULL, mdsmethod="classical",
                        mdsdim=4, summary.out=FALSE, points.out=FALSE,...)
claraCBI(data,k,usepam=TRUE,diss=inherits(data,"dist"),...)
pamkCBI(data,krange=2:10,k=NULL,criterion="asw", usepam=TRUE,
        scaling=FALSE,diss=inherits(data,"dist"),...)
tclustCBI(data,k,trim=0.05,...)
dbscanCBI(data,eps,MinPts,diss=inherits(data,"dist"),...)
mahalCBI(data,clustercut=0.5,...)
mergenormCBI(data, G=NULL, k=NULL, modelNames=NULL, nnk=0,
                         hcmodel = NULL,
                         Vinv = NULL, mergemethod="bhat",
                         cutoff=0.1,...)
```

```
speccCBI(data,k,...)
pdfclustCBI(data,...)

stupidkcentroidsCBI(dmatrix,k,distances=TRUE)
stupidknnCBI(dmatrix,k)
stupidkfnCBI(dmatrix,k)
stupidkavenCBI(dmatrix,k)
```

Arguments

data a numeric matrix. The data matrix - usually a cases*variables-data matrix.

claraCBI, pamkCBI and dbscanCBI work with an n*n-dissimilarity matrix as

well, see parameter diss.

dmatrix a squared numerical dissimilarity matrix or a dist-object.

k numeric, usually integer. In most cases, this is the number of clusters for meth-

ods where this is fixed. For hclustCBI and disthclustCBI see parameter cut below. Some methods have a k parameter on top of a G or krange parameter for compatibility; k in these cases does not have to be specified but if it is, it is

always a single number of clusters and overwrites G and krange.

scaling either a logical value or a numeric vector of length equal to the number of vari-

ables. If scaling is a numeric vector with length equal to the number of variables, then each variable is divided by the corresponding value from scaling. If scaling is TRUE then scaling is done by dividing the (centered) variables by their root-mean-square, and if scaling is FALSE, no scaling is done before

execution.

runs integer. Number of random initializations from which the k-means algorithm is

started

criterion "ch" or "asw". Decides whether number of clusters is estimated by the Calinski-

Harabasz criterion or by the average silhouette width.

cut either "level" or "number". This determines how cutree is used to obtain a

partition from a hierarchy tree. cut="level" means that the tree is cut at a particular dissimilarity level, cut="number" means that the tree is cut in order to obtain a fixed number of clusters. The parameter k specifies the number of

clusters or the dissimilarity level, depending on cut.

method method for hierarchical clustering, see the documentation of hclust.

noisecut numeric. All clusters of size <=noisecut in the disthclustCBI/hclustCBI-

partition are joined and declared as noise/outliers.

minlevel integer. minlevel=1 means that all clusters in the tree are given out by hclusttreeCBI or disthclusttreeCBI, including one-point clusters (but excluding the cluster with all points). minlevel=2 excludes the one-point clusters. minlevel=3 excludes the two-point cluster which has been merged first, and increasing the value of minlevel by 1 in all further steps means that the remaining earliest formed cluster is excluded. G vector of integers. Number of clusters or numbers of clusters used by mclustBIC. If G has more than one entry, the number of clusters is estimated by the BIC. modelNames vector of string. Models for covariance matrices, see documentation of mclustBIC. integer. Tuning constant for NNclean, which is used to estimate the initial noise nnk for noisemclustCBI and distnoisemclustCBI. See parameter k in the documentation of NNclean. nnk=0 means that no noise component is fitted.

string or NULL. Determines the initialization of the EM-algorithm for mclustBIC.

Documented in hc.

hcmodel

Vinv numeric. See documentation of mclustBIC.

summary.out logical. If TRUE, the result of summary.mclustBIC is added as component

mclustsummary to the output of noisemclustCBI and distnoisemclustCBI.

mdsmethod "classical", "kruskal" or "sammon". Determines the multidimensional scaling

method to compute Euclidean data from a dissimilarity matrix. See cmdscale,

isoMDS and sammon.

mdsdim integer. Dimensionality of MDS solution.

points out logical. If TRUE, the matrix of MDS points is added as component points to the

output of noisemclustCBI.

usepam logical. If TRUE, the function pam is used for clustering, otherwise clara. pam is

better, clara is faster.

diss logical. If TRUE, data will be considered as a dissimilarity matrix. In claraCBI,

this requires usepam=TRUE.

krange vector of integers. Numbers of clusters to be compared.

trim numeric between 0 and 1. Proportion of data points trimmed, i.e., assigned to

noise. See tclust in the tclust package.

eps numeric. The radius of the neighborhoods to be considered by dbscan.

MinPts integer. How many points have to be in a neighborhood so that a point is con-

sidered to be a cluster seed? See documentation of dbscan.

clustercut numeric between 0 and 1. If fixmahal is used for fuzzy clustering, a crisp parti-

tion is generated and points with cluster membership values above clustercut

are considered as members of the corresponding cluster.

mergemethod method for merging Gaussians, passed on as method to mergenormals.

cutoff numeric between 0 and 1, tuning constant for mergenormals.

distances logical (only for stupidkcentroidsCBI). If FALSE, dmatrix is interpreted as

cases&variables data matrix.

.. further parameters to be transferred to the original clustering functions (not re-

quired).

Details

All these functions call clustering methods implemented in R to cluster data and to provide output in the format required by clusterboot. Here is a brief overview. For further details see the help pages of the involved clustering methods.

- **kmeansCBI** an interface to the function kmeansruns calling kmeans for k-means clustering. (kmeansruns allows the specification of several random initializations of the k-means algorithm and estimation of k by the Calinski-Harabasz index or the average silhouette width.)
- **hclustCBI** an interface to the function hclust for agglomerative hierarchical clustering with noise component (see parameter noisecut above). This function produces a partition and assumes a cases*variables matrix as input.
- **hclusttreeCBI** an interface to the function hclust for agglomerative hierarchical clustering. This function gives out all clusters belonging to the hierarchy (upward from a certain level, see parameter minlevel above).
- **disthclustCBI** an interface to the function hclust for agglomerative hierarchical clustering with noise component (see parameter noisecut above). This function produces a partition and assumes a dissimilarity matrix as input.
- noisemclustCBI an interface to the function mclustBIC, for normal mixture model based clustering. Warning: mclustBIC often has problems with multiple points. In clusterboot, it is recommended to use this together with multipleboot=FALSE.
- distnoisemclustCBI an interface to the function mclustBIC for normal mixture model based clustering. This assumes a dissimilarity matrix as input and generates a data matrix by multidimensional scaling first. Warning: mclustBIC often has problems with multiple points. In clusterboot, it is recommended to use this together with multipleboot=FALSE.
- **claraCBI** an interface to the functions pam and clara for partitioning around medoids.
- pamkCBI an interface to the function pamk calling pam for partitioning around medoids. The number of clusters is estimated by the Calinski-Harabasz index or by the average silhouette width.
- **tclustCBI** an interface to the function tclust in the tclust package for trimmed Gaussian clustering. This assumes a cases*variables matrix as input.
- **dbscanCBI** an interface to the function dbscan for density based clustering.
- **mahalCBI** an interface to the function fixmahal for fixed point clustering. This assumes a cases*variables matrix as input.
- **mergenormCBI** an interface to the function mergenormals for clustering by merging Gaussian mixture components. Unlike mergenormals, mergenormCBI includes the computation of the initial Gaussian mixture. This assumes a cases*variables matrix as input.
- **speccCBI** an interface to the function specc for spectral clustering. See the specc help page for additional tuning parameters. This assumes a cases*variables matrix as input.
- pdfclustCBI an interface to the function pdfCluster for density-based clustering. See the pdfCluster help page for additional tuning parameters. This assumes a cases*variables matrix as input.
- **stupidkcentroidsCBI** an interface to the function stupidkcentroids for random centroid-based clustering. See the **stupidkcentroids** help page. This can have a distance matrix as well as a cases*variables matrix as input, see parameter distances.

stupidknnCBI an interface to the function stupidknn for random nearest neighbour clustering. See the stupidknn help page. This assumes a distance matrix as input.

stupidkfnCBI an interface to the function stupidkfn for random farthest neighbour clustering. See the stupidkfn help page. This assumes a distance matrix as input.

stupidkavenCBI an interface to the function stupidkaven for random average dissimilarity clustering. See the **stupidkaven** help page. This assumes a distance matrix as input.

Value

All interface functions return a list with the following components (there may be some more, see summary.out and points.out above):

result clustering result, usually a list with the full output of the clustering method (the

precise format doesn't matter); whatever you want to use later.

nc number of clusters. If some points don't belong to any cluster, these are declared

"noise". nc includes the "noise cluster", and there should be another component

nccl, being the number of clusters not including the noise cluster.

clusterlist this is a list consisting of a logical vectors of length of the number of data points

(n) for each cluster, indicating whether a point is a member of this cluster (TRUE) or not. If a noise cluster is included, it should always be the last vector in this

list.

partition an integer vector of length n, partitioning the data. If the method produces a

partition, it should be the clustering. This component is only used for plots, so you could do something like rep(1,n) for non-partitioning methods. If a noise

cluster is included, nc=nccl+1 and the noise cluster is cluster no. nc.

clustermethod a string indicating the clustering method.

The output of some of the functions has further components:

nccl see nc above.

nnk by noisemclustCBI and distnoisemclustCBI, see above.

initnoise logical vector, indicating initially estimated noise by NNclean, called by noisemclustCBI

and distnoisemclustCBI.

noise logical. TRUE if points were classified as noise/outliers by disthclustCBI.

Author(s)

Christian Hennig <christian.hennig@unibo.it>https://www.unibo.it/sitoweb/christian.hennig/en/

See Also

clusterboot, dist, kmeans, kmeansruns, hclust, mclustBIC, pam, pamk, clara, dbscan, fixmahal, tclust, pdfCluster

100 kmeansruns

Examples

```
options(digits=3)
set.seed(20000)
face <- rFace(50,dMoNo=2,dNoEy=0,p=2)
dbs <- dbscanCBI(face,eps=1.5,MinPts=4)
dhc <- disthclustCBI(dist(face),method="average",k=1.5,noisecut=2)
table(dbs$partition,dhc$partition)
dm <- mergenormCBI(face,G=10,modelNames="EEE",nnk=2)
dtc <- tclustCBI(face,6,trim=0.1,restr.fact=500)
table(dm$partition,dtc$partition)</pre>
```

kmeansruns

k-means with estimating k and initialisations

Description

This calls the function kmeans to perform a k-means clustering, but initializes the k-means algorithm several times with random points from the data set as means. Furthermore, it is more robust against the occurrence of empty clusters in the algorithm and it estimates the number of clusters by either the Calinski Harabasz index (calinhara) or average silhouette width (see pam.object). The Duda-Hart test (dudahart2) is applied to decide whether there should be more than one cluster (unless 1 is excluded as number of clusters).

Usage

Arguments

data	A numeric matrix of data, or an object that can be coerced to such a matrix (such as a numeric vector or a data frame with all numeric columns).
krange	integer vector. Numbers of clusters which are to be compared by the average silhouette width criterion. Note: average silhouette width and Calinski-Harabasz can't estimate number of clusters nc=1. If 1 is included, a Duda-Hart test is applied and 1 is estimated if this is not significant.
criterion	one of "asw" or "ch". Determines whether average silhouette width or Calinski-Harabasz is applied.
iter.max	integer. The maximum number of iterations allowed.
runs	integer. Number of starts of the k-means algorithm.
scaledata	logical. If TRUE, the variables are centered and scaled to unit variance before execution.

kmeansruns 101

alpha	numeric between 0 and 1, tuning constant for dudahart2 (only used for 1-cluster test).
critout	logical. If TRUE, the criterion value is printed out for every number of clusters.
plot	logical. If TRUE, every clustering resulting from a run of the algorithm is plotted.
	further arguments to be passed on to kmeans.

Value

The output of the optimal run of the kmeans-function with added components bestk and crit. A list with components

cluster A vector of integers indicating the cluster to which each point is allocated.

centers A matrix of cluster centers.

withinss The within-cluster sum of squares for each cluster.

size The number of points in each cluster.
bestk The optimal number of clusters.

crit Vector with values of the criterion for all used numbers of clusters (0 if num-

ber not tried).

Author(s)

Christian Hennig <christian.hennig@unibo.it>https://www.unibo.it/sitoweb/christian.hennig/en/

References

Calinski, T., and Harabasz, J. (1974) A Dendrite Method for Cluster Analysis, *Communications in Statistics*, 3, 1-27.

Duda, R. O. and Hart, P. E. (1973) Pattern Classification and Scene Analysis. Wiley, New York.

Hartigan, J. A. and Wong, M. A. (1979). A K-means clustering algorithm. *Applied Statistics*, 28, 100-108.

Kaufman, L. and Rousseeuw, P.J. (1990). "Finding Groups in Data: An Introduction to Cluster Analysis". Wiley, New York.

See Also

kmeans, pamk, calinhara, dudahart2)

```
options(digits=3)
set.seed(20000)
face <- rFace(50,dMoNo=2,dNoEy=0,p=2)
pka <- kmeansruns(face,krange=1:5,critout=TRUE,runs=2,criterion="asw")
pkc <- kmeansruns(face,krange=1:5,critout=TRUE,runs=2,criterion="ch")</pre>
```

102 Icmixed

lcmixed	flexmix method for mixed Gaussian/multinomial mixtures

Description

lcmixed is a method for the flexmix-function in package flexmix. It provides the necessary information to run an EM-algorithm for maximum likelihood estimation for a latent class mixture (clustering) model where some variables are continuous and modelled within the mixture components by Gaussian distributions and some variables are categorical and modelled within components by independent multinomial distributions. lcmixed can be called within flexmix. The function flexmixedruns is a wrapper function that can be run to apply lcmixed.

Note that at least one categorical variable is needed, but it is possible to use data without continuous variable.

There are further format restrictions to the data (see below in the documentation of continuous and discrete), which can be ignored when running lcmixed through flexmixedruns.

Usage

Arguments

formula	a formula to specify response and explanatory variables. For $1 cmixed$ this always has the form x^1 , where x is a matrix or data frome of all variables to be involved, because regression and explanatory variables are not implemented.
continuous	number of continuous variables. Note that the continuous variables always need to be the first variables in the matrix or data frame.
discrete	number of categorical variables. Always the last variables in the matrix or data frame. Note that categorical variables always must be coded as integers 1,2,3, etc. without interruption.
ppdim	vector of integers specifying the number of (in the data) existing categories for each categorical variable.
diagonal	logical. If TRUE, Gaussian models are fitted restricted to diagonal covariance matrices. Otherwise, covariance matrices are unrestricted. TRUE is consistent with the "within class independence" assumption for the multinomial variables.
pred.ordinal	logical. If FALSE, the within-component predicted value for categorical variables is the probability mode, otherwise it is the mean of the standard $(1,2,3,)$ scores, which may be better for ordinal variables.
printlik	logical. If TRUE, the loglikelihood is printed out whenever computed.

lcmixed 103

Details

The data need to be organised case-wise, i.e., if there are categorical variables only, and 15 cases with values c(1,1,2) on the 3 variables, the data matrix needs 15 rows with values 1 1 2.

General documentation on flexmix methods can be found in Chapter 4 of Friedrich Leisch's "FlexMix: A General Framework for Finite Mixture Models and Latent Class Regression in R", https://CRAN.R-project.org/package=flexmix

Value

An object of class FLXMC (not documented; only used internally by flexmix).

Author(s)

Christian Hennig <christian.hennig@unibo.it>https://www.unibo.it/sitoweb/christian.hennig/en

References

Hennig, C. and Liao, T. (2013) How to find an appropriate clustering for mixed-type variables with application to socio-economic stratification, *Journal of the Royal Statistical Society, Series C Applied Statistics*, 62, 309-369.

See Also

flexmixedruns, flexmix, flexmix-class, discrete.recode, which recodes a dataset into the format required by lcmixed

```
set.seed(112233)
options(digits=3)
require(MASS)
require(flexmix)
data(Cars93)
Cars934 <- Cars93[,c(3,5,8,10)]
cc <-
discrete.recode(Cars934,xvarsorted=FALSE,continuous=c(2,3),discrete=c(1,4))
fcc <- flexmix(cc$data~1,k=2,
model=lcmixed(continuous=2,discrete=2,ppdim=c(6,3),diagonal=TRUE))
summary(fcc)</pre>
```

104 localshape

localshape	Local shape matrix	

Description

This computes a matrix formalising 'local shape', i.e., aggregated standardised variance/covariance in a Mahalanobis neighbourhood of the data points. This can be used for finding clusters when used as one of the covariance matrices in Invariant Coordinate Selection (function ics in package ICS), see Hennig's discussion and rejoinder of Tyler et al. (2009).

Usage

Arguments

xdata objects times variables data matrix.

proportion proportion of points to be considered as neighbourhood.

mscatter "mcd" or "cov"; specified minimum covariance determinant or classical covari-

ance matrix to be used for Mahalanobis distance computation.

mcdalpha if mscatter="mcd", this is the alpha parameter to be used by the MCD covari-

ance matrix, i.e. one minus the asymptotic breakdown point, see covMcd.

covstandard one of "trace", "det" or "none", determining by what constant the pointwise

neighbourhood covariance matrices are standardised. "det" makes the affine

equivariant, as noted in the discussion rejoinder of Tyler et al. (2009).

Value

The local shape matrix.

Author(s)

Christian Hennig <christian.hennig@unibo.it>https://www.unibo.it/sitoweb/christian.hennig/en

References

Tyler, D. E., Critchley, F., Duembgen, L., Oja, H. (2009) Invariant coordinate selection (with discussion). *Journal of the Royal Statistical Society, Series B*, 549-592.

```
options(digits=3)
data(iris)
localshape(iris[,-5],mscatter="cov")
```

mahalanodisc 105

mahalanodisc	Mahalanobis for AWC	

Description

Vector of Mahalanobis distances or their root. For use in awcoord only.

Usage

```
mahalanodisc(x2, mg, covg, modus="square")
```

Arguments

x2 numerical data matrix.

mg mean vector.

covg covariance matrix.

modus "md" (roots of Mahalanobis distances) or "square" (original squared form of

Mahalanobis distances).

Details

The covariance matrix is inverted by use of solvecov, which can be expected to give reasonable results for singular within-class covariance matrices.

Value

vector of (rooted) Mahalanobis distances.

Author(s)

```
Christian Hennig <christian.hennig@unibo.it>https://www.unibo.it/sitoweb/christian.hennig/en/
```

See Also

```
awcoord, solvecov
```

```
options(digits=3)
x <- cbind(rnorm(50),rnorm(50))
mahalanodisc(x,c(0,0),cov(x))
mahalanodisc(x,c(0,0),matrix(0,ncol=2,nrow=2))</pre>
```

106 mahalanofix

mahalanofix	Mahalanobis distances from center of indexed points

Description

Computes the vector of (classical or robust) Mahalanobis distances of all points of x to the center of the points indexed (or weighted) by gv. The latter also determine the covariance matrix.

Thought for use within fixmahal.

Usage

Arguments

_	
x	a numerical data matrix, rows are points, columns are variables.
n	positive integer. Number of points.
р	positive integer. Number of variables.
gv	for mahalanofix a logical or $0\text{-}1$ vector of length n. For mahalanofuz a numerical vector with values between 0 and 1 .
cmax	positive number. used in solvecov if covariance matrix is singular.
method	"ml", "classical", "mcd" or "mve". Method to compute the covariance matrix estimator. See cov.rob, fixmahal.

Details

solvecov is used to invert the covariance matrix. The methods "mcd" and "mve" in mahalanofix do not work properly with point constellations with singular covariance matrices!

Value

A list of the following components:

md	vector of Mahalanobis distances.
mg	mean of the points indexed by gv, weighted mean in mahalanofuz.
covg	covariance matrix of the points indexed by gv, weighted covariance matrix in mahalanofuz.
covinv	covg inverted by solvecov.
coll	logical. If TRUE, covg has been (numerically) singular.

mahalconf 107

Note

Methods "mcd" and "mve" require library lqs.

Author(s)

Christian Hennig <christian.hennig@unibo.it>https://www.unibo.it/sitoweb/christian.hennig/en/

See Also

```
fixmahal, solvecov, cov.rob
```

Examples

mahalconf

Mahalanobis fixed point clusters initial configuration

Description

Generates an initial configuration of startn points from dataset x for the fixmahal fixed point iteration.

Thought only for use within fixmahal.

Usage

```
mahalconf(x, no, startn, covall, plot)
```

Arguments

X	numerical matrix. Rows are points, columns are variables.
no	integer between 1 and nrow(x). Number of the first point of the configuration.
startn	integer between 1 and nrow(x).
covall	covariance matrix for the computation of the first Mahalanobis distances.
plot	a string. If equal to "start" or "both", the first two variables and the first $ncol(x)+1$ points are plotted.

108 mergenormals

Details

mahalconf first chooses the p (number of variables) nearest points to point no. no in terms of the Mahalanobis distance w.r.t. covall, so that there are p+1 points. In every further step, the covariance matrix of the current configuration is computed and the nearest point in terms of the new Mahalanobis distance is added. solvecov is used to invert singular covariance matrices.

Value

A logical vector of length nrow(x).

Author(s)

Christian Hennig <christian.hennig@unibo.it>https://www.unibo.it/sitoweb/christian.hennig/en/

See Also

```
fixmahal, solvecov
```

Examples

```
set.seed(4634)
face <- rFace(600,dMoNo=2,dNoEy=0,p=2)
mahalconf(face,no=200,startn=20,covall=cov(face),plot="start")</pre>
```

mergenormals

Clustering by merging Gaussian mixture components

Description

Clustering by merging Gaussian mixture components; computes all methods introduced in Hennig (2010) from an initial mclust clustering. See details section for details.

Usage

mergenormals 109

Arguments

1	guments	
	xdata	data (something that can be coerced into a matrix).
	mclustsummary	output object from summary.mclustBIC for xdata. Either mclustsummary or all of clustering, probs, muarray, Sigmaarray and z need to be specified (the latter are obtained from mclustsummary if they are not provided). I am not aware of restrictions of the usage of mclustBIC to produce an initial clustering; covariance matrix models can be restricted and a noise component can be included if desired, although I have probably not tested all possibilities.
	clustering	vector of integers. Initial assignment of data to mixture components.
	probs	vector of component proportions (for all components; should sum up to one).
	muarray	matrix of component means (rows).
	Sigmaarray	array of component covariance matrices (third dimension refers to component number).
	Z	matrix of observation- (row-)wise posterior probabilities of belonging to the components (columns).
	method	one of "bhat", "ridge.uni", "ridge.ratio", "demp", "dipuni", "diptantrum", "predictive". See details.
	cutoff	numeric between 0 and 1. Tuning constant, see details and Hennig (2010). If not specified, the default values given in (9) in Hennig (2010) are used.
	by	real between 0 and 1. Interval width for density computation along the ridgeline, used for methods "ridge.uni" and "ridge.ratio". Methods "dipuni" and "diptantrum" require ridgeline computations and use it as well.
	numberstop	integer. If specified, cutoff is ignored and components are merged until the number of clusters specified here is reached.
	renumber	logical. If TRUE merged clusters are renumbered from 1 to their number. If not, numbers of the original clustering are used (numbers of components that were merged into others then will not appear).
	М	integer. Number of times the dataset is divided into two halves. Used if method="predictive".
	• • •	additional optional parameters to pass on to ridgeline.diagnosis or mixpredictive (in mergenormals).
	object	object of class mergenorm, output of mergenormals.
	X	object of class summary.mergenorm, output of summary.mergenorm.

Details

Mixture components are merged in a hierarchical fashion. The merging criterion is computed for all pairs of current clusters and the two clusters with the highest criterion value (lowest, respectively, for method="predictive") are merged. Then criterion values are recomputed for the merged cluster. Merging is continued until the criterion value to merge is below (or above, for method="predictive") the cutoff value. Details are given in Hennig (2010). The following criteria are offered, specified by the method-argument.

[&]quot;ridge.uni" components are only merged if their mixture is unimodal according to Ray and Lindsay's (2005) ridgeline theory, see ridgeline.diagnosis. This ignores argument cutoff.

110 mergenormals

"ridge.ratio" ratio between density minimum between components and minimum of density maxima according to Ray and Lindsay's (2005) ridgeline theory, see ridgeline.diagnosis.

"bhat" Bhattacharyya upper bound on misclassification probability between two components, see bhattacharyya.matrix.

"demp" direct estimation of misclassification probability between components, see Hennig (2010).

"dipuni" this uses method="ridge.ratio" to decide which clusters to merge but stops merging according to the p-value of the dip test computed as in Hartigan and Hartigan (1985), see dip.test.

"diptantrum" as "dipuni", but p-value of dip test computed as in Tantrum, Murua and Stuetzle (2003), see dipp.tantrum.

"predictive" this uses method="demp" to decide which clusters to merge but stops merging according to the value of prediction strength (Tibshirani and Walther, 2005) as computed in mixpredictive.

Value

mergenormals gives out an object of class mergenorm, which is a List with components

clustering integer vector. Final clustering.

clusternumbers vector of numbers of remaining clusters. These are given in terms of the original

clusters even of renumber=TRUE, in which case they may be needed to under-

stand the numbering of some further components, see below.

defunct.components

vector of numbers of components that were "merged away".

valuemerged vector of values of the merging criterion (see details) at which components were

merged.

mergedtonumbers

vector of numbers of clusters to which the original components were merged.

parameters a list, if mclustsummary was provided. Entry no. i refers to number i in

clusternumbers. The list entry i contains the parameters of the original mixture components that make up cluster i, as extracted by extract.mixturepars.

predvalues vector of prediction strength values for clusternumbers from 1 to the number of

components in the original mixture, if method=="predictive". See mixpredictive.

orig.decisionmatrix

square matrix with entries giving the original values of the merging criterion

(see details) for every pair of original mixture components.

new.decisionmatrix

square matrix as orig.decisionmatrix, but with final entries; numbering of rows and columns corresponds to clusternumbers; all entries corresponding to

other rows and columns can be ignored.

probs final cluster values of probs (see arguments) for merged components, gener-

ated by (potentially repeated) execution of mergeparameters out of the original

ones. Numbered according to clusternumbers.

muarray final cluster means, analogous to probs.

Sigmaarray final cluster covariance matrices, analogous to probs.

mergenormals 111

z i	final matrix of	posterior	probabilities of	observations b	belonging to the clusters,
	1 .				

analogous to probs.

noise logical. If TRUE, there was a noise component fitted in the initial mclust cluster-

ing (see help for initialization in mclustBIC). In this case, a cluster number 0 indicates noise. noise is ignored by the merging methods and kept as it was

originally.

method as above. cutoff as above.

summary.mergenorm gives out a list with components clustering, clusternumbers, defunct.components, valuemerged as above, plus onc (original number of components) and mnc (number of clusters after merging).

Author(s)

Christian Hennig <christian.hennig@unibo.it>https://www.unibo.it/sitoweb/christian.hennig/en/

References

J. A. Hartigan and P. M. Hartigan (1985) The Dip Test of Unimodality, *Annals of Statistics*, 13, 70-84.

Hennig, C. (2010) Methods for merging Gaussian mixture components, *Advances in Data Analysis and Classification*, 4, 3-34.

Ray, S. and Lindsay, B. G. (2005) The Topography of Multivariate Normal Mixtures, *Annals of Statistics*, 33, 2042-2065.

Tantrum, J., Murua, A. and Stuetzle, W. (2003) Assessment and Pruning of Hierarchical Model Based Clustering, *Proceedings of the ninth ACM SIGKDD international conference on Knowledge discovery and data mining*, Washington, D.C., 197-205.

Tibshirani, R. and Walther, G. (2005) Cluster Validation by Prediction Strength, *Journal of Computational and Graphical Statistics*, 14, 511-528.

```
require(mclust)
 require(MASS)
 options(digits=3)
 data(crabs)
 dc <- crabs[,4:8]</pre>
 cm <- mclustBIC(crabs[,4:8],G=9,modelNames="EEE")</pre>
 scm <- summary(cm,crabs[,4:8])</pre>
 cmnbhat <- mergenormals(crabs[,4:8],scm,method="bhat")</pre>
 summary(cmnbhat)
 cmndemp <- mergenormals(crabs[,4:8],scm,method="demp")</pre>
  summary(cmndemp)
# Other methods take a bit longer, but try them!
# The values of by and M below are still chosen for reasonably fast execution.
# cmnrr <- mergenormals(crabs[,4:8],scm,method="ridge.ratio",by=0.05)</pre>
# cmd <- mergenormals(crabs[,4:8],scm,method="dip.tantrum",by=0.05)</pre>
# cmp <- mergenormals(crabs[,4:8],scm,method="predictive",M=3)</pre>
```

112 mergeparameters

mergeparameters	New parameters from merging two Gaussian mixture components

Description

Re-computes pointwise posterior probabilities, mean and covariance matrix for a mixture component obtained by merging two mixture components in a Gaussian mixture.

Usage

```
mergeparameters(xdata, j1, j2, probs, muarray,Sigmaarray, z)
```

Arguments

xdata	data (something that can be coerced into a matrix).
j1	integer. Number of first mixture component to be merged.
j2	integer. Number of second mixture component to be merged.
probs	vector of component proportions (for all components; should sum up to one).
muarray	matrix of component means (rows).
Sigmaarray	array of component covariance matrices (third dimension refers to component number).
Z	matrix of observation- (row-)wise posterior probabilities of belonging to the components (columns).

Value

List with components

probs	see above; sum of probabilities for original components j1 and j2 is now probs[j1]. Note that generally, also for the further components, values for the merged component are in place j1 and values in place j2 are not changed. This means that in order to have only the information for the new mixture after merging, the entries
muarray	in places j2 need to be suppressed. see above; weighted mean of means of component j1 and j2 is now in place j1.
illuar r ay	see above, weighted filean of fileans of component j' and j' is now in place j'.
Sigmaarray	see above; weighted covariance matrix handled as above.
Z	see above; original entries for columns j1 and j2 are summed up and now in column j1.

Author(s)

Christian Hennig <christian.hennig@unibo.it>https://www.unibo.it/sitoweb/christian.hennig/en/

minsize 113

References

Hennig, C. (2010) Methods for merging Gaussian mixture components, *Advances in Data Analysis and Classification*, 4, 3-34.

Examples

```
options(digits=3)
set.seed(98765)
require(mclust)
iriss <- iris[sample(150,20),-5]
irisBIC <- mclustBIC(iriss)
siris <- summary(irisBIC,iriss)
probs <- siris$parameters$pro
muarray <- siris$parameters$mean
Sigmaarray <- siris$parameters$variance$sigma
z <- siris$z
mpi <- mergeparameters(iriss,1,2,probs,muarray,Sigmaarray,z)
mpi$probs
mpi$muarray</pre>
```

minsize

Minimum size of regression fixed point cluster

Description

Computes the minimum size of a fixed point cluster (FPC) which is found at least mtf times with approximated probability prob by ir fixed point iterations of fixreg.

Thought for use within fixreg.

Usage

```
minsize(n, p, ir, mtf, prob = 0.5)
```

Arguments

```
n positive integer. Total number of points.

p positive integer. Number of independent variables.

ir positive integer. Number of fixed point iterations.

mtf positive integer.

prob numerical between 0 and 1.
```

Details

The computation is based on the binomial distribution with probability given by clusexpect with ir=1.

114 mixdens

Value

An integer.

Author(s)

Christian Hennig <christian.hennig@unibo.it>https://www.unibo.it/sitoweb/christian.hennig/en/

References

Hennig, C. (2002) Fixed point clusters for linear regression: computation and comparison, *Journal* of Classification 19, 249-276.

See Also

```
fixreg, clusexpect, itnumber
```

Examples

```
minsize(500,4,7000,2)
```

mixdens

Density of multivariate Gaussian mixture, mclust parameterisation

Description

Computes density values for data from a mixture of multivariate Gaussian distributions with parameters based on the way models are specified and parameters are stored in package mclust.

Usage

```
mixdens(modelName,data,parameters)
```

Arguments

modelName an mclust model name. See mclustModelNames.

data matrix; density values are computed for every observation (row).

parameters of Gaussian mixture in the format used in the output of summary.mclustBIC.

Value

Vector of density values for the observations.

Author(s)

```
Christian Hennig <christian.hennig@unibo.it>https://www.unibo.it/sitoweb/christian.hennig/en/
```

mixpredictive 115

Examples

```
set.seed(98765)
require(mclust)
iriss <- iris[sample(150,20),-5]
irisBIC <- mclustBIC(iriss)
siris <- summary(irisBIC,iriss)
round(mixdens(siris$modelName,iriss,siris$parameters),digits=2)</pre>
```

mixpredictive

Prediction strength of merged Gaussian mixture

Description

Computes the prediction strength of clustering by merging Gaussian mixture components, see mergenormals. The predictive strength is defined according to Tibshirani and Walther (2005), carried out as described in Hennig (2010), see details.

Usage

```
mixpredictive(xdata, Gcomp, Gmix, M=50, ...)
```

Arguments

xdata data (something that can be coerced into a matrix).
 Gcomp integer. Number of components of the underlying Gaussian mixture.
 Gmix integer. Number of clusters after merging Gaussian components.
 M integer. Number of times the dataset is divided into two halves.

further arguments that can potentially arrive in calls but are currently not used.

Details

The prediction strength for a certain number of clusters Gmix under a random partition of the dataset in halves A and B is defined as follows. Both halves are clustered with Gmix clusters. Then the points of A are classified to the clusters of B. This is done by use of the maximum a posteriori rule for mixtures as in Hennig (2010), differently from Tibshirani and Walther (2005). A pair of points A in the same A-cluster is defined to be correctly predicted if both points are classified into the same cluster on B. The same is done with the points of B relative to the clustering on A. The prediction strength for each of the clusterings is the minimum (taken over all clusters) relative frequency of correctly predicted pairs of points of that cluster. The final mean prediction strength statistic is the mean over all 2M clusterings.

Value

List with components

predcorr vector of length M with relative frequencies of correct predictions (clusterwise

minimum).

mean.pred mean of predcorr.

116 mvdcoord

Author(s)

Christian Hennig <christian.hennig@unibo.it>https://www.unibo.it/sitoweb/christian.hennig/en/

References

Hennig, C. (2010) Methods for merging Gaussian mixture components, *Advances in Data Analysis and Classification*, 4, 3-34.

Tibshirani, R. and Walther, G. (2005) Cluster Validation by Prediction Strength, *Journal of Computational and Graphical Statistics*, 14, 511-528.

See Also

prediction.strength for Tibshirani and Walther's original method. mergenormals for the clustering method applied here.

Examples

```
set.seed(98765)
iriss <- iris[sample(150,20),-5]
mp <- mixpredictive(iriss,2,2,M=2)</pre>
```

mvdcoord

Mean/variance differences discriminant coordinates

Description

Discriminant projections as defined in Young, Marco and Odell (1987). The principle is to maximize the projection of a matrix consisting of the differences between the means of all classes and the first mean and the differences between the covariance matrices of all classes and the forst covariance matrix.

Usage

```
mvdcoord(xd, clvecd, clnum=1, sphere="mcd", ...)
```

Arguments

xd	the data matrix; a numerical object which can be coerced to a matrix.
clvecd	integer vector of class numbers; length must equal nrow(xd).
clnum	integer. Number of the class to which all differences are computed.
sphere	a covariance matrix or one of "mve", "mcd", "classical", "none". The matrix used for sphering the data. "mcd" and "mve" are robust covariance matrices as implemented in cov.rob. "classical" refers to the classical covariance matrix. "none" means no sphering and use of the raw data.

... no effect

ncoord 117

Value

List with the following components

ev eigenvalues in descending order.

units columns are coordinates of projection basis vectors. New points x can be pro-

jected onto the projection basis vectors by x %*% units

proj projections of xd onto units.

Author(s)

Christian Hennig <christian.hennig@unibo.it>https://www.unibo.it/sitoweb/christian.hennig/en/

References

Young, D. M., Marco, V. R. and Odell, P. L. (1987). Quadratic discrimination: some results on optimal low-dimensional representation, *Journal of Statistical Planning and Inference*, 17, 307-319.

See Also

plotcluster for straight forward discriminant plots. discrproj for alternatives. rFace for generation of the example data used below.

Examples

```
set.seed(4634)
face <- rFace(300,dMoNo=2,dNoEy=0,p=3)
grface <- as.integer(attr(face,"grouping"))
mcf <- mvdcoord(face,grface)
plot(mcf$proj,col=grface)
# ...done in one step by function plotcluster.</pre>
```

ncoord

Neighborhood based discriminant coordinates

Description

Neighborhood based discriminant coordinates as defined in Hastie and Tibshirani (1996) and a robustified version as defined in Hennig (2003). The principle is to maximize the projection of a between classes covariance matrix, which is defined by averaging the between classes covariance matrices in the neighborhoods of all points.

Usage

118 ncoord

Arguments

xd the data matrix; a numerical object which can be coerced to a matrix.

clvecd integer vector of class numbers; length must equal nrow(xd).

nn integer. Number of points which belong to the neighborhood of each point (in-

cluding the point itself).

weighted logical. FALSE corresponds to the original method of Hastie and Tibshirani

(1996). If TRUE, the between classes covariance matrices B are weighted by w/trace B, where w is some weight depending on the sizes of the classes in the neighborhood. Division by trace B reduces the effect of outliers. TRUE coore-

sponds to WNC as defined in Hennig (2003).

sphere a covariance matrix or one of "mve", "mcd", "classical", "none". The matrix

used for sphering the data. "mcd" and "mve" are robust covariance matrices as implemented in cov.rob. "classical" refers to the classical covariance matrix.

"none" means no sphering and use of the raw data.

orderall logical. By default, the neighborhoods are computed by ordering all points each

time. If FALSE, the neighborhoods are computed by selecting nn times the near-

est point from the remaining points, which may be faster sometimes.

countmode optional positive integer. Every countmode algorithm runs noord shows a mes-

sage.

... no effect

Value

List with the following components

ev eigenvalues in descending order.

units columns are coordinates of projection basis vectors. New points x can be pro-

jected onto the projection basis vectors by x %*% units

proj projections of xd onto units.

Author(s)

Christian Hennig <christian.hennig@unibo.it>https://www.unibo.it/sitoweb/christian.hennig/en/

References

Hastie, T. and Tibshirani, R. (1996). Discriminant adaptive nearest neighbor classification. *IEEE Transactions on Pattern Analysis and Machine Intelligence* 18, 607-616.

Hennig, C. (2004) Asymmetric linear dimension reduction for classification. Journal of Computational and Graphical Statistics 13, 930-945 .

Hennig, C. (2005) A method for visual cluster validation. In: Weihs, C. and Gaul, W. (eds.): Classification - The Ubiquitous Challenge. Springer, Heidelberg 2005, 153-160.

neginc 119

See Also

plotcluster for straight forward discriminant plots. discrproj for alternatives. rFace for generation of the example data used below.

Examples

```
set.seed(4634)
face <- rFace(600,dMoNo=2,dNoEy=0)
grface <- as.integer(attr(face,"grouping"))
ncf <- ncoord(face,grface)
plot(ncf$proj,col=grface)
ncf2 <- ncoord(face,grface,weighted=TRUE)
plot(ncf2$proj,col=grface)
# ...done in one step by function plotcluster.</pre>
```

neginc

Neg-entropy normality index for cluster validation

Description

Cluster validity index based on the neg-entropy distances of within-cluster distributions to normal distribution, see Lago-Fernandez and Corbacho (2010).

Usage

```
neginc(x,clustering)
```

Arguments

x something that can be coerced into a numerical matrix. Euclidean dataset.

clustering vector of integers with length =nrow(x); indicating the cluster for each observation.

Value

Index value, see Lago-Fernandez and Corbacho (2010). The lower (i.e., the more negative) the better.

Author(s)

Christian Hennig <christian.hennig@unibo.it>https://www.unibo.it/sitoweb/christian.hennig/en/

References

Lago-Fernandez, L. F. and Corbacho, F. (2010) Normality-based validation for crisp clustering. *Pattern Recognition* 43, 782-795.

120 nselectboot

Examples

```
options(digits=3)
iriss <- as.matrix(iris[c(1:10,51:55,101:105),-5])
irisc <- as.numeric(iris[c(1:10,51:55,101:105),5])
neginc(iriss,irisc)</pre>
```

nselectboot

Selection of the number of clusters via bootstrap

Description

Selection of the number of clusters via bootstrap as explained in Fang and Wang (2012). Several times 2 bootstrap samples are drawn from the data and the number of clusters is chosen by optimising an instability estimation from these pairs.

In principle all clustering methods can be used that have a CBI-wrapper, see clusterboot, kmeansCBI. However, the currently implemented classification methods are not necessarily suitable for all of them, see argument classification.

Usage

Arguments

data something that can be coerced into a matrix. The data matrix - either an n*p-data

matrix (or data frame) or an n*n-dissimilarity matrix (or dist-object).

B integer. Number of resampling runs.

distances logical. If TRUE, the data is interpreted as dissimilarity matrix. If data is a

dist-object, distances=TRUE automatically, otherwise distances=FALSE by default. This means that you have to set it to TRUE manually if data is a dissim-

ilarity matrix.

clustermethod an interface function (the function name, not a string containing the name,

has to be provided!). This defines the clustering method. See the "Details"-section of clusterboot and kmeansCBI for the format. Clustering methods for nselectboot must have a k-argument for the number of clusters and must otherwise follow the specifications in clusterboot. Note that nselectboot won't work with CBI-functions that implicitly already estimate the number of clusters such as pamkCBI; use claraCBI if you want to run it for pam/clara clustering.

classification string. This determines how non-clustered points are classified to given clusters.

Options are explained in classifidist (if distances=TRUE) and classifinp (otherwise). Certain classification methods are connected to certain clustering methods. classification="averagedist" is recommended for average

nselectboot 121

linkage, classification="centroid" is recommended for k-means, clara and pam (with distances it will work with claraCBI only), classification="knn" with nnk=1 is recommended for single linkage and classification="qda" is recommended for Gaussian mixtures with flexible covariance matrices.

centroidname string. Indicates the name of the component of CBIoutput\$result that contains

the cluster centroids in case of classification="centroid", where CBIoutput is the output object of clustermethod. If clustermethod is kmeansCBI or claraCBI, centroids are recognised automatically if centroidname=NULL. If centroidname=NULL and distances=FALSE, cluster means are computed as the

cluster centroids.

krange integer vector; numbers of clusters to be tried.

count logical. If TRUE, numbers of clusters and bootstrap runs are printed.

nnk number of nearest neighbours if classification="knn", see classifdist (if

distances=TRUE) and classifup (otherwise).

largeisgood logical. If TRUE, output component stabk is taken as one minus the original

instability value so that larger values of stabk are better.

... arguments to be passed on to the clustering method.

Value

nselectboot returns a list with components kopt, stabk, stab.

kopt optimal number of clusters.

stabk mean instability values for numbers of clusters (or one minus this if largeisgood=TRUE).

stab matrix of instability values for all bootstrap runs and numbers of clusters.

Author(s)

Christian Hennig <christian.hennig@unibo.it>https://www.unibo.it/sitoweb/christian.hennig/en/

References

Fang, Y. and Wang, J. (2012) Selection of the number of clusters via the bootstrap method. *Computational Statistics and Data Analysis*, 56, 468-477.

See Also

classifdist, classifnp, clusterboot,kmeansCBI

```
set.seed(20000)
face <- rFace(50,dMoNo=2,dNoEy=0,p=2)
nselectboot(dist(face),B=2,clustermethod=disthclustCBI,
method="average",krange=5:7)
nselectboot(dist(face),B=2,clustermethod=claraCBI,</pre>
```

122 pamk

```
classification="centroid",krange=5:7)
nselectboot(face,B=2,clustermethod=kmeansCBI,
    classification="centroid",krange=5:7)
# Of course use larger B in a real application.
```

pamk

Partitioning around medoids with estimation of number of clusters

Description

This calls the function pam or clara to perform a partitioning around medoids clustering with the number of clusters estimated by optimum average silhouette width (see pam.object) or Calinski-Harabasz index (calinhara). The Duda-Hart test (dudahart2) is applied to decide whether there should be more than one cluster (unless 1 is excluded as number of clusters or data are dissimilarities).

Usage

test).

Arguments

data	a data matrix or data frame or something that can be coerced into a matrix, or dissimilarity matrix or object. See pam for more information.
krange	integer vector. Numbers of clusters which are to be compared by the average silhouette width criterion. Note: average silhouette width and Calinski-Harabasz can't estimate number of clusters nc=1. If 1 is included, a Duda-Hart test is applied and 1 is estimated if this is not significant.
criterion	one of "asw", "multiasw" or "ch". Determines whether average silhouette width (as given out by pam/clara, or as computed by distcritmulti if "multiasw" is specified; recommended for large data sets with usepam=FALSE) or Calinski-Harabasz is applied. Note that the original Calinski-Harabasz index is not defined for dissimilarities; if dissimilarity data is run with criterion="ch", the dissimilarity-based generalisation in Hennig and Liao (2013) is used.
usepam	logical. If TRUE, pam is used, otherwise clara (recommended for large datasets with 2,000 or more observations; dissimilarity matrices can not be used with clara).
scaling	either a logical value or a numeric vector of length equal to the number of variables. If scaling is a numeric vector with length equal to the number of variables, then each variable is divided by the corresponding value from scaling. If scaling is TRUE then scaling is done by dividing the (centered) variables by their root-mean-square, and if scaling is FALSE, no scaling is done.
alpha	numeric between 0 and 1, tuning constant for dudahart2 (only used for 1-cluster

pamk 123

diss logical flag: if TRUE (default for dist or dissimilarity-objects), then data will be considered as a dissimilarity matrix (and the potential number of clus-

ters 1 will be ignored). If FALSE, then data will be considered as a matrix of

observations by variables.

critout logical. If TRUE, the criterion value is printed out for every number of clusters.

ns passed on to distcritmulti if criterion="multiasw".
seed passed on to distcritmulti if criterion="multiasw".

... further arguments to be transferred to pam or clara.

Value

A list with components

pamobject The output of the optimal run of the pam-function.

nc the optimal number of clusters.

crit vector of criterion values for numbers of clusters. crit[1] is the p-value of the

Duda-Hart test if 1 is in krange and diss=FALSE.

Note

clara and pam can handle NA-entries (see their documentation) but dudahart2 cannot. Therefore NA should not occur if 1 is in krange.

Author(s)

Christian Hennig <christian.hennig@unibo.it>https://www.unibo.it/sitoweb/christian.hennig/en/

References

Calinski, R. B., and Harabasz, J. (1974) A Dendrite Method for Cluster Analysis, *Communications in Statistics*, 3, 1-27.

Duda, R. O. and Hart, P. E. (1973) Pattern Classification and Scene Analysis. Wiley, New York.

Hennig, C. and Liao, T. (2013) How to find an appropriate clustering for mixed-type variables with application to socio-economic stratification, *Journal of the Royal Statistical Society, Series C Applied Statistics*, 62, 309-369.

Kaufman, L. and Rousseeuw, P.J. (1990). "Finding Groups in Data: An Introduction to Cluster Analysis". Wiley, New York.

See Also

pam, clara distcritmulti

124 piridge

Examples

```
options(digits=3)
set.seed(20000)
face <- rFace(50,dMoNo=2,dNoEy=0,p=2)
pk1 <- pamk(face,krange=1:5,criterion="asw",critout=TRUE)
pk2 <- pamk(face,krange=1:5,criterion="multiasw",ns=2,critout=TRUE)
# "multiasw" is better for larger data sets, use larger ns then.
pk3 <- pamk(face,krange=1:5,criterion="ch",critout=TRUE)</pre>
```

piridge

Ridgeline Pi-function

Description

The Pi-function is given in (6) in Ray and Lindsay, 2005. Equating it to the mixture proportion yields locations of two-component Gaussian mixture density extrema.

Usage

```
piridge(alpha, mu1, mu2, Sigma1, Sigma2, showplot=FALSE)
```

Arguments

alpha sequence of values between 0 and 1 for which the Pi-function is computed.

mu1 mean vector of component 1.
mu2 mean vector of component 2.
Sigma1 covariance matrix of component 1.
Sigma2 covariance matrix of component 2.

showplot logical. If TRUE, the Pi-function is plotted against alpha.

Value

Vector of values of the Pi-function for values of alpha.

Author(s)

```
Christian Hennig <christian.hennig@unibo.it>https://www.unibo.it/sitoweb/christian.hennig/en/
```

References

Ray, S. and Lindsay, B. G. (2005) The Topography of Multivariate Normal Mixtures, *Annals of Statistics*, 33, 2042-2065.

```
q \leftarrow piridge(seq(0,1,0.1),c(1,1),c(2,5),diag(2),diag(2))
```

piridge.zeroes 125

piridge.zeroes	Extrema of two-component Gaussian mixture

Description

By use of the Pi-function in Ray and Lindsay, 2005, locations of two-component Gaussian mixture density extrema or saddlepoints are computed.

Usage

Arguments

prop	proportion of mixture component 1.
mu1	mean vector of component 1.
mu2	mean vector of component 2.
Sigma1	covariance matrix of component 1.
Sigma2	covariance matrix of component 2.
alphamin	minimum alpha value.
alphamax	maximum alpha value.
by	interval between alpha-values where to look for extrema.

Value

```
list with components
```

```
number.zeroes number of zeroes of Pi-function, i.e., extrema or saddlepoints of density. estimated.roots estimated alpha-values at which extrema or saddlepoints occur.
```

Author(s)

Christian Hennig <christian.hennig@unibo.it>https://www.unibo.it/sitoweb/christian.hennig/en/

References

Ray, S. and Lindsay, B. G. (2005) The Topography of Multivariate Normal Mixtures, *Annals of Statistics*, 33, 2042-2065.

```
q \leftarrow piridge.zeroes(0.2,c(1,1),c(2,5),diag(2),diag(2),by=0.1)
```

126 plot.valstat

plot.valstat

Simulation-standardised plot and print of cluster validation statistics

Description

Visualisation and print function for cluster validation output compared to results on simulated random clusterings. The print method can also be used to compute and print an aggregated cluster validation index.

Unlike for many other plot methods, the additional arguments of plot.valstat are essential. print.valstat should make good sense with the defaults, but for computing the aggregate index need to be set.

Usage

Arguments

Х	object of class "valstat", such as sublists stat, qstat, sstat of clusterbenchstats- output.
simobject	list of simulation results as produced by randomclustersim and documented there; typically sublist sim of clusterbenchstats-output.
statistic	one of "avewithin", "mnnd", "variation", "diameter", "gap", "sindex", "minsep", "asw", "dindex validation statistic to be plotted.
xlim	passed on to plot. Default is the range of all involved numbers of clusters, minimum minus 0.5 to maximum plus 0.5.
ylim	passed on to plot.
nmethods	integer. Number of clustering methods to involve (these are those from number

col colours used for the different clustering methods.

1 to nmethods specified in x\$name).

plot.valstat 127

cex passed on to plot.

pch vector of symbols for random clustering results from stupidkcentroids, stupidkfn,

stupidkaven, stupidknn. To be passed on to plot.

simcol vector of colours used for random clustering results in order stupidkcentroids,

stupidkfn, stupidkaven, stupidknn.

shift numeric vector. Indicates the amount to which the results from stupidkcentroids,

stupidkfn, stupidkaven, stupidknn are plotted to the right of their respective

number of clusters (negative numbers plot to the left).

include.othernc

this indicates whether methods should be included that estimated their number of clusters themselves and gave a result outside the standard range as given by x\$minG and x\$maxG. If not NULL, this is a list of integer vectors of length 2. The first number is the number of the clustering method (the order is determined by argument x\$name), the second number is the number of clusters for those methods that estimate the number of clusters themselves and estimated a number outside the standard range. Normally what will be used here, if not NULL, is the output parameter cm\$othernc of clusterbenchstats, see also

cluster.magazine.

statistics vector of character strings specifying the validation statistics that will be in-

cluded in the output (unless you want to restrict the output for some reason, the

default should be fine.

aggregate logical. If TRUE, an aggegate validation statistic will be computed as the weighted

mean of the involved statistic. This requires weights to be set. In order for this to make sense, values of the validation statistics should be comparable, which is achieved by standardisation in clusterbenchstats. Accordingly, x should be the qstat or sstat-component of the clusterbenchstats-output rather than

the stat-component.

weights vector of numericals. Weights for computation of the aggregate statistic in case

that aggregate=TRUE. The order of clustering methods corresponding to the

weight vector is given by x\$name.

digits minimal number of significant digits, passed on to print. table.

... no effect.

Details

Whereas print.valstat, at least with aggregate=TRUE makes more sense for the qstat or sstat-component of the clusterbenchstats-output rather than the stat-component, plot.valstat should be run with the stat-component if simobject is specified, because the simulated cluster validity statistics are unstandardised and need to be compared with unstandardised values on the dataset of interest.

print.valstat will print all values for all validation indexes and the aggregated index (in case of aggregate=TRUE and set weights will be printed last.

Value

print.valstats returns the results table as invisible object.

128 plotcluster

Author(s)

Christian Hennig <christian.hennig@unibo.it>https://www.unibo.it/sitoweb/christian.hennig/en/

References

Hennig, C. (2019) Cluster validation by measurement of clustering characteristics relevant to the user. In C. H. Skiadas (ed.) *Data Analysis and Applications 1: Clustering and Regression, Modeling-estimating, Forecasting and Data Mining, Volume 2*, Wiley, New York 1-24, https://arxiv.org/abs/1703.09282

Akhanli, S. and Hennig, C. (2020) Calibrating and aggregating cluster validity indexes for context-adapted comparison of clusterings. *Statistics and Computing*, 30, 1523-1544, https://link.springer.com/article/10.1007/s11222-020-09958-2, https://arxiv.org/abs/2002.01822

See Also

clusterbenchstats, valstat.object, cluster.magazine

```
set.seed(20000)
 options(digits=3)
 face <- rFace(10,dMoNo=2,dNoEy=0,p=2)
 clustermethod=c("kmeansCBI","hclustCBI","hclustCBI")
 clustermethodpars <- list()</pre>
 clustermethodpars[[2]] <- clustermethodpars[[3]] <- list()</pre>
 clustermethodpars[[2]]$method <- "ward.D2"</pre>
 clustermethodpars[[3]]$method <- "single"</pre>
 methodname <- c("kmeans", "ward", "single")</pre>
 cbs <- clusterbenchstats(face, G=2:3, clustermethod=clustermethod,
   methodname=methodname, distmethod=rep(FALSE, 3),
   clustermethodpars=clustermethodpars,nnruns=2,kmruns=2,fnruns=2,avenruns=2)
 plot(cbs$stat,cbs$sim)
 plot(cbs$stat,cbs$sim,statistic="dindex")
 plot(cbs$stat,cbs$sim,statistic="avewithin")
 print(cbs\$sstat,aggregate=TRUE,weights=c(1,0,0,0,0,1,0,0,0,0,0,1,0,0,0,0))
# Some of the values are "NaN" because due to the low number of runs of
# the stupid clustering methods there is no variation. If this happens
# in a real application, nnruns etc. should be chosen higher than 2.
# Also useallg=TRUE in clusterbenchstats may help.
```

plotcluster 129

Description

Plots to distinguish given classes by ten available projection methods. Includes classical discriminant coordinates, methods to project differences in mean and covariance structure, asymmetric methods (separation of a homogeneous class from a heterogeneous one), local neighborhood-based methods and methods based on robust covariance matrices. One-dimensional data is plotted against the cluster number.

Usage

```
plotcluster(x, clvecd, clnum=NULL,
            method=ifelse(is.null(clnum), "dc", "awc"),
            bw=FALSE,
            ignorepoints=FALSE, ignorenum=0, pointsbyclvecd=TRUE,
            xlab=NULL, ylab=NULL,
            pch=NULL, col=NULL, ...)
```

Arguments

Х the data matrix; a numerical object which can be coerced to a matrix.

clvecd vector of class numbers which can be coerced into integers; length must equal

nrow(xd).

method one of

"dc" usual discriminant coordinates, see discrcoord,

"bc" Bhattacharyya coordinates, first coordinate showing mean differences, second showing covariance matrix differences, see batcoord,

"vbc" variance dominated Bhattacharyya coordinates, see batcoord,

"mvdc" added mean and variance differences optimizing coordinates, see mvdcoord,

"adc" asymmetric discriminant coordinates, see adcoord,

"awc" asymmetric discriminant coordinates with weighted observations, see awcoord,

"arc" asymmetric discriminant coordinates with weighted observations and robust MCD-covariance matrix, see awcoord,

"nc" neighborhood based coordinates, see ncoord,

"wnc" neighborhood based coordinates with weighted neighborhoods, see ncoord,

"anc" asymmetric neighborhood based coordinates, see ancoord.

Note that "bc", "vbc", "adc", "awc", "arc" and "anc" assume that there are only two classes.

integer. Number of the class which is attempted to plot homogeneously by "asymmetric methods", which are the methods assuming that there are only two

classes, as indicated above. clnum is ignored for methods "dc" and "nc".

logical. If TRUE, the classes are distinguished by symbols, and the default color

is black/white. If FALSE, the classes are distinguished by colors, and the default symbol is pch=1.

ignorepoints logical. If TRUE, points with label ignorenum in clvecd are ignored in the com-

putation for method and are only projected afterwards onto the resulting units. If pch=NULL, the plot symbol for these points is "N".

clnum

bw

130 plotcluster

ignorenum one of the potential values of the components of clvecd. Only has effect if

 ${\tt ignorepoints=TRUE}, see above.$

pointsbyclvecd logical. If TRUE and pch=NULL and/or col=NULL, some hopefully suitable plot

symbols (numbers and letters) and colors are chosen to distinguish the values of clvecd, starting with "1"/"black" for the cluster with the smallest clvecd-code (note that colors for clusters with numbers larger than minimum number +3 are drawn at random from all available colors). FALSE produces potentially less reasonable (but nonrandom) standard colors and symbols if method is "dc" or "nc", and will only distinguish whether clvecd=clnum or not for the other

methods.

xlab label for x-axis. If NULL, a default text is used.

ylab label for y-axis. If NULL, a default text is used.

pch plotting symbol, see par. If NULL, the default is used.

col plotting color, see par. If NULL, the default is used.

... additional parameters passed to plot or the projection methods.

Note

For some of the asymmetric methods, the area in the plot occupied by the "homogeneous class" (see clnum above) may be very small, and it may make sense to run plotcluster a second time specifying plot parameters xlim and ylim in a suitable way. It often makes sense to magnify the plot region containing the homogeneous class in this way so that its separation from the rest can be seen more clearly.

Author(s)

Christian Hennig <christian.hennig@unibo.it>https://www.unibo.it/sitoweb/christian.hennig/en/

References

Hennig, C. (2004) Asymmetric linear dimension reduction for classification. Journal of Computational and Graphical Statistics 13, 930-945.

Hennig, C. (2005) A method for visual cluster validation. In: Weihs, C. and Gaul, W. (eds.): Classification - The Ubiquitous Challenge. Springer, Heidelberg 2005, 153-160.

Seber, G. A. F. (1984). Multivariate Observations. New York: Wiley.

Fukunaga (1990). Introduction to Statistical Pattern Recognition (2nd ed.). Boston: Academic Press.

See Also

discrcoord, batcoord, mvdcoord, adcoord, awcoord, ncoord, ancoord.

discrproj is an interface to all these projection methods.

rFace for generation of the example data used below.

prediction.strength 131

Examples

```
set.seed(4634)
face <- rFace(300,dMoNo=2,dNoEy=0)
grface <- as.integer(attr(face,"grouping"))
plotcluster(face,grface)
plotcluster(face,grface==1)
plotcluster(face,grface, clnum=1, method="vbc")</pre>
```

prediction.strength

Prediction strength for estimating number of clusters

Description

Computes the prediction strength of a clustering of a dataset into different numbers of components. The prediction strength is defined according to Tibshirani and Walther (2005), who recommend to choose as optimal number of cluster the largest number of clusters that leads to a prediction strength above 0.8 or 0.9. See details.

Various clustering methods can be used, see argument clustermethod. In Tibshirani and Walther (2005), only classification to the nearest centroid is discussed, but more methods are offered here, see argument classification.

Usage

Arguments

xdata data (something that can be coerced into a matrix).

Gmin integer. Minimum number of clusters. Note that the prediction strength for

1 cluster is trivially 1, which is automatically included if GMin>1. Therefore

GMin<2 is useless.

Gmax integer. Maximum number of clusters.

M integer. Number of times the dataset is divided into two halves.

clustermethod an interface function (the function name, not a string containing the name,

has to be provided!). This defines the clustering method. See the "Details"-section of clusterboot and kmeansCBI for the format. Clustering methods for prediction.strength must have a k-argument for the number of clusters, must operate on n times p data matrices and must otherwise follow the specifications in clusterboot Note that prediction.strength won't work with CBI-functions that implicitly already estimate the number of clusters such as

pamkCBI; use claraCBI if you want to run it for pam/clara clustering.

132 prediction.strength

classification string. This determines how non-clustered points are classified to given clus-

ters. Options are explained in classifnp and classifdist, the latter for dissimilarity data. Certain classification methods are connected to certain clustering methods. classification="averagedist" is recommended for average linkage, classification="centroid" is recommended for k-means, clara and pam (with distances it will work with claraCBI only), classification="knn" with nnk=1 is recommended for single linkage and classification="qda" is

recommended for Gaussian mixtures with flexible covariance matrices.

centroidname string. Indicates the name of the component of CBI output \$result that contains

the cluster centroids in case of classification="centroid", where CBI output is the output object of clustermethod. If clustermethod is kmeansCBI or claraCBI, centroids are recognised automatically if centroidname=NULL. If centroidname=NULL and distances=FALSE, cluster means are computed as the

cluster centroids.

cutoff numeric between 0 and 1. The optimal number of clusters is the maximum one

with prediction strength above cutoff.

nnk number of nearest neighbours if classification="knn", see classifnp.

distances logical. If TRUE, data will be interpreted as dissimilarity matrix, passed on to

clustering methods as "dist"-object, and classifdist will be used for classi-

fication

count logical. TRUE will print current number of clusters and simulation run number

on the screen.

x object of class predstr.

... arguments to be passed on to the clustering method.

Details

The prediction strength for a certain number of clusters k under a random partition of the dataset in halves A and B is defined as follows. Both halves are clustered with k clusters. Then the points of A are classified to the clusters of B. In the original paper this is done by assigning every observation in A to the closest cluster centroid in B (corresponding to classification="centroid"), but other methods are possible, see classifnp. A pair of points A in the same A-cluster is defined to be correctly predicted if both points are classified into the same cluster on B. The same is done with the points of B relative to the clustering on A. The prediction strength for each of the clusterings is the minimum (taken over all clusters) relative frequency of correctly predicted pairs of points of that cluster. The final mean prediction strength statistic is the mean over all 2M clusterings.

Value

prediction.strength gives out an object of class predstr, which is a list with components

predcorr list of vectors of length M with relative frequencies of correct predictions (clus-

terwise minimum). Every list entry refers to a certain number of clusters.

mean.pred means of predcorr for all numbers of clusters.

optimalk optimal number of clusters.

cutoff see above.

randcmatrix 133

method a string identifying the clustering method.

Gmax see above.

M see above.

Author(s)

Christian Hennig <christian.hennig@unibo.it>https://www.unibo.it/sitoweb/christian.hennig/en/

References

Tibshirani, R. and Walther, G. (2005) Cluster Validation by Prediction Strength, *Journal of Computational and Graphical Statistics*, 14, 511-528.

See Also

```
kmeansCBI, classifnp
```

Examples

```
options(digits=3)
set.seed(98765)
iriss <- iris[sample(150,20),-5]
prediction.strength(iriss,2,3,M=3)
prediction.strength(iriss,2,3,M=3,clustermethod=claraCBI)
# The examples are fast, but of course M should really be larger.</pre>
```

randcmatrix

Random partition matrix

Description

For use within regmix. Generates a random 0-1-matrix with n rows and cln columns so that every row contains exactly one one and every columns contains at least p+3 ones.

Usage

```
randcmatrix(n,cln,p)
```

Arguments

n positive integer. Number of rows.
cln positive integer. Number of columns.
p positive integer. See above.

Value

An n*cln-matrix.

randconf randconf

Author(s)

Christian Hennig <christian.hennig@unibo.it>https://www.unibo.it/sitoweb/christian.hennig/en/

See Also

```
regmix
```

Examples

```
set.seed(111)
randcmatrix(10,2,1)
```

randconf

Generate a sample indicator vector

Description

Generates a logical vector of length n with p TRUEs.

Usage

```
randconf(n, p)
```

Arguments

n positive integer.

p positive integer.

Value

A logical vector.

Author(s)

Christian Hennig <christian.hennig@unibo.it>https://www.unibo.it/sitoweb/christian.hennig/en/

See Also

sample

```
randconf(10,3)
```

randomclustersim 135

randomclustersim S	Simulation of validity indexes based on random clusterings
--------------------	--

Description

For a given dataset this simulates random clusterings using stupidkcentroids, stupidknn, stupidkfn, and stupidkaven. It then computes and stores a set of cluster validity indexes for every clustering.

Usage

```
randomclustersim(datadist,datanp=NULL,npstats=FALSE,useboot=FALSE,
                    bootmethod="nselectboot",
                    bootruns=25,
                    G,nnruns=100,kmruns=100,fnruns=100,avenruns=100,
                    nnk=4, dnnk=2,
                    pamcrit=TRUE,
                    multicore=FALSE,cores=detectCores()-1,monitor=TRUE)
```

Ar

rguments	
datadist	distances on which validation-measures are based, dist object or distance matrix.
datanp	optional observations times variables data matrix, see npstats.
npstats	logical. If TRUE, distrsimilarity is called and the two statistics computed there are added to the output. These are based on datanp and require datanp to be specified.
useboot	logical. If TRUE, a stability index (either nselectboot or prediction.strength) will be involved.
bootmethod	either "nselectboot" or "prediction.strength"; stability index to be used if useboot=TRUE.
bootruns	integer. Number of resampling runs. If useboot=TRUE, passed on as B to nselectboot or M to prediction.strength.
G	vector of integers. Numbers of clusters to consider.
nnruns	integer. Number of runs of stupidknn.
kmruns	integer. Number of runs of stupidkcentroids.
fnruns	integer. Number of runs of stupidkfn.
avenruns	integer. Number of runs of stupidkaven.
nnk	nnk-argument to be passed on to cqcluster.stats.
dnnk	nnk-argument to be passed on to distrsimilarity.
pamcrit	pamcrit-argument to be passed on to cqcluster.stats.
multicore	logical. If TRUE, parallel computing is used through the function mclapply from package parallel; read warnings there if you intend to use this; it won't work on Windows.
cores	integer. Number of cores for parallelisation.
monitor	logical. If TRUE, it will print some runtime information.

136 randomclustersim

Value

List with components

nn list, indexed by number of clusters. Every entry is a data frame with nnruns

observations for every simulation run of stupidknn. The variables of the data

frame are avewithin, mnnd, cvnnd, maxdiameter, widestgap, sindex, minsep, asw, dindex, denscut,

if pamcrit=TRUE also pamc, if npstats=TRUE also kdnorm, kdunif. All these

are cluster validation indexes; documented as values of clustatsum.

fn list, indexed by number of clusters. Every entry is a data frame with fnruns

observations for every simulation run of stupidkfn. The variables of the data

frame are avewithin, mnnd, cvnnd, maxdiameter, widestgap, sindex, minsep, asw, dindex, denscut,

if pamcrit=TRUE also pamc, if npstats=TRUE also kdnorm, kdunif. All these

are cluster validation indexes; documented as values of clustatsum.

aven list, indexed by number of clusters. Every entry is a data frame with avenruns

observations for every simulation run of stupidkaven. The variables of the data

frame are avewithin, mnnd, cvnnd, maxdiameter, widestgap, sindex, minsep, asw, dindex, denscut,

if pamcrit=TRUE also pamc, if npstats=TRUE also kdnorm, kdunif. All these

are cluster validation indexes; documented as values of clustatsum.

km list, indexed by number of clusters. Every entry is a data frame with kmruns ob-

servations for every simulation run of stupidkcentroids. The variables of the

data frame are avewithin, mnnd, cvnnd, maxdiameter, widestgap, sindex, minsep, asw, dindex, dens

if pamcrit=TRUE also pamc, if npstats=TRUE also kdnorm, kdunif. All these

are cluster validation indexes; documented as values of clustatsum.

nnruns number of involved runs of stupidknn,

fnruns number of involved runs of stupidkfn,

avenruns number of involved runs of stupidkaven,

kmruns number of involved runs of stupidkcentroids,

boot if useboot=TRUE, stability value; stabk for method nselectboot; mean.pred

for method prediction.strength.

Author(s)

Christian Hennig <christian.hennig@unibo.it>https://www.unibo.it/sitoweb/christian.hennig/en/

References

Hennig, C. (2019) Cluster validation by measurement of clustering characteristics relevant to the user. In C. H. Skiadas (ed.) *Data Analysis and Applications 1: Clustering and Regression, Modeling-estimating, Forecasting and Data Mining, Volume 2*, Wiley, New York 1-24, https://arxiv.org/abs/1703.09282

Akhanli, S. and Hennig, C. (2020) Calibrating and aggregating cluster validity indexes for context-adapted comparison of clusterings. *Statistics and Computing*, 30, 1523-1544, https://link.springer.com/article/10.1007/s11222-020-09958-2, https://arxiv.org/abs/2002.01822

regmix 137

See Also

stupidkcentroids, stupidknn, stupidkfn, stupidkaven, clustatsum

Examples

regmix

Mixture Model ML for Clusterwise Linear Regression

Description

Computes an ML-estimator for clusterwise linear regression under a regression mixture model with Normal errors. Parameters are proportions, regression coefficients and error variances, all independent of the values of the independent variable, and all may differ for different clusters. Computation is by the EM-algorithm. The number of clusters is estimated via the Bayesian Information Criterion (BIC). Note that package flexmix has more sophisticated tools to do the same thing and is recommended. The functions are kept in here only for compatibility reasons.

Usage

```
regmix(indep, dep, ir=1, nclust=1:7, icrit=1.e-5, minsig=1.e-6, warnings=FALSE)
regem(indep, dep, m, cln, icrit=1.e-5, minsig=1.e-6, warnings=FALSE)
```

Arguments

indep	numerical matrix or vector. Independent variables.
dep	numerical vector. Dependent variable.
ir	positive integer. Number of iteration runs for every number of clusters.
nclust	vector of positive integers. Numbers of clusters.
icrit	positive numerical. Stopping criterion for the iterations (difference of loglikelihoods).
minsig	positive numerical. Minimum value for the variance parameters (likelihood is unbounded if variances are allowed to converge to 0).
warnings	logical. If TRUE, warnings are given during the EM iteration in case of collinear regressors, too small mixture components and error variances smaller than minimum. In the former two cases, the algorithm is terminated without a result, but an optimal solution is still computed from other algorithm runs (if there are others). In the latter case, the corresponding variance is set to the minimum.

138 regmix

cln positive integer. (Single) number of clusters.

m matrix of positive numericals. Number of columns must be cln. Number of

rows must be number of data points. Columns must add up to 1. Initial configuration for the EM iteration in terms of a probability vector for every point which gives its degree of membership to every cluster. As generated by randcmatrix.

Details

The result of the EM iteration depends on the initial configuration, which is generated randomly by randcmatrix for regmix. regmix calls regem. To provide the initial configuration manually, use parameter m of regem directly. Take a look at the example about how to generate m if you want to specify initial parameters.

The original paper DeSarbo and Cron (1988) suggests the AIC for estimating the number of clusters. The use of the BIC is advocated by Wedel and DeSarbo (1995). The BIC is defined here as 2*loglik -log(n)*((p+3)*cln-1), p being the number of independent variables, i.e., the larger the better.

See the entry for the input parameter warnings for the treatment of several numerical problems.

Value

regmix returns a list containing the components clnopt,loglik,bic,coef,var,eps,z,g. regem returns a list containing the components loglik,coef,var,z,g,warn.

clnopt optimal number of clusters according to the BIC.

loglik loglikelihood for the optimal model.

bic vector of BIC values for all numbers of clusters in nclust.

coef matrix of regression coefficients. First row: intercept parameter. Second row:

parameter of first independent variable and so on. Columns corresponding to

clusters.

var vector of error variance estimators for the clusters.

eps vector of cluster proportion estimators.

z matrix of estimated a posteriori probabilities of the points (rows) to be generated

by the clusters (columns). Compare input argument m.

g integer vector of estimated cluster numbers for the points (via argmax over z).

warn logical. TRUE if one of the estimated clusters has too few points and/or collinear

regressors.

Author(s)

Christian Hennig <christian.hennig@unibo.it>https://www.unibo.it/sitoweb/christian.hennig/en/

regmix 139

References

DeSarbo, W. S. and Cron, W. L. (1988) A maximum likelihood methodology for clusterwise linear regression, *Journal of Classification* 5, 249-282.

Wedel, M. and DeSarbo, W. S. (1995) A mixture likelihood approach for generalized linear models, *Journal of Classification* 12, 21-56.

See Also

Regression mixtures can also (and probably better) be computed with the flexmix package, see flexmix. (When I first write the regmix-function, flexmix didn't exist.)

fixreg for fixed point clusters for clusterwise linear regression.

EMclust for Normal mixture model fitting (non-regression).

```
## Not run:
# This apparently gives slightly different
# but data-analytically fine results
# on some versions of R.
set.seed(12234)
data(tonedata)
attach(tonedata)
rmt1 <- regmix(stretchratio,tuned,nclust=1:2)</pre>
# nclust=1:2 makes the example fast;
# a more serious application would rather use the default.
rmt1$g
round(rmt1$bic,digits=2)
# start with initial parameter values
cln <- 3
n <- 150
initcoef <- cbind(c(2,0),c(0,1),c(0,2.5))
initvar <-c(0.001,0.0001,0.5)
initeps <- c(0.4, 0.3, 0.3)
# computation of m from initial parameters
m <- matrix(nrow=n, ncol=cln)</pre>
stm <- numeric(0)</pre>
for (i in 1:cln)
  for (j in 1:n){
    m[j,i] <- initeps[i]*dnorm(tuned[j],mean=initcoef[1,i]+</pre>
               initcoef[2,i]*stretchratio[j], sd=sqrt(initvar[i]))
  for (j in 1:n){
    stm[j] <- sum(m[j,])</pre>
    for (i in 1:cln)
      m[j,i] \leftarrow m[j,i]/stm[j]
rmt2 <- regem(stretchratio, tuned, m, cln)
## End(Not run)
```

rFace

rFace "Face-shaped" clustered benchmark datasets

Description

Generates "face-shaped" clustered benchmark datasets. This is based on a collaboration with Martin Maechler.

Usage

```
rFace(n, p = 6, nrep.top = 2, smile.coef = 0.6, dMoNo = 1.2, dNoEy = 1)
```

Arguments

n integer greater or equal to 10. Number of points.

p integer greater or equal to 2. Dimension.

nrep. top integer. Number of repetitions of the hair-top point.

smile.coef numeric. Coefficient for quadratic term used for generation of mouth-points.

Positive values=>smile.

dMoNo number. Distance from mouth to nose.

dNoEy number. Minimum vertical distance from mouth to eyes.

Details

The function generates a nice benchmark example for cluster analysis. There are six "clusters" in this data, of which the first five are clearly homogeneous patterns, but with different distributional shapes and different qualities of separation. The clusters are distinguished only in the first two dimensions. The attribute grouping is a factor giving the cluster numbers, see below. The sixth group of points corresponds to some hairs, and is rather a collection of outliers than a cluster in itself. This group contains nrep. top+2 points. Of the remaining points, 20% belong to cluster 1, the chin (quadratic function plus noise). 10% belong to cluster 2, the right eye (Gaussian). 30% belong to cluster 3, the mouth (Gaussian/squared Gaussian). 20% belong to cluster 4, the nose (Gaussian/gamma), and 20% belong to cluster 5, the left eye (uniform).

The distributions of the further variables are homogeneous over all points. The third dimension is exponentially distributed, the fourth dimension is Cauchy distributed, all further distributions are Gaussian.

Please consider the source code for exact generation of the clusters.

Value

An n times p numeric matrix with attributes

grouping a factor giving the cluster memberships of the points.

indexlist a list of six vectors containing the indices of points belonging to the six groups.

ridgeline 141

Author(s)

Christian Hennig <christian.hennig@unibo.it>https://www.unibo.it/sitoweb/christian.hennig/en/

Examples

```
set.seed(4634)
face <- rFace(600,dMoNo=2,dNoEy=0)
grface <- as.integer(attr(face, "grouping"))
plot(face, col = grface)
# pairs(face, col = grface, main ="rFace(600,dMoNo=2,dNoEy=0)")</pre>
```

ridgeline

Ridgeline computation

Description

Computes (alpha*Sigma1^-1+(1-alpha)*Sigma2^-1)^-1* alpha*(Sigma1^-1*mu1)+(1-alpha)*(Sigma2^-1*mu2)) as required for the computation of the ridgeline (Ray and Lindsay, 2005) to find all density extrema of a two-component Gaussian mixture with mean vectors mu1 and mu2 and covariance matrices Sigma1, Sigma2.

Usage

```
ridgeline(alpha, mu1, mu2, Sigma1, Sigma2)
```

Arguments

alpha numeric between 0 and 1.

mu1 mean vector of component 1.

mu2 mean vector of component 2.

Sigma1 covariance matrix of component 1.

Sigma2 covariance matrix of component 2.

Value

A vector. See above.

Author(s)

Christian Hennig <christian.hennig@unibo.it>https://www.unibo.it/sitoweb/christian.hennig/en/

References

Ray, S. and Lindsay, B. G. (2005) The Topography of Multivariate Normal Mixtures, *Annals of Statistics*, 33, 2042-2065.

ridgeline.diagnosis

Examples

```
\label{eq:condition} \\ \text{ridgeline}(0.5, c(1,1), c(2,5), \\ \\ \text{diag}(2), \\ \\ \text{diag}(2)) \\
```

ridgeline.diagnosis

Ridgeline plots, ratios and unimodality

Description

Computes ridgeline ratios and unimodality checks for pairs of components given the parameters of a Gaussian mixture. Produces ridgeline plots.

Usage

Arguments

propvector	vector of component proportions. Length must be number of components, and must sum up to $1. \\$
muarray	matrix of component means (different components are in different columns).
Sigmaarray	three dimensional array with component covariance matrices (the third dimension refers to components).
k	integer. Number of components.
ipairs	"all" or list of vectors of two integers. If ipairs="all", computations are carried out for all pairs of components. Otherwise, ipairs gives the pairs of components for which computations are carried out.
compute.ratio	logical. If TRUE, a matrix of ridgeline ratios is computed, see Hennig (2010a).
by	real between 0 and 1. Interval width for density computation along the ridgeline.
ratiocutoff	real between 0 and 1. If not NULL, the connection.matrix (see below) is computed by checking whether ridgeline ratios between components are below ratiocutoff.
ridgelineplot	one of "none", "matrix", "pairwise". If "matrix", a matrix of pairwise ridgeline plots (see Hennig 2010b) will be plotted. If "pairwise", pairwise ridgeline plots are plotted (you may want to set par(ask=TRUE) to see them all). No plotting if "none".

ridgeline.diagnosis 143

Value

A list with components

merged.clusters

vector of integers, stating for every mixture component the number of the cluster of components that would be merged by merging connectivity components of the graph specified by connection.matrix.

connection.matrix

zero-one matrix, in which a one means that the mixture of the corresponding pair of components of the original mixture is either unimodel (if ratiocutoff=NULL) or that their ridgeline ratio is above ratiocutoff. If ipairs!="all", ignored pairs always have 0 in this matrix, same for ratio.matrix.

ratio.matrix

matrix with entries between 0 und 1, giving the ridgeline ratio, which is the density minimum of the mixture of the corresponding pair of components along the ridgeline divided by the minimum of the two maxima closest to the beginning and the end of the ridgeline.

Author(s)

Christian Hennig <christian.hennig@unibo.it>https://www.unibo.it/sitoweb/christian.hennig/en/

References

Hennig, C. (2010a) Methods for merging Gaussian mixture components, *Advances in Data Analysis and Classification*, 4, 3-34.

Hennig, C. (2010b) Ridgeline plot and clusterwise stability as tools for merging Gaussian mixture components. To appear in *Classification as a Tool for Research*, Proceedings of IFCS 2009.

Ray, S. and Lindsay, B. G. (2005) The Topography of Multivariate Normal Mixtures, *Annals of Statistics*, 33, 2042-2065.

See Also

```
ridgeline, dridgeline, piridge, piridge.zeroes
```

```
muarray <- cbind(c(0,0),c(0,0.1),c(10,10)) sigmaarray <- array(c(diag(2),diag(2),diag(2)),dim=c(2,2,3)) rd <- ridgeline.diagnosis(c(0.5,0.3,0.2),muarray,sigmaarray,ridgelineplot="matrix",by=0.1) # Much slower but more precise with default by=0.001.
```

144 simmatrix

simmatrix

Extracting intersections between clusters from fpc-object

Description

Extracts the information about the size of the intersections between representative Fixed Point Clusters (FPCs) of stable groups from the output of the FPC-functions fixreg and fixmahal.

Usage

```
simmatrix(fpcobj)
```

Arguments

fpcobj

an object of class rfpc or mfpc.

Value

A non-negative real-valued vector giving the number of points in the intersections of the representative FPCs of stable groups.

Note

The intersection between representative FPCs no. i and j is at position sseg(i, j).

Author(s)

```
Christian\ Hennig\ < christian\ .\ hennig\ @unibo\ .\ it\ >\ https://www.unibo\ .\ it/sitoweb/christian\ .\ hennig/en/
```

See Also

```
fixmahal, fixreg, sseg
```

```
set.seed(190000)
data(tonedata)
# Note: If you do not use the installed package, replace this by
# tonedata <- read.table("(path/)tonedata.txt", header=TRUE)
attach(tonedata)
tonefix <- fixreg(stretchratio,tuned,mtf=1,ir=20)
simmatrix(tonefix)[sseg(2,3)]</pre>
```

solvecov 145

solvecov

Inversion of (possibly singular) symmetric matrices

Description

Tries to invert a matrix by solve. If this fails because of singularity, an eigenvector decomposition is computed, and eigenvalues below 1/cmax are replaced by 1/cmax, i.e., cmax will be the corresponding eigenvalue of the inverted matrix.

Usage

```
solvecov(m, cmax = 1e+10)
```

Arguments

m a numeric symmetric matrix.cmax a positive value, see above.

Value

A list with the following components:

inv the inverted matrix

coll TRUE if solve failed because of singularity.

Author(s)

 $Christian\ Hennig\ < christian\ .\ hennig\ @unibo\ .\ it\ >\ https://www.unibo\ .\ it/sitoweb/christian\ .\ hennig/en/$

See Also

```
solve, eigen
```

Examples

```
x <- c(1,0,0,1,0,1,0,0,1)
dim(x) <- c(3,3)
solvecov(x)</pre>
```

146 stupidkaven

sseg

Position in a similarity vector

Description

sseg(i,j) gives the position of the similarity of objects i and j in the similarity vectors produced by fixreg and fixmahal. sseg should only be used as an auxiliary function in fixreg and fixmahal.

Usage

```
sseg(i, j)
```

Arguments

- i positive integer.
- j positive integer.

Value

A positive integer.

Author(s)

Christian Hennig <christian.hennig@unibo.it>https://www.unibo.it/sitoweb/christian.hennig/en/

Examples

```
sseg(3,4)
```

stupidkaven

Stupid average dissimilarity random clustering

Description

Picks k random starting points from given dataset to initialise k clusters. Then, one by one, the point not yet assigned to any cluster with smallest average dissimilarity to the points of any already existing cluster is assigned to that cluster, until all points are assigned. This is a random versione of average linkage clustering, see Akhanli and Hennig (2020).

Usage

```
stupidkaven(d,k)
```

stupidkcentroids 147

Arguments

d dist-object or dissimilarity matrix.

k integer. Number of clusters.

Value

The clustering vector (values 1 to k, length number of objects behind d),

Author(s)

```
Christian Hennig <christian.hennig@unibo.it>https://www.unibo.it/sitoweb/christian.hennig/en/
```

References

Akhanli, S. and Hennig, C. (2020) Calibrating and aggregating cluster validity indexes for context-adapted comparison of clusterings. *Statistics and Computing*, 30, 1523-1544, https://link.springer.com/article/10.1007/s11222-020-09958-2, https://arxiv.org/abs/2002.01822

See Also

```
stupidkcentroids, stupidknn, stupidkfn
```

Examples

```
set.seed(20000)
options(digits=3)
face <- rFace(200,dMoNo=2,dNoEy=0,p=2)
stupidkaven(dist(face),3)</pre>
```

stupidkcentroids

Stupid k-centroids random clustering

Description

Picks k random centroids from given dataset and assigns every point to closest centroid. This is called stupid k-centroids in Hennig (2019).

Usage

```
stupidkcentroids(xdata, k, distances = inherits(xdata, "dist"))
```

Arguments

xdata cases*variables data, dist-object or dissimilarity matrix, see distances.

k integer. Number of clusters.

distances logical. If TRUE, xdata is interpreted as distances.

148 stupidkfn

Value

The clustering vector (values 1 to k, length number of objects behind xdata),

Author(s)

Christian Hennig <christian.hennig@unibo.it>https://www.unibo.it/sitoweb/christian.hennig/en/

References

Hennig, C. (2019) Cluster validation by measurement of clustering characteristics relevant to the user. In C. H. Skiadas (ed.) *Data Analysis and Applications 1: Clustering and Regression, Modeling-estimating, Forecasting and Data Mining, Volume 2*, Wiley, New York 1-24, https://arxiv.org/abs/1703.09282

Akhanli, S. and Hennig, C. (2020) Calibrating and aggregating cluster validity indexes for context-adapted comparison of clusterings. *Statistics and Computing*, 30, 1523-1544, https://link.springer.com/article/10.1007/s11222-020-09958-2, https://arxiv.org/abs/2002.01822

See Also

stupidknn, stupidkfn, stupidkaven

Examples

```
set.seed(20000)
options(digits=3)
face <- rFace(200,dMoNo=2,dNoEy=0,p=2)
stupidkcentroids(dist(face),3)</pre>
```

stupidkfn

Stupid farthest neighbour random clustering

Description

Picks k random starting points from given dataset to initialise k clusters. Then, one by one, a point not yet assigned to any cluster is assigned to that cluster, until all points are assigned. The point/cluster pair to be used is picked according to the smallest distance of a point to the farthest point to it in any of the already existing clusters as in complete linkage clustering, see Akhanli and Hennig (2020).

Usage

```
stupidkfn(d,k)
```

Arguments

d dist-object or dissimilarity matrix.

k integer. Number of clusters.

stupidknn 149

Value

The clustering vector (values 1 to k, length number of objects behind d),

Author(s)

Christian Hennig <christian.hennig@unibo.it>https://www.unibo.it/sitoweb/christian.hennig/en/

References

Akhanli, S. and Hennig, C. (2020) Calibrating and aggregating cluster validity indexes for context-adapted comparison of clusterings. *Statistics and Computing*, 30, 1523-1544, https://link.springer.com/article/10.1007/s11222-020-09958-2, https://arxiv.org/abs/2002.01822

See Also

stupidkcentroids, stupidknn, stupidkaven

Examples

```
set.seed(20000)
options(digits=3)
face <- rFace(200,dMoNo=2,dNoEy=0,p=2)
stupidkfn(dist(face),3)</pre>
```

stupidknn

Stupid nearest neighbour random clustering

Description

Picks k random starting points from given dataset to initialise k clusters. Then, one by one, the point not yet assigned to any cluster that is closest to an already assigned point is assigned to that cluster, until all points are assigned. This is called stupid nearest neighbour clustering in Hennig (2019).

Usage

```
stupidknn(d,k)
```

Arguments

d dist-object or dissimilarity matrix.

k integer. Number of clusters.

Value

The clustering vector (values 1 to k, length number of objects behind d),

150 tdecomp

Author(s)

Christian Hennig <christian.hennig@unibo.it>https://www.unibo.it/sitoweb/christian.hennig/en/

References

Hennig, C. (2019) Cluster validation by measurement of clustering characteristics relevant to the user. In C. H. Skiadas (ed.) *Data Analysis and Applications 1: Clustering and Regression, Modeling-estimating, Forecasting and Data Mining, Volume 2*, Wiley, New York 1-24, https://arxiv.org/abs/1703.09282

Akhanli, S. and Hennig, C. (2020) Calibrating and aggregating cluster validity indexes for context-adapted comparison of clusterings. *Statistics and Computing*, 30, 1523-1544, https://link.springer.com/article/10.1007/s11222-020-09958-2, https://arxiv.org/abs/2002.01822

See Also

stupidkcentroids, stupidkfn, stupidkaven

Examples

```
set.seed(20000)
options(digits=3)
face <- rFace(200,dMoNo=2,dNoEy=0,p=2)
stupidknn(dist(face),3)</pre>
```

tdecomp

Root of singularity-corrected eigenvalue decomposition

Description

Computes transposed eigenvectors of matrix m times diagonal of square root of eigenvalues so that eigenvalues smaller than 1e-6 are set to 1e-6.

Usage

```
tdecomp(m)
```

Arguments

m

a symmetric matrix of minimum format 2*2.

Details

Thought for use in discreoord only.

Value

a matrix.

tonedata 151

Note

Thought for use within discreoord only.

Author(s)

Christian Hennig <christian.hennig@unibo.it>https://www.unibo.it/sitoweb/christian.hennig/en/

Examples

```
x <- rnorm(10)
y <- rnorm(10)
z <- cov(cbind(x,y))
round(tdecomp(z),digits=2)</pre>
```

tonedata

Tone perception data

Description

The tone perception data stem from an experiment of Cohen (1980) and have been analyzed in de Veaux (1989). A pure fundamental tone was played to a trained musician. Electronically generated overtones were added, determined by a stretching ratio of stretchratio. stretchratio=2.0 corresponds to the harmonic pattern usually heard in traditional definite pitched instruments. The musician was asked to tune an adjustable tone to the octave above the fundamental tone. tuned gives the ratio of the adjusted tone to the fundamental, i.e. tuned=2.0 would be the correct tuning for all stretchratio-values. The data analyzed here belong to 150 trials with the same musician. In the original study, there were four further musicians.

Usage

```
data(tonedata)
```

Format

A data frame with 2 variables stretchratio and tuned and 150 cases.

Source

Cohen, E. A. (1980) *Inharmonic tone perception*. Unpublished Ph.D. dissertation, Stanford University

References

de Veaux, R. D. (1989) Mixtures of Linear Regressions, *Computational Statistics and Data Analysis* 8, 227-245.

valstat.object

unimodal.ind

Is a fitted denisity unimodal or not?

Description

Checks whether a series of fitted density values (such as given out as y-component of density) is unimodal.

Usage

```
unimodal.ind(y)
```

Arguments

У

numeric vector of fitted density values in order of increasing x-values such as given out as y-component of density.

Value

Logical. TRUE if unimodal.

Author(s)

Christian Hennig <christian.hennig@unibo.it>https://www.unibo.it/sitoweb/christian.hennig/en/

Examples

```
unimodal.ind(c(1,3,3,4,2,1,0,0))
```

valstat.object

Cluster validation statistics - object

Description

The objects of class "valstat" store cluster validation statistics from various clustering methods run with various numbers of clusters.

valstat.object 153

Value

A legitimate valstat object is a list. The format of the list relies on the number of involved clustering methods, nmethods, say, i.e., the length of the method-component explained below. The first nmethods elements of the valstat-list are just numbered. These are themselves lists that are numbered between 1 and the maxG-component defined below. Element [[i]][[j]] refers to the clustering from clustering method number i with number of clusters j. Every such element is a list with components avewithin,mnnd,cvnnd,maxdiameter,widestgap,sindex,minsep,asw,dindex,denscut,highdgap,pear Further optional components are pamc,kdnorm,kdunif,dmode,aggregated. All these are cluster validation indexes, as follows.

avewithin average distance within clusters (reweighted so that every observation, rather

than every distance, has the same weight).

mnnd average distance to nnkth nearest neighbour within cluster. (nnk is a parameter

of cgcluster.stats, default 2.)

cvnnd coefficient of variation of dissimilarities to nnkth nearest wthin-cluster neigh-

bour, measuring uniformity of within-cluster densities, weighted over all clusters, see Sec. 3.7 of Hennig (2019). (nnk is a parameter of cqcluster.stats,

default 2.)

maxdiameter maximum cluster diameter.

widest gap widest within-cluster gap or average of cluster-wise widest within-cluster gap,

depending on parameter averagegap of cqcluster.stats, default FALSE.

sindex separation index. Defined based on the distances for every point to the closest

point not in the same cluster. The separation index is then the mean of the smallest proportion sepprob (parameter of cqcluster.stats, default 0.1) of

these. See Hennig (2019).

minsep minimum cluster separation.

asw average silhouette width. See silhouette.

dindex this index measures to what extent the density decreases from the cluster mode

to the outskirts; I-densdec in Sec. 3.6 of Hennig (2019); low values are good.

denscut this index measures whether cluster boundaries run through density valleys; I-

densbound in Sec. 3.6 of Hennig (2019); low values are good.

highdgap this measures whether there is a large within-cluster gap with high density on

both sides; I-highdgap in Sec. 3.6 of Hennig (2019); low values are good.

pearsongamma correlation between distances and a 0-1-vector where 0 means same cluster, 1

means different clusters. "Normalized gamma" in Halkidi et al. (2001).

withinss a generalisation of the within clusters sum of squares (k-means objective func-

tion), which is obtained if d is a Euclidean distance matrix. For general distance measures, this is half the sum of the within cluster squared dissimilarities di-

vided by the cluster size.

entropy entropy of the distribution of cluster memberships, see Meila(2007).

pame average distance to cluster centroid, which is the observation that minimises this

average distance.

kdnorm Kolmogorov distance between distribution of within-cluster Mahalanobis dis-

tances and appropriate chi-squared distribution, aggregated over clusters (I am

grateful to Agustin Mayo-Iscar for the idea).

154 valstat.object

kdunif Kolmogorov distance between distribution of distances to dnnkth nearest within-

cluster neighbor and appropriate Gamma-distribution, see Byers and Raftery (1998), aggregated over clusters. dnnk is parameter nnk of distrsimilarity,

corresponding to dnnk of clusterbenchstats.

dmode aggregated density mode index equal to 0.75*dindex+0.25*highdgap before

standardisation.

Furthermore, a valstat object has the following list components:

maxG maximum number of clusters.

minG minimum number of clusters (list entries below that number are empty lists).

method vector of names (character strings) of clustering CBI-functions, see kmeansCBI.

name vector of names (character strings) of clustering methods. These can be user-

chosen names (see argument methodsnames in clusterbenchstats) and may distinguish different methods run by the same CBI-function but with different

parameter values such as complete and average linkage for hclustCBI.

statistics vector of names (character strings) of cluster validation indexes.

GENERATION

These objects are generated as part of the clusterbenchstats-output.

METHODS

The valstat class has methods for the following generic functions: print, plot, see plot.valstat.

Author(s)

Christian Hennig <christian.hennig@unibo.it>https://www.unibo.it/sitoweb/christian.hennig/en/

References

Hennig, C. (2019) Cluster validation by measurement of clustering characteristics relevant to the user. In C. H. Skiadas (ed.) *Data Analysis and Applications 1: Clustering and Regression, Modeling-estimating, Forecasting and Data Mining, Volume 2*, Wiley, New York 1-24, https://arxiv.org/abs/1703.09282

Akhanli, S. and Hennig, C. (2020) Calibrating and aggregating cluster validity indexes for context-adapted comparison of clusterings. *Statistics and Computing*, 30, 1523-1544, https://link.springer.com/article/10.1007/s11222-020-09958-2, https://arxiv.org/abs/2002.01822

See Also

clusterbenchstats, plot.valstat.

weightplots 155

weightplots	Ordered posterior plots	

Description

Ordered posterior plots for Gaussian mixture components, see Hennig (2010).

Usage

Arguments

z	matrix with rows corresponding to observations and columns corresponding to mixture components. Entries are probabilities that an observation has been generated by a mixture component. These will normally be estimated a posteriori probabilities, as generated as component z of the output object from summary.mclustBIC.
clusternumbers	"all" or vector of integers. Numbers of components for which plots are drawn.
clustercol	colour used for the main components for which a plot is drawn.
allcol	colours used for respective other components in plots in which they are not main components.
lty	line types for components.
clusterlwd	numeric. Line width for main component.
legendposition	"none" or vector with two coordinates in the plot, where a legend should be printed.
weightcutoff	numeric between 0 and 1. Observations are only taken into account for which the posterior probability for the main component is larger than this.
ask	logical. If TRUE, it sets par(ask=TRUE) in the beginning and par(ask=FALSE) after all plots were showed.
	further parameters to be passed on to legend.

Details

Shows posterior probabilities for observations belonging to all mixture components on the y-axis, with points ordered by posterior probability for main component.

Value

Invisible matrix of posterior probabilities z from mclustsummary.

156 wfu

Author(s)

Christian Hennig <christian.hennig@unibo.it>https://www.unibo.it/sitoweb/christian.hennig/en/

References

Hennig, C. (2010) Methods for merging Gaussian mixture components, *Advances in Data Analysis and Classification*, 4, 3-34.

Examples

wfu

Weight function (for Mahalabobis distances)

Description

Function of the elements of md, which is 1 for arguments smaller than ca, 0 for arguments larger than ca2 and linear (default: continuous) in between.

Thought for use in fixmahal.

Usage

```
wfu(md, ca, ca2, a1 = 1/(ca - ca2), a0 = -a1 * ca2)
```

Arguments

md	vector of positive numericals
ca	positive numerical.
ca2	positive numerical.
a1	numerical. Slope.
a0	numerical. Intercept.

Value

A vector of numericals between 0 and 1.

xtable 157

Author(s)

Christian Hennig <christian.hennig@unibo.it>https://www.unibo.it/sitoweb/christian.hennig/en/

See Also

fixmahal

Examples

```
md <- seq(0,10,by=0.1)
round(wfu(md,ca=5,ca2=8),digits=2)</pre>
```

xtable

Partition crosstable with empty clusters

Description

This produces a crosstable between two integer vectors (partitions) of the same length with a given maximum vector entry k so that the size of the table is k*k with zeroes for missing entries between 1 and k (the command table does pretty much the same thing but will leave out missing entries).

Usage

```
xtable(c1,c2,k)
```

Arguments

c1 vector of integers.

c2 vector of integers of same length as c1.

k integer. Must be larger or equal to maximum entry in c1 and c2.

Value

A matrix of dimensions c(k,k). Entry [i,j] gives the number of places in which c1==i & c2==j.

Author(s)

```
Christian Hennig <christian.hennig@unibo.it>https://www.unibo.it/sitoweb/christian.hennig/en/
```

See Also

table

158 zmisclassification.matrix

Examples

```
c1 <- 1:3
c2 <- c(1,1,2)
xtable(c1,c2,3)</pre>
```

zmisclassification.matrix

Matrix of misclassification probabilities between mixture components

Description

Matrix of misclassification probabilities in a mixture distribution between two mixture components from estimated posterior probabilities regardless of component parameters, see Hennig (2010).

Usage

Arguments

Z	matrix of posterior probabilities for observations (rows) to belong to mixture components (columns), so entries need to sum up to 1 for each row.
pro	vector of component proportions, need to sum up to 1. Computed from z as default.
clustering	vector of integers giving the estimated mixture components for every observation. Computed from z as default.
ipairs	"all" or list of vectors of two integers. If ipairs="all", computations are carried out for all pairs of components. Otherwise, ipairs gives the pairs of components for which computations are carried out.
symmetric	logical. If TRUE, the matrix is symmetrised, see parameter stat.
stat	"max" or "mean". The statistic by which the two misclassification probabilities are aggregated if symmetric=TRUE.

Value

A matrix with the (symmetrised, if required) misclassification probabilities between each pair of mixture components. If symmetric=FALSE, matrix entry [i,j] is the estimated probability that an observation generated by component j is classified to component i by maximum a posteriori rule.

Author(s)

Christian Hennig <christian.hennig@unibo.it>https://www.unibo.it/sitoweb/christian.hennig/en/

zmisclassification.matrix 159

References

Hennig, C. (2010) Methods for merging Gaussian mixture components, *Advances in Data Analysis and Classification*, 4, 3-34.

See Also

confusion

Examples

```
set.seed(12345)
m <- rpois(20,lambda=5)
dim(m) <- c(5,4)
m <- m/apply(m,1,sum)
round(zmisclassification.matrix(m,symmetric=FALSE),digits=2)</pre>
```

Index

* arith	cvnn, 57
can, 16	dbscan, 59
cweight, 59	dipp.tantrum, 62
wfu, 156	diptest.multi, 63
	distancefactor, 68
* array con.comp, 48	distoritmulti, 70
solvecov, 145	distrsimilarity, 71
tdecomp, 150	dridgeline, 73
xtable, 157	dudahart2, 74
* classif	extract.mixturepars, 75
adcoord. 6	findrep, 76
ancoord, 8	fixmahal, 77
awcoord, 9	fixreg, 84
batcoord, 11	flexmixedruns, 89
discroord, 64	fpclusters, 92
discreto, 66	itnumber, 93
distrimilarity, 71	kmeansCBI, 95
mvdcoord, 116	
	kmeansruns, 100
ncoord, 117	lcmixed, 102
plotcluster, 128	mahalconf, 107
* cluster	mergenormals, 108
bhattacharyya.matrix, 14	mergeparameters, 112
calinhara, 15	minsize, 113
cdbw, 18	mixdens, 114
cgrestandard, 19	mixpredictive, 115
classifdist, 21	neginc, 119
clucols, 23	nselectboot, 120
clujaccard, 24	pamk, 122
clusexpect, 25	piridge, 124
clustatsum, 26	piridge.zeroes, 125
cluster.magazine, 29	plot.valstat, 126
cluster.stats, 31	prediction.strength, 131
cluster.varstats, 35	randcmatrix, 133
clusterbenchstats, 37	randomclustersim, 135
clusterboot, 41	regmix, 137
cmahal, 47	ridgeline, 141
con.comp, 48	ridgeline.diagnosis, 142
confusion, 49	stupidkaven, 146
cqcluster.stats,51	stupidkcentroids, 147

stupidkfn, 148	mixdens, 114
stupidknn, 149	mixpredictive, 115
valstat.object, 152	mvdcoord, 116
weightplots, 155	ncoord, 117
zmisclassification.matrix, 158	nselectboot, 120
* datasets	pamk, 122
tonedata, 151	piridge, 124
* data	piridge.zeroes, 125
rFace, 140	plot.valstat, 126
* distribution	plotcluster, 128
randconf, 134	prediction.strength, 131
* manip	randomclustersim, 135
cat2bin, 17	ridgeline, 141
discrete.recode, 65	ridgeline.diagnosis, 142
jittervar, 94	stupidkaven, 146
* multivariate	stupidkcentroids, 147
adcoord, 6	stupidkfn, 148
ancoord, 8	stupidknn, 149
awcoord, 9	weightplots, 155
batcoord, 11	zmisclassification.matrix, 158
bhattacharyya.dist, 13	* regression
bhattacharyya.matrix, 14	fixreg,84
cgrestandard, 19	regmix, 137
classifdist, 21	* robust
clustatsum, 26	fixmahal,77
cluster.magazine, 29	fixreg,84
cluster.stats, 31	* univar
clusterbenchstats, 37	clusexpect, 25
clusterboot, 41	itnumber,93
confusion, 49	minsize, 113
cov.wml, 50	unimodal.ind, 152
cqcluster.stats, 51	* utilities
dbscan, 59	simmatrix, 144
diptest.multi, 63	sseg, 146
discreoord, 64	
discrproj, 66	adcoord, 6, 67, 68, 129, 130
distripton, 66 distrsimilarity, 71	ancoord, 8, 67, 68, 129, 130
	awcoord, 9, 59, 67, 68, 105, 129, 130
dridgeline, 73	
extract.mixturepars, 75	batcoord, 11, 65, 67, 68, 81, 83, 129, 130
fixmahal,77	batvarcoord (batcoord), 11
kmeansCBI, 95	bhattacharyya.dist,13, <i>15</i>
kmeansruns, 100	bhattacharyya.matrix, 14, <i>110</i>
localshape, 104	1.1
mahalanodisc, 105	calinhara, 4, 15, 34, 57, 100, 101, 122
mahalanofix, 106	can, 16, 85, 88
mahalconf, 107	cat2bin, 17
mergenormals, 108	cdbw, 18, 76, 77
mergeparameters, 112	cgrestandard, 19, 26, 39, 40

clara, 5, 45, 97–99, 122, 123	distancefactor, 68
claraCBI, 46, 120, 121, 131, 132	distcritmulti, 33, 34, 56, 57, 70, 122, 123
claraCBI (kmeansCBI), 95	disthclustCBI, 46
classifdist, 21, 120, 121, 132	disthclustCBI (kmeansCBI), 95
classifnp, 120, 121, 132, 133	disthclusttreeCBI (kmeansCBI), 95
classifnp (classifdist), 21	distnoisemclustCBI, 46
clucols, 23	distnoisemclustCBI (kmeansCBI), 95
clugrey (clucols), 23	distrsimilarity, 4, 26-28, 38, 39, 71, 135,
clujaccard, 24	154
clusexpect, 25, 86, 88, 93, 113, 114	dridgeline, 73, <i>143</i>
clustatsum, 19–21, 26, 39, 40, 136, 137	dudahart2, 4, 74, 100, 101, 122, 123
cluster.magazine, 29, 39, 40, 127, 128	addita: 02, 7, 7 1, 100, 101, 122, 120
cluster.stats, 16, 31, 51, 57, 71, 72, 74	eigen, <i>145</i>
cluster.varstats, 35	EMclust, <i>139</i>
clusterbenchstats, 19–21, 26, 30, 37, 51,	emskewCBI (kmeansCBI), 95
126–128, 154	extract.mixturepars, 75, 110
clusterboot, 34, 41, 57, 95, 98, 99, 120, 121,	one: accimization opar c, 70, 110
131	findrep, 76
	fixmahal, 45, 47, 48, 77, 88, 92, 97-99,
clusym (clucols), 23	106–108, 144, 157
cmahal, 47, 78, 79, 83	fixreg, 16, 17, 25, 83, 84, 92, 93, 113, 114,
cmdscale, 97	139, 144
con.comp, 48	flexmix, 4, 92, 102, 103, 139
confusion, 49, <i>159</i>	flexmixedruns, 89, 102, 103
cov, 51	fpc-package, 4
cov.rob, 8, 10, 78, 83, 106, 107, 116, 118	fpclusters, 92
cov.wml, 50, 83	fpclusters.mfpc(fixmahal),77
cov.wt, 50, 51	fpclusters.rfpc(fixreg), 84
covMcd, 104	fpmi (fixmahal), 77
cqcluster.stats, 4, 26–28, 34, 38–40, 51,	· p (· 1/a.1/31/), / /
72, 135, 153	grey, <i>23</i>
cutree, 49	
cvnn, 57	hc, 97
cweight, 59	hclust, 49, 96, 98, 99
da: 70	hclustCBI, 38, 46, 154
daisy, 70	hclustCBI (kmeansCBI), 95
data.matrix, 65	hclusttreeCBI,46
dbscan, 45, 59, 97–99	hclusttreeCBI (kmeansCBI), 95
dbscanCBI, 46	
dbscanCBI (kmeansCBI), 95	isoMDS, 97
density, 62, 152	itnumber, 85, 88, 93, 114
dip, 62, 63	
dip. test, 62, 63, 110	jitter, <i>94</i>
dipp.tantrum, 62, 110	jittervar, <mark>94</mark>
diptest.multi, 63	
discrcoord, 12, 13, 64, 67, 68, 129, 130, 151	kmeans, <i>5</i> , <i>44</i> , <i>98–101</i>
discrete.recode, 18, 65, 92, 103	kmeansCBI, 5, 27, 29, 30, 37, 38, 40, 44–46,
discrproj, 5, 7, 9, 11, 35, 36, 66, 117, 119,	95, 120, 121, 131, 133, 154
130	kmeansruns, 98, 99, 100
dist, 34, 46, 57, 70, 99	knn, 22

lcmixed, 66, 69, 92, 102	<pre>print.clboot(clusterboot), 41</pre>
lda, 22	<pre>print.clusterbenchstats</pre>
legend, <i>155</i>	(clusterbenchstats), 37
localshape, 104	print.dbscan(dbscan), 59
	<pre>print.mfpc(fixmahal), 77</pre>
mahalanodisc, 105	<pre>print.predstr(prediction.strength), 131</pre>
mahalanofix, 106	<pre>print.rfpc(fixreg), 84</pre>
mahalanofuz (mahalanofix), 106	print.summary.cquality
mahalCBI, 46	(cqcluster.stats), 51
mahalCBI (kmeansCBI), 95	<pre>print.summary.mergenorm (mergenormals),</pre>
mahalconf, <i>79</i> , <i>80</i> , <i>83</i> , 107	108
mclapply, 39, 135	<pre>print.summary.mfpc(fixmahal),77</pre>
mclustBIC, 43, 44, 75, 97–99, 109, 111	print.summary.rfpc(fixreg),84
mclustModelNames, 114	print.table, 127
mergenormals, 45, 97, 98, 108, 115, 116	print.valstat, 4, 37
mergenormCBI (kmeansCBI), 95	print.valstat(plot.valstat), 126
mergeparameters, 110, 112	<pre>print.varwisetables (cluster.varstats),</pre>
minsize, 88, 113	35
mixdens, 114	
mixpredictive, 110, 115	qda, 22
mvdcoord, 67, 68, 116, 129, 130	444, 22
	randcmatrix, 133, <i>138</i>
ncoord, 67, 68, 117, 129, 130	randconf, 134
neginc, 119	randomclustersim, 19, 20, 39, 126, 135
NNclean, 97, 99	regem (regmix), 137
noisemclustCBI, 46	regmix, 88, 134, 137
noisemclustCBI (kmeansCBI), 95	rFace, 7, 9, 11, 13, 65, 68, 83, 117, 119, 130,
nselectboot, 23, 27, 28, 38, 120, 136	140
pam, 5, 22, 45, 69, 97–99, 122, 123	rfpi (fixreg), 84
pam.object, 100, 122	ridgeline, 141, <i>143</i>
pamk, 45, 98, 99, 101, 122	ridgeline.diagnosis, <i>109</i> , <i>110</i> , 142
pamkCBI, 46, 120, 131	
pamkCBI (kmeansCBI), 95	sammon, 97
par, 80, 86, 130	sample, <i>134</i>
pdfclustCBI (kmeansCBI), 95	scale, 29, 38
pdfCluster, 98, 99	silhouette, 27, 33, 34, 55, 57, 71, 153
piridge, 124, <i>143</i>	simmatrix, 144
piridge.zeroes, 125, 143	solve, <i>145</i>
plot.clboot(clusterboot),41	solvecov, 80, 83, 105–108, 145
plot.dbscan (dbscan), 59	specc, <i>45</i> , <i>98</i>
plot.mfpc(fixmahal),77	speccCBI (kmeansCBI), 95
plot.rfpc(fixreg),84	sseg, <i>81–83</i> , <i>87</i> , <i>88</i> , <i>144</i> , 146
plot.valstat, 126, 154	stupidkaven, 21, 39, 99, 127, 135–137, 146,
plotcluster, 7, 9, 11, 13, 44, 65, 83, 117,	148–150
119, 128	stupidkavenCBI (kmeansCBI), 95
predict.dbscan (dbscan), 59	stupidkcentroids, 4, 21, 39, 98, 127,
prediction.strength, 23, 27, 28, 38, 116,	135–137, 147, 147, 149, 150
131, <i>136</i>	stupidkcentroidsCBI (kmeansCBI), 95

```
stupidkfn, 21, 39, 99, 127, 135-137, 147,
         148, 148, 150
stupidkfnCBI (kmeansCBI), 95
stupidknn, 4, 21, 39, 99, 127, 135-137,
         147–149, 149
stupidknnCBI (kmeansCBI), 95
summary.cquality, 27
summary.cquality(cqcluster.stats), 51
summary.mclustBIC, 75, 97, 109, 114, 155
summary.mergenorm (mergenormals), 108
summary.mfpc(fixmahal), 77
summary.rfpc(fixreg),84
table, 157
tclust, 43, 99
tclustCBI (kmeansCBI), 95
tdecomp, 7, 8, 10, 64, 150
tonedata, 151
try, 91
unimodal.ind, 152
valstat.object, 20, 21, 39, 40, 128, 152
var, 51
weightplots, 155
wfu, 78, 80, 83, 156
xtable, 157
zmisclassification.matrix, 158
```