# Package 'gelnet'

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Title Generalized Elastic Nets	
<b>Description</b> Implements several extensions of the elastic net regularization scheme. These extensions include individual feature penalties for the L1 term, feature-feature penalties for the L2 term, as well as translation coefficients for the latter.	
Author Artem Sokolov	
Maintainer Artem Sokolov <artem.sokolov@gmail.com></artem.sokolov@gmail.com>	
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adj2lapl

Generate a graph Laplacian

## **Description**

Generates a graph Laplacian from the graph adjacency matrix.

## Usage

```
adj2lapl(A)
```

## **Arguments**

Α

n-by-n adjacency matrix for a graph with n nodes

#### **Details**

A graph Laplacian is defined as:  $l_{i,j} = deg(v_i)$ , if i = j;  $l_{i,j} = -1$ , if  $i \neq j$  and  $v_i$  is adjacent to  $v_j$ ; and  $l_{i,j} = 0$ , otherwise

### Value

The n-by-n Laplacian matrix of the graph

#### See Also

adj2nlapl

adj2nlapl

Generate a normalized graph Laplacian

## **Description**

Generates a normalized graph Laplacian from the graph adjacency matrix.

#### Usage

```
adj2nlapl(A)
```

## **Arguments**

Α

n-by-n adjacency matrix for a graph with n nodes

## **Details**

A normalized graph Laplacian is defined as:  $l_{i,j}=1$ , if i=j;  $l_{i,j}=-1/\sqrt{deg(v_i)deg(v_j)}$ , if  $i\neq j$  and  $v_i$  is adjacent to  $v_j$ ; and  $l_{i,j}=0$ , otherwise

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## Value

The n-by-n Laplacian matrix of the graph

## See Also

```
adj2nlapl
```

gelnet	GELnet for linear regression, binary classification and one-class prob-
	lems.

## Description

Infers the problem type and learns the appropriate GELnet model via coordinate descent.

## Usage

```
gelnet(X, y, 11, 12, nFeats = NULL, a = rep(1, n), d = rep(1, p),
P = diag(p), m = rep(0, p), max.iter = 100, eps = 1e-05,
w.init = rep(0, p), b.init = NULL, fix.bias = FALSE, silent = FALSE,
balanced = FALSE, nonneg = FALSE)
```

## Arguments

n-by-p matrix of n samples in p dimensions
n-by-1 vector of response values. Must be numeric vector for regression, factor with 2 levels for binary classification, or NULL for a one-class task.
coefficient for the L1-norm penalty
coefficient for the L2-norm penalty
alternative parameterization that returns the desired number of non-zero weights. Takes precedence over 11 if not NULL (default: NULL)
n-by-1 vector of sample weights (regression only)
p-by-1 vector of feature weights
p-by-p feature association penalty matrix
p-by-1 vector of translation coefficients
maximum number of iterations
convergence precision
initial parameter estimate for the weights
initial parameter estimate for the bias term
set to TRUE to prevent the bias term from being updated (regression only) (default: FALSE)
set to TRUE to suppress run-time output to stdout (default: FALSE)
boolean specifying whether the balanced model is being trained (binary classification only) (default: FALSE)
set to TRUE to enforce non-negativity constraints on the weights (default: FALSE ) $$

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#### **Details**

The method determines the problem type from the labels argument y. If y is a numeric vector, then a regression model is trained by optimizing the following objective function:

$$\frac{1}{2n} \sum_{i} a_i (y_i - (w^T x_i + b))^2 + R(w)$$

If y is a factor with two levels, then the function returns a binary classification model, obtained by optimizing the following objective function:

$$-\frac{1}{n}\sum_{i}y_{i}s_{i} - \log(1 + \exp(s_{i})) + R(w)$$

where

$$s_i = w^T x_i + b$$

Finally, if no labels are provided (y == NULL), then a one-class model is constructed using the following objective function:

$$-\frac{1}{n}\sum_{i} s_i - \log(1 + \exp(s_i)) + R(w)$$

where

$$s_i = w^T x_i$$

In all cases, the regularizer is defined by

$$R(w) = \lambda_1 \sum_{j} d_j |w_j| + \frac{\lambda_2}{2} (w - m)^T P(w - m)$$

The training itself is performed through cyclical coordinate descent, and the optimization is terminated after the desired tolerance is achieved or after a maximum number of iterations.

## Value

A list with two elements:

w p-by-1 vector of p model weights

**b** scalar, bias term for the linear model (omitted for one-class models)

## See Also

```
gelnet.lin.obj, gelnet.logreg.obj, gelnet.oneclass.obj
```

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gelnet.cv	k-fold cross-validation for parameter tuning.

## **Description**

Performs k-fold cross-validation to select the best pair of the L1- and L2-norm penalty values.

## Usage

```
gelnet.cv(X, y, nL1, nL2, nFolds = 5, a = rep(1, n), d = rep(1, p), P = diag(p), m = rep(0, p), max.iter = 100, eps = 1e-05, w.init = rep(0, p), b.init = 0, fix.bias = FALSE, silent = FALSE, balanced = FALSE)
```

## **Arguments**

Χ	n-by-p matrix of n samples in p dimensions
у	n-by-1 vector of response values. Must be numeric vector for regression, factor with 2 levels for binary classification, or NULL for a one-class task.
nL1	number of values to consider for the L1-norm penalty
nL2	number of values to consider for the L2-norm penalty
nFolds	number of cross-validation folds (default:5)
a	n-by-1 vector of sample weights (regression only)
d	p-by-1 vector of feature weights
Р	p-by-p feature association penalty matrix
m	p-by-1 vector of translation coefficients
max.iter	maximum number of iterations
eps	convergence precision
w.init	initial parameter estimate for the weights
b.init	initial parameter estimate for the bias term
fix.bias	set to TRUE to prevent the bias term from being updated (regression only) (default: FALSE)
silent	set to TRUE to suppress run-time output to stdout (default: FALSE)
balanced	boolean specifying whether the balanced model is being trained (binary classification only) (default: FALSE)

#### **Details**

Cross-validation is performed on a grid of parameter values. The user specifies the number of values to consider for both the L1- and the L2-norm penalties. The L1 grid values are equally spaced on [0, L1s], where L1s is the smallest meaningful value of the L1-norm penalty (i.e., where all the model weights are just barely zero). The L2 grid values are on a logarithmic scale centered on 1.

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## Value

A list with the following elements:

- 11 the best value of the L1-norm penalty
- 12 the best value of the L2-norm penalty
- w p-by-1 vector of p model weights associated with the best (11,12) pair.
- **b** scalar, bias term for the linear model associated with the best (11,12) pair. (omitted for one-class models)

**perf** performance value associated with the best model. (Likelihood of data for one-class, AUC for binary classification, and -RMSE for regression)

#### See Also

gelnet

gelnet.ker	Kernel models for linear regression, binary classification and one- class problems.

## **Description**

Infers the problem type and learns the appropriate kernel model.

## Usage

```
gelnet.ker(K, y, lambda, a, max.iter = 100, eps = 1e-05, v.init = rep(0,
nrow(K)), b.init = 0, fix.bias = FALSE, silent = FALSE,
balanced = FALSE)
```

#### **Arguments**

K	n-by-n matrix of pairwise kernel values over a set of n samples
У	n-by-1 vector of response values. Must be numeric vector for regression, factor with 2 levels for binary classification, or NULL for a one-class task.
lambda	scalar, regularization parameter
а	n-by-1 vector of sample weights (regression only)
max.iter	maximum number of iterations (binary classification and one-class problems only)
eps	convergence precision (binary classification and one-class problems only)
v.init	initial parameter estimate for the kernel weights (binary classification and one- class problems only)
b.init	initial parameter estimate for the bias term (binary classification only)
fix.bias	set to TRUE to prevent the bias term from being updated (regression only) (default: FALSE)

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silent set to TRUE to suppress run-time output to stdout (default: FALSE)

balanced boolean specifying whether the balanced model is being trained (binary classification only) (default: FALSE)

#### **Details**

The entries in the kernel matrix K can be interpreted as dot products in some feature space  $\phi$ . The corresponding weight vector can be retrieved via  $w = \sum_i v_i \phi(x_i)$ . However, new samples can be classified without explicit access to the underlying feature space:

$$w^{T}\phi(x) + b = \sum_{i} v_{i}\phi^{T}(x_{i})\phi(x) + b = \sum_{i} v_{i}K(x_{i}, x) + b$$

The method determines the problem type from the labels argument y. If y is a numeric vector, then a ridge regression model is trained by optimizing the following objective function:

$$\frac{1}{2n} \sum_{i} a_i (z_i - (w^T x_i + b))^2 + w^T w$$

If y is a factor with two levels, then the function returns a binary classification model, obtained by optimizing the following objective function:

$$-\frac{1}{n}\sum_{i}y_{i}s_{i} - \log(1 + \exp(s_{i})) + w^{T}w$$

where

$$s_i = w^T x_i + b$$

Finally, if no labels are provided (y == NULL), then a one-class model is constructed using the following objective function:

$$-\frac{1}{n}\sum_{i} s_i - \log(1 + \exp(s_i)) + w^T w$$

where

$$s_i = w^T x_i$$

In all cases,  $w = \sum_i v_i \phi(x_i)$  and the method solves for  $v_i$ .

#### Value

A list with two elements:

v n-by-1 vector of kernel weights

**b** scalar, bias term for the linear model (omitted for one-class models)

## See Also

gelnet.lin.obj

gelnet.lin.obj

Linear regression objective function value

## **Description**

Evaluates the linear regression objective function value for a given model. See details.

## Usage

```
gelnet.lin.obj(w, b, X, z, l1, l2, a = rep(1, nrow(X)), d = rep(1, ncol(X)), P = diag(ncol(X)), m = rep(0, ncol(X)))
```

#### **Arguments**

W	p-by-1 vector of model weights
b	the model bias term
Χ	n-by-p matrix of n samples in p dimensions
z	n-by-1 response vector
11	L1-norm penalty scaling factor $\lambda_1$
12	L2-norm penalty scaling factor $\lambda_2$
а	n-by-1 vector of sample weights
d	p-by-1 vector of feature weights
Р	p-by-p feature-feature penalty matrix
m	p-by-1 vector of translation coefficients

## **Details**

Computes the objective function value according to

$$\frac{1}{2n} \sum_{i} a_i (z_i - (w^T x_i + b))^2 + R(w)$$

where

$$R(w) = \lambda_1 \sum_{j} d_j |w_j| + \frac{\lambda_2}{2} (w - m)^T P(w - m)$$

## Value

The objective function value.

#### See Also

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gelnet.logreg.obj

Logistic regression objective function value

## **Description**

Evaluates the logistic regression objective function value for a given model. See details. Computes the objective function value according to

$$-\frac{1}{n}\sum_{i}y_{i}s_{i} - \log(1 + \exp(s_{i})) + R(w)$$

where

$$s_i = w^T x_i + b$$

$$R(w) = \lambda_1 \sum_j d_j |w_j| + \frac{\lambda_2}{2} (w - m)^T P(w - m)$$

When balanced is TRUE, the loss average over the entire data is replaced with averaging over each class separately. The total loss is then computes as the mean over those per-class estimates.

## Usage

```
gelnet.logreg.obj(w, b, X, y, l1, l2, d = rep(1, ncol(X)),
P = diag(ncol(X)), m = rep(0, ncol(X)), balanced = FALSE)
```

## **Arguments**

W	p-by-1 vector of model weights
b	the model bias term
X	n-by-p matrix of n samples in p dimensions
у	n-by-1 binary response vector sampled from 0,1
11	L1-norm penalty scaling factor $\lambda_1$
12	L2-norm penalty scaling factor $\lambda_2$
d	p-by-1 vector of feature weights
P	p-by-p feature-feature penalty matrix
m	p-by-1 vector of translation coefficients
balanced	boolean specifying whether the balanced model is being evaluated

### Value

The objective function value.

#### See Also

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gelnet.oneclass.obj One-class regression objective function value

## **Description**

Evaluates the one-class objective function value for a given model See details.

## Usage

```
gelnet.oneclass.obj(w, X, l1, l2, d = rep(1, ncol(X)), P = diag(ncol(X)), m = rep(0, ncol(X)))
```

## **Arguments**

W	p-by-1 vector of model weights
Χ	n-by-p matrix of n samples in p dimensions
11	L1-norm penalty scaling factor $\lambda_1$
12	L2-norm penalty scaling factor $\lambda_2$
d	p-by-1 vector of feature weights
P	p-by-p feature-feature penalty matrix
m	p-by-1 vector of translation coefficients

## **Details**

Computes the objective function value according to

$$-\frac{1}{n}\sum_{i} s_i - \log(1 + \exp(s_i)) + R(w)$$

where

$$s_i = w^T x_i$$

$$R(w) = \lambda_1 \sum_j d_j |w_j| + \frac{\lambda_2}{2} (w - m)^T P(w - m)$$

## Value

The objective function value.

## See Also

L1.ceiling

L1.ceiling	The largest meaningful value of the L1 parameter
5	o w J

## **Description**

Computes the smallest value of the LASSO coefficient L1 that leads to an all-zero weight vector for a given linear regression problem.

#### Usage

```
L1.ceiling(X, y, a = rep(1, nrow(X)), d = rep(1, ncol(X)),

P = diag(ncol(X)), m = rep(0, ncol(X)), 12 = 1, balanced = FALSE)
```

## **Arguments**

Χ	n-by-p matrix of n samples in p dimensions
У	n-by-1 vector of response values. Must be numeric vector for regression, factor with 2 levels for binary classification, or NULL for a one-class task.
а	n-by-1 vector of sample weights (regression only)
d	p-by-1 vector of feature weights
Р	p-by-p feature association penalty matrix
m	p-by-1 vector of translation coefficients
12	coefficient for the L2-norm penalty
balanced	boolean specifying whether the balanced model is being trained (binary classification only) (default: FALSE)

## **Details**

The cyclic coordinate descent updates the model weight  $w_k$  using a soft threshold operator  $S(\cdot, \lambda_1 d_k)$  that clips the value of the weight to zero, whenever the absolute value of the first argument falls below  $\lambda_1 d_k$ . From here, it is straightforward to compute the smallest value of  $\lambda_1$ , such that all weights are clipped to zero.

#### Value

The largest meaningful value of the L1 parameter (i.e., the smallest value that yields a model with all zero weights)

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