# Package 'hSDM'

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Maintainer Ghislain Vieilledent <ghislain.vieilledent@cirad.fr>

Description User-friendly and fast set of functions for estimating parameters of hierarchical Bayesian species distribution models (Latimer et al. 2006 <doi:10.1890/04-0609>). Such models allow interpreting the observations (occurrence and abundance of a species) as a result of several hierarchical processes including ecological processes (habitat suitability, spatial dependence and anthropogenic disturbance) and observation processes (species detectability). Hierarchical species distribution models are essential for accurately characterizing the environmental response of species, predicting their probability of occurrence, and assessing uncertainty in the model results.

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 https://github.com/ghislainv/hSDM

BugReports https://github.com/ghislainv/hSDM/issues

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Author Ghislain Vieilledent [aut, cre]
(<a href="https://orcid.org/0000-0002-1685-4997">https://orcid.org/0000-0002-1685-4997</a>),
Matthieu Autier [ctb],
Alan E. Gelfand [ctb],
Jérôme Guélat [ctb],
Marc Kéry [ctb],

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Andrew M. Latimer [ctb], Cory Merow [ctb], Frédéric Mortier [ctb], John A. Silander Jr. [ctb], Adam M. Wilson [ctb], Shanshan Wu [ctb], CIRAD [cph, fnd]

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hSDM-package

hierarchical Bayesian species distribution models

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# **Description**

hSDM is an R package for estimating parameters of hierarchical Bayesian species distribution models. Such models allow interpreting the observations (occurrence and abundance of a species) as a result of several hierarchical processes including ecological processes (habitat suitability, spatial dependence and anthropogenic disturbance) and observation processes (species detectability). Hierarchical species distribution models are essential for accurately characterizing the environmental response of species, predicting their probability of occurrence, and assessing uncertainty in the model results.

#### **Details**

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# Author(s)

Ghislain Vieilledent <ghislain.vieilledent@cirad.fr>
Cory Merow <cory.merow@gmail.com>
Jérôme Guélat <jerome.guelat@vogelwarte.ch>
Andrew M. Latimer <amlatimer@ucdavis.edu>
Marc Kéry <marc.kery@vogelwarte.ch>
Alan E. Gelfand <alan@stat.duke.edu>
Adam M. Wilson <adam.wilson@yale.edu>
Frédéric Mortier <frederic.mortier@cirad.fr>
John A. Silander Jr. <john.silander@uconn.edu>

altitude Virtual altitudinal data

# **Description**

Data frame with virtual altitudinal data. The data frame is used in the examples of the hSDM package vignette to derive an altitude raster determining species habitat suitability.

4 cfr.env

# Usage

altitude

#### **Format**

altitude is a data frame with 2500 observations (50 x 50 cells) and 3 variables:

x coordinates of the center of the cell on the x axis y coordinates of the center of the cell on the y axis

altitude altitude (m)

cfr.env

Environmental data for South Africa's Cap Floristic Region

# Description

Data include environmental variables for 36909 one minute by one minute grid cells on the whole South Africa's Cap Floristic Region.

## Usage

cfr.env

#### **Format**

cfr.env is a data frame with 36909 observations (cells) on the following six environmental variables.

1on longitude

lat latitude

min07 minimum temperature of the coldest month (July)

smdwin winter soil moisture days

fert3 moderately high fertility (percent of grid cell)

ph1 acidic soil (percent of grid cell)

text1 fine soil texture (percent of grid cell)

text2 moderately fine soil texture (percent of grid cell)

# Source

Cory Merow's personal data

#### References

Latimer, A. M.; Wu, S. S.; Gelfand, A. E. and Silander, J. A. (2006) Building statistical models to analyze species distributions. *Ecological Applications*, 16, 33-50.

data.Kery2010 5

data.Kery2010

Count data for the Willow tit (from Kéry and Royle 2010)

# **Description**

Repeated count data for the Willow tit (*Poecile montanus*, a pesserine bird) in Switzerland on the period 1999-2003. Data come from the Swiss national breeding bird survey MHB (Monitoring Haüfige Brutvögel).

# Usage

```
data.Kery2010
```

## **Format**

data.Kery2010 is a data frame with 264 observations (1 km<sup>2</sup> quadrats) and the following 10 variables.

```
coordx quadrat x coordinate
coordy quadrat y coordinate
elevation mean quadrat elevation (m)
forest quadrat forest cover (in %)
count1 count for survey 1
count2 count for survey 2
count3 count for survey 3
juldate1 Julian date of survey 1
juldate2 Julian date of survey 2
juldate3 Julian date of survey 3
```

# Source

Kéry and Royle, 2010, Journal of Animal Ecology, 79, 453-461.

# References

Kéry, M. and Andrew Royle, J. 2010. Hierarchical modelling and estimation of abundance and population trends in metapopulation designs. *Journal of Animal Ecology*, 79, 453-461.

6 datacells.Latimer2006

datacells.Latimer2006 Data of presence-absence (from Latimer et al. 2006)

## **Description**

Data come from a small region including 476 one minute by one minute grid cells. This region is a small corner of South Africa's Cape Floristic Region, and includes very high plant species diversity and a World Biosphere Reserve. The data frame can be used as an example for several functions in the hSDM package.

# Usage

datacells.Latimer2006

#### **Format**

datacells.Latimer2006 is a data frame with 476 observations (cells) on the following 9 variables.

y the number of times the species was observed to be present in each cell

n the number of visits or sample locations in each cell (which can be zero)

rough elevational range or "roughness"

julmint July minimum temperature

pptcv interannual variation in precipitation

smdsum summer soil moisture days

evi enhanced vegetation or "greenness" index

ph1 percent acidic soil

num number of neighbors of each cell, this is a sparse representation of the adjacency matrix for the subregion.

#### Source

Latimer et al. (2006) Ecological Applications, Appendix B

#### References

Latimer, A. M.; Wu, S. S.; Gelfand, A. E. and Silander, J. A. (2006) Building statistical models to analyze species distributions. *Ecological Applications*, 16, 33-50.

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frogs

Counts of the number of frogs in a water body

#### **Description**

Counts of the number of frogs in ponds of the Canton Aargau, Switzerland.

# Usage

```
data(frogs)
```

#### **Format**

A data frame with 481 observations on the following 10 variables.

count1 number of counted frogs during the first visit

count2 number of counted frogs uring the second visit

elevation elevation, meters above sea level

year year

fish presence of fish (1 = present, 0 = absent)

waterarea area of the water body in square meters

vegetation indicator of vegetation (1 = vegetation present, 0 = no vegetation present)

pondid name of the pond, corresponds to observation id

x x coordinate

y y coordinate

#### **Details**

The amphibian monitoring program started in 1999 and is mainly aimed at surveying population trends of endangered amphibian species. Every year, about 30 water bodies in two or three randomly selected priority areas (out of ten priority areas of high amphibian diversity) are surveyed. Additionally, a random selection of water bodies that potentially are suitable for one of the endangered amphibian species but that do not belong to the priority areas were surveyed. Each water body is surveyed by single trained volunteer during two nocturnal visits per year. Volunteers recorded anurans by walking along the water's edge with precise rules for the duration of a survey taking account of the size of the surveyed water body and noting visual encounters and calls. As fare as possible, encountered individuals of the Pelophylax-complex were identified as Marsh Frog (Pelophylax ridibundus), Pool Frog (P. lessonaea) or hybrids (P. esculentus) based on morphological characteristics or based on their calls. In the given data set, however, these three taxa are lumped together.

#### **Source**

The data is provided by Isabelle Floess, Landschaft und Gewaesser, Kanton Aargau.

8 hSDM.binomial

## References

Schmidt, B. R., 2005: Monitoring the distribution of pond-breeding amphibians, when species are detected imperfectly. - Aquatic conservation: marine and freshwater ecosystems 15: 681-692.

Tanadini, L. G.; Schmidt, B. R., 2011: Population size influences amphibian detection probability: implications for biodiversity monitoring programs. - Plos One 6: e28244.

## **Examples**

data(frogs)

hSDM.binomial

Binomial logistic regression model

# **Description**

The hSDM.binomial function performs a Binomial logistic regression in a Bayesian framework. The function calls a Gibbs sampler written in C code which uses an adaptive Metropolis algorithm to estimate the conditional posterior distribution of model's parameters.

# Usage

```
hSDM.binomial(presences, trials, suitability, data, suitability.pred = NULL, burnin = 5000, mcmc = 10000, thin = 10, beta.start, mubeta = 0, Vbeta = 1e+06, seed = 1234, verbose = 1, save.p = 0)
```

## **Arguments**

presences	A vector indicating the number of successes (or presences) for each observation.	
trials	A vector indicating the number of trials for each observation. $t_n$ should be superior or equal to $y_n$ , the number of successes for observation $n$ . If $t_n=0$ , then $y_n=0$ .	
suitability	A one-sided formula of the form $`\sim x1++xp"$ with p terms specifying the explicative variables for the suitability process of the model.	
data	A data frame containing the model's explicative variables.	
suitability.pred		
	An optional data frame in which to look for variables with which to predict. If NULL, the observations are used.	
burnin	The number of burnin iterations for the sampler.	
mcmc	The number of Gibbs iterations for the sampler. Total number of Gibbs iterations is equal to burnin+mcmc. burnin+mcmc must be divisible by 10 and superior or equal to 100 so that the progress bar can be displayed.	
thin	The thinning interval used in the simulation. The number of mcmc iterations	

must be divisible by this value.

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beta.start Starting values for beta parameters of the suitability process. If beta.start

takes a scalar value, then that value will serve for all of the betas.

mubeta Means of the priors for the  $\beta$  parameters of the suitability process. mubeta must

be either a scalar or a p-length vector. If mubeta takes a scalar value, then that value will serve as the prior mean for all of the betas. The default value is set to

0 for an uninformative prior.

Vbeta Variances of the Normal priors for the  $\beta$  parameters of the suitability process.

Vbeta must be either a scalar or a p-length vector. If Vbeta takes a scalar value, then that value will serve as the prior variance for all of the betas. The default

variance is large and set to 1.0E6 for an uninformative flat prior.

seed The seed for the random number generator. Default to 1234.

verbose A switch (0,1) which determines whether or not the progress of the sampler is

printed to the screen. Default is 1: a progress bar is printed, indicating the step

(in %) reached by the Gibbs sampler.

save.p A switch (0,1) which determines whether or not the sampled values for predic-

tions are saved. Default is 0: the posterior mean is computed and returned in the theta.pred vector. Be careful, setting save.p to 1 might require a large

amount of memory.

#### **Details**

We model an ecological process where the presence or absence of the species is explained by habitat suitability.

## **Ecological process:**

$$y_i \sim \mathcal{B}inomial(\theta_i, t_i)$$

$$logit(\theta_i) = X_i\beta$$

## Value

mcmc An mcmc object that contains the posterior sample. This object can be summa-

rized by functions provided by the coda package. The posterior sample of the

deviance D, with  $D = -2\log(\prod_i P(y_i|\beta, t_i))$ , is also provided.

theta.pred If save.p is set to 0 (default), theta.pred is the predictive posterior mean of the

probability associated to the suitability process for each prediction. If save.p is set to 1, theta.pred is an mcmc object with sampled values of the probability

associated to the suitability process for each prediction.

theta.latent Predictive posterior mean of the probability associated to the suitability process

for each observation.

# Author(s)

Ghislain Vieilledent <ghislain.vieilledent@cirad.fr>

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## References

Gelfand, A. E.; Schmidt, A. M.; Wu, S.; Silander, J. A.; Latimer, A. and Rebelo, A. G. (2005) Modelling species diversity through species level hierarchical modelling. *Applied Statistics*, 54, 1-20.

Latimer, A. M.; Wu, S. S.; Gelfand, A. E. and Silander, J. A. (2006) Building statistical models to analyze species distributions. *Ecological Applications*, 16, 33-50.

#### See Also

```
plot.mcmc, summary.mcmc
```

# **Examples**

```
## Not run:
# hSDM.binomial()
# Example with simulated data
#========
#== Load libraries
library(hSDM)
#========
#== Data simulation
#= Number of sites
nsite <- 200
#= Set seed for repeatability
seed <- 1234
#= Number of visits associated to each site
set.seed(seed)
visits<- rpois(nsite,3)</pre>
visits[visits==0] <- 1</pre>
#= Ecological process (suitability)
set.seed(seed)
x1 <- rnorm(nsite,0,1)</pre>
set.seed(2*seed)
x2 <- rnorm(nsite, 0, 1)
X <- cbind(rep(1,nsite),x1,x2)</pre>
beta.target <- c(-1,1,-1)
logit.theta <- X %*% beta.target</pre>
theta <- inv.logit(logit.theta)</pre>
set.seed(seed)
Y <- rbinom(nsite, visits, theta)
```

```
#= Data-sets
data.obs <- data.frame(Y,visits,x1,x2)</pre>
#== Site-occupancy model
mod.hSDM.binomial <- hSDM.binomial(presences=data.obs$Y,</pre>
                                   trials=data.obs$visits,
                                   suitability=~x1+x2,
                                   data=data.obs,
                                   suitability.pred=NULL,
                                   burnin=1000, mcmc=1000, thin=1,
                                   beta.start=0,
                                   mubeta=0, Vbeta=1.0E6,
                                   seed=1234, verbose=1,
                                   save.p=0)
#=======
#== Outputs
#= Parameter estimates
summary(mod.hSDM.binomial$mcmc)
pdf(file="Posteriors_hSDM.binomial.pdf")
plot(mod.hSDM.binomial$mcmc)
dev.off()
#== glm resolution to compare
mod.glm <- glm(cbind(Y,visits-Y)~x1+x2,family="binomial",data=data.obs)</pre>
summary(mod.glm)
#= Predictions
summary(mod.hSDM.binomial$theta.latent)
summary(mod.hSDM.binomial$theta.pred)
pdf(file="Pred-Init.pdf")
plot(theta,mod.hSDM.binomial$theta.pred)
abline(a=0,b=1,col="red")
dev.off()
## End(Not run)
```

hSDM.binomial.iCAR

Binomial logistic regression model with CAR process

# **Description**

The hSDM.binomial.iCAR function performs a Binomial logistic regression model in a hierarchical Bayesian framework. The suitability process includes a spatial correlation process. The spatial correlation is modelled using an intrinsic CAR model. The hSDM.binomial.iCAR function calls

a Gibbs sampler written in C code which uses an adaptive Metropolis algorithm to estimate the conditional posterior distribution of hierarchical model's parameters.

# Usage

```
hSDM.binomial.iCAR(presences, trials, suitability, spatial.entity, data, n.neighbors, neighbors, suitability.pred=NULL, spatial.entity.pred=NULL, burnin = 5000, mcmc = 10000, thin = 10, beta.start, Vrho.start, mubeta = 0, Vbeta = 1e+06, priorVrho = "1/Gamma", shape = 0.5, rate = 0.0005, Vrho.max=1000, seed = 1234, verbose = 1, save.rho = 0, save.p = 0)
```

## **Arguments**

presences A vector indicating the number of successes (or presences) for each observation. trials A vector indicating the number of trials for each observation.  $t_i$  should be superior to zero and superior or equal to  $y_i$ , the number of successes for observation i.

suitability A one-sided formula of the form  $\sim x_1 + ... + x_p$  with p terms specifying the explicative variables for the suitability process.

spatial.entity A vector indicating the spatial entity identifier (from one to the total number of entities) for each observation. Several observations can occur in one spatial entity. A spatial entity can be a raster cell for example.

data A data frame containing the model's variables.

n.neighbors A vector of integers that indicates the number of neighbors (adjacent entities) of each spatial entity. length(n.neighbors) indicates the total number of spatial

entities.

A vector of integers indicating the neighbors (adjacent entities) of each spatial entity. Must be of the form c(neighbors of entity 1, neighbors of entity 2, ..., neighbors of the last entity). Length of the neighbors vector should be equal to sum(n.neighbors).

suitability.pred

neighbors

mcmc

An optional data frame in which to look for variables with which to predict. If NULL, the observations are used.

spatial.entity.pred

An optional vector indicating the spatial entity identifier (from one to the total number of entities) for predictions. If NULL, the vector spatial.entity for observations is used.

burnin The number of burnin iterations for the sampler.

The number of Gibbs iterations for the sampler. Total number of Gibbs iterations is equal to burn integer, burn integer, burninteger must be divisible by 10 and superior or

is equal to burnin+mcmc. burnin+mcmc must be divisible by 10 and superior or

equal to 100 so that the progress bar can be displayed.

thin The thinning interval used in the simulation. The number of mcmc iterations

must be divisible by this value.

beta. start Starting values for  $\beta$  parameters of the suitability process. This can either be a

scalar or a p-length vector.

Vrho.start	Positive scalar indicating the starting value for the variance of the spatial random effects.
mubeta	Means of the priors for the $\beta$ parameters of the suitability process. mubeta must be either a scalar or a p-length vector. If mubeta takes a scalar value, then that value will serve as the prior mean for all of the betas. The default value is set to 0 for an uninformative prior.
Vbeta	Variances of the Normal priors for the $\beta$ parameters of the suitability process. Vbeta must be either a scalar or a p-length vector. If Vbeta takes a scalar value, then that value will serve as the prior variance for all of the betas. The default variance is large and set to 1.0E6 for an uninformative flat prior.
priorVrho	Type of prior for the variance of the spatial random effects. Can be set to a fixed positive scalar, or to an inverse-gamma distribution ("1/Gamma") with parameters shape and rate, or to a uniform distribution ("Uniform") on the interval [0,Vrho.max]. Default set to "1/Gamma".
shape	The shape parameter for the Gamma prior on the precision of the spatial random effects. Default value is shape=0.05 for uninformative prior.
rate	The rate (1/scale) parameter for the Gamma prior on the precision of the spatial random effects. Default value is rate=0.0005 for uninformative prior.
Vrho.max	Upper bound for the uniform prior of the spatial random effect variance. Default set to 1000.
seed	The seed for the random number generator. Default set to 1234.
verbose	A switch $(0,1)$ which determines whether or not the progress of the sampler is printed to the screen. Default is 1: a progress bar is printed, indicating the step (in %) reached by the Gibbs sampler.
save.rho	A switch (0,1) which determines whether or not the sampled values for rhos are saved. Default is 0: the posterior mean is computed and returned in the rho.pred vector. Be careful, setting save.rho to 1 might require a large amount of memory.
save.p	A switch $(0,1)$ which determines whether or not the sampled values for predictions are saved. Default is 0: the posterior mean is computed and returned in the theta.pred vector. Be careful, setting save.p to 1 might require a large amount of memory.

# **Details**

We model an ecological process where the presence or absence of the species is explained by habitat suitability. The ecological process includes an intrinsic conditional autoregressive (iCAR) model for spatial autocorrelation between observations, assuming that the probability of presence of the species at one site depends on the probability of presence of the species on neighboring sites.

# **Ecological process:**

$$y_i \sim \mathcal{B}inomial(\theta_i, t_i)$$
  
 $logit(\theta_i) = X_i\beta + \rho_{j(i)}$ 

 $\rho_i$ : spatial random effect

j(i): index of the spatial entity for observation i.

#### **Spatial autocorrelation:**

An intrinsic conditional autoregressive model (iCAR) is assumed:

$$\rho_j \sim \mathcal{N}ormal(\mu_j, V_\rho/n_j)$$

 $\mu_i$ : mean of  $\rho_{i'}$  in the neighborhood of j.

 $V_{\rho}$ : variance of the spatial random effects.

 $n_i$ : number of neighbors for spatial entity j.

#### Value

mcmc An mcmc object that contains the posterior sample. This object can be summa-

rized by functions provided by the coda package. The posterior sample of the

deviance D, with  $D = -2 \log(\prod_i P(y_i|...))$ , is also provided.

rho.pred If save.rho is set to 0 (default), rho.pred is the predictive posterior mean of

the spatial random effect associated to each spatial entity. If save.rho is set to 1, rho.pred is an mcmc object with sampled values for each spatial random

effect associated to each spatial entity.

theta.pred If save.p is set to 0 (default), theta.pred is the predictive posterior mean of the

probability associated to the suitability process for each prediction. If save.p is set to 1, theta.pred is an mcmc object with sampled values of the probability

associated to the suitability process for each prediction.

theta.latent Predictive posterior mean of the probability associated to the suitability process

for each observation.

#### Author(s)

Ghislain Vieilledent <ghislain.vieilledent@cirad.fr>

## References

Gelfand, A. E.; Schmidt, A. M.; Wu, S.; Silander, J. A.; Latimer, A. and Rebelo, A. G. (2005) Modelling species diversity through species level hierarchical modelling. *Applied Statistics*, 54, 1-20.

Latimer, A. M.; Wu, S. S.; Gelfand, A. E. and Silander, J. A. (2006) Building statistical models to analyze species distributions. *Ecological Applications*, 16, 33-50.

Lichstein, J. W.; Simons, T. R.; Shriner, S. A. & Franzreb, K. E. (2002) Spatial autocorrelation and autoregressive models in ecology *Ecological Monographs*, 72, 445-463.

Diez, J. M. & Pulliam, H. R. (2007) Hierarchical analysis of species distributions and abundance across environmental gradients *Ecology*, 88, 3144-3152.

# See Also

plot.mcmc, summary.mcmc

## **Examples**

```
## Not run:
# hSDM.binomial.iCAR()
# Example with simulated data
#=========
#== Load libraries
library(hSDM)
library(raster)
library(sp)
#== Multivariate normal distribution
rmvn <- function(n, mu = 0, V = matrix(1), seed=1234) {
   p <- length(mu)</pre>
   if (any(is.na(match(dim(V), p)))) {
       stop("Dimension problem!")
   D <- chol(V)
   set.seed(seed)
   t(matrix(rnorm(n*p),ncol=p)%*%D+rep(mu,rep(n,p)))
}
#========
#== Data simulation
#= Set seed for repeatability
seed <- 1234
#= Landscape
xLand <- 30
yLand <- 30
Landscape <- raster(ncol=xLand,nrow=yLand,crs='+proj=utm +zone=1')</pre>
Landscape[] <- 0
extent(Landscape) <- c(0,xLand,0,yLand)</pre>
coords <- coordinates(Landscape)</pre>
ncells <- ncell(Landscape)</pre>
#= Neighbors
neighbors.mat <- adjacent(Landscape, cells=c(1:ncells), directions=8, pairs=TRUE, sorted=TRUE)</pre>
n.neighbors <- as.data.frame(table(as.factor(neighbors.mat[,1])))[,2]</pre>
adj <- neighbors.mat[,2]</pre>
#= Generate symmetric adjacency matrix, A
A <- matrix(0,ncells,ncells)
index.start <- 1</pre>
for (i in 1:ncells) {
   index.end <- index.start+n.neighbors[i]-1</pre>
```

```
A[i,adj[c(index.start:index.end)]] <- 1
    index.start <- index.end+1</pre>
}
#= Spatial effects
Vrho.target <- 5</pre>
d <- 1 # Spatial dependence parameter = 1 for intrinsic CAR
Q \leftarrow diag(n.neighbors)-d*A + diag(.0001,ncells) \# Add small constant to make <math>Q non-singular
covrho <- Vrho.target*solve(Q) # Covariance of rhos</pre>
set.seed(seed)
rho <- c(rmvn(1,mu=rep(0,ncells),V=covrho,seed=seed)) # Spatial Random Effects</pre>
rho <- rho-mean(rho) # Centering rhos on zero</pre>
#= Raster and plot spatial effects
r.rho <- rasterFromXYZ(cbind(coords,rho))</pre>
plot(r.rho)
#= Sample the observation sites in the landscape
nsite <- 250
set.seed(seed)
x.coord <- runif(nsite,0,xLand)</pre>
set.seed(2*seed)
y.coord <- runif(nsite,0,yLand)</pre>
sites.sp <- SpatialPoints(coords=cbind(x.coord,y.coord))</pre>
cells <- extract(Landscape, sites.sp, cell=TRUE)[,1]</pre>
#= Number of visits associated to each observation point
set.seed(seed)
visits <- rpois(nsite,3)</pre>
visits[visits==0] <- 1</pre>
#= Ecological process (suitability)
set.seed(seed)
x1 <- rnorm(nsite,0,1)</pre>
set.seed(2*seed)
x2 <- rnorm(nsite, 0, 1)
X <- cbind(rep(1,nsite),x1,x2)</pre>
beta.target <- c(-1,1,-1)
logit.theta <- X %*% beta.target + rho[cells]</pre>
theta <- inv.logit(logit.theta)</pre>
set.seed(seed)
Y <- rbinom(nsite, visits, theta)
#= Relative importance of spatial random effects
RImp <- mean(abs(rho[cells])/abs(X %*% beta.target))</pre>
RImp
#= Data-sets
data.obs <- data.frame(Y,visits,x1,x2,cell=cells)</pre>
#== Site-occupancy model
```

```
Start <- Sys.time() # Start the clock</pre>
mod.hSDM.binomial.iCAR <- hSDM.binomial.iCAR(presences=data.obs$Y,</pre>
                                                 trials=data.obs$visits,
                                                 suitability=\sim x1+x2,
                                                 spatial.entity=data.obs$cell,
                                                 data=data.obs,
                                                 n.neighbors=n.neighbors,
                                                 neighbors=adj,
                                                 suitability.pred=NULL,
                                                 spatial.entity.pred=NULL,
                                                 burnin=5000, mcmc=5000, thin=5,
                                                 beta.start=0,
                                                 Vrho.start=1,
                                                 mubeta=0, Vbeta=1.0E6,
                                                 priorVrho="1/Gamma",
                                                 shape=0.5, rate=0.0005,
                                                 seed=1234, verbose=1,
                                                 save.rho=1, save.p=0)
Time.hSDM <- difftime(Sys.time(),Start,units="sec") # Time difference</pre>
#= Computation time
Time.hSDM
#=======
#== Outputs
#= Parameter estimates
summary(mod.hSDM.binomial.iCAR$mcmc)
pdf("Posteriors_hSDM.binomial.iCAR.pdf")
plot(mod.hSDM.binomial.iCAR$mcmc)
dev.off()
#= Predictions
summary(mod.hSDM.binomial.iCAR$theta.latent)
summary(mod.hSDM.binomial.iCAR$theta.pred)
pdf(file="Pred-Init.pdf")
plot(theta,mod.hSDM.binomial.iCAR$theta.pred)
abline(a=0,b=1,col="red")
dev.off()
#= Summary plots for spatial random effects
# rho.pred
rho.pred <- apply(mod.hSDM.binomial.iCAR$rho.pred,2,mean)</pre>
r.rho.pred <- rasterFromXYZ(cbind(coords,rho.pred))</pre>
pdf(file="Summary_hSDM.binomial.iCAR.pdf")
par(mfrow=c(2,2))
# rho target
plot(r.rho, main="rho target")
plot(sites.sp,add=TRUE)
# rho estimated
```

hSDM.Nmixture

N-mixture model

## **Description**

The hSDM.Nmixture function can be used to model species distribution including different processes in a hierarchical Bayesian framework: a  $\mathcal{P}oisson$  suitability process (refering to environmental suitability explaining abundance) and a  $\mathcal{B}inomial$  observability process (refering to various ecological and methodological issues explaining species detection). The hSDM.Nmixture function calls a Gibbs sampler written in C code which uses an adaptive Metropolis algorithm to estimate the conditional posterior distribution of hierarchical model's parameters.

# Usage

```
hSDM.Nmixture(# Observations
                     counts, observability, site, data.observability,
                     # Habitat
                     suitability, data.suitability,
                     # Predictions
                     suitability.pred = NULL,
                     # Chains
                     burnin = 5000, mcmc = 10000, thin = 10,
                     # Starting values
                     beta.start,
                     gamma.start,
                     # Priors
                     mubeta = 0, Vbeta = 1.0E6,
                     mugamma = 0, Vgamma = 1.0E6,
                     # Various
                     seed = 1234, verbose = 1,
                     save.p = 0, save.N = 0)
```

## **Arguments**

counts A vector indicating the count (or abundance) for each observation.

observability A one-sided formula of the form  $\sim w_1 + ... + w_q$  with q terms specifying the

explicative variables for the observability process.

site A vector indicating the site identifier (from one to the total number of sites) for

each observation. Several observations can occur at one site. A site can be a

raster cell for example.

data.observability

A data frame containing the model's variables for the observability process.

suitability A one-sided formula of the form  $\sim x_1 + ... + x_p$  with p terms specifying the

explicative variables for the suitability process.

data.suitability

A data frame containing the model's variables for the suitability process.

suitability.pred

An optional data frame in which to look for variables with which to predict. If

NULL, the observations are used.

burnin The number of burnin iterations for the sampler.

mcmc The number of Gibbs iterations for the sampler. Total number of Gibbs iterations

is equal to burnin+mcmc. burnin+mcmc must be divisible by 10 and superior or

equal to 100 so that the progress bar can be displayed.

thin The thinning interval used in the simulation. The number of mcmc iterations

must be divisible by this value.

beta. start Starting values for  $\beta$  parameters of the suitability process. This can either be a

scalar or a p-length vector.

gamma.start Starting values for  $\beta$  parameters of the observability process. This can either be

a scalar or a q-length vector.

mubeta Means of the priors for the  $\beta$  parameters of the suitability process. mubeta must

be either a scalar or a p-length vector. If mubeta takes a scalar value, then that value will serve as the prior mean for all of the betas. The default value is set to

0 for an uninformative prior.

Vbeta Variances of the Normal priors for the  $\beta$  parameters of the suitability process.

Vbeta must be either a scalar or a p-length vector. If Vbeta takes a scalar value, then that value will serve as the prior variance for all of the betas. The default

variance is large and set to 1.0E6 for an uninformative flat prior.

mugamma Means of the Normal priors for the  $\gamma$  parameters of the observability process.

mugamma must be either a scalar or a p-length vector. If mugamma takes a scalar value, then that value will serve as the prior mean for all of the gammas. The

default value is set to 0 for an uninformative prior.

Vgamma Variances of the Normal priors for the  $\gamma$  parameters of the observability process.

Vgamma must be either a scalar or a p-length vector. If Vgamma takes a scalar value, then that value will serve as the prior variance for all of the gammas. The

default variance is large and set to 1.0E6 for an uninformative flat prior.

seed The seed for the random number generator. Default set to 1234.

A switch (0,1) which determines whether or not the progress of the sampler is printed to the screen. Default is 1: a progress bar is printed, indicating the step (in %) reached by the Gibbs sampler.

Save.p

A switch (0,1) which determines whether or not the sampled values for predictions are saved. Default is 0: the posterior mean is computed and returned in the lambda.pred vector. Be careful, setting save.p to 1 might require a large amount of memory.

Save.N

A switch (0,1) which determines whether or not the sampled values for the latent count variable N for each observed cells are saved. Default is 0: the mean

## **Details**

The model integrates two processes, an ecological process associated to the abundance of the species due to habitat suitability and an observation process that takes into account the fact that the probability of detection of the species is inferior to one.

(rounded to the closest integer) is computed and returned in the N. pred vector. Be careful, setting save. N to 1 might require a large amount of memory.

# **Ecological process:**

$$N_i \sim \mathcal{P}oisson(\lambda_i)$$
  
 $log(\lambda_i) = X_i\beta$ 

# **Observation process:**

$$y_{it} \sim \mathcal{B}inomial(N_i, \delta_{it})$$
  
 $logit(\delta_{it}) = W_{it}\gamma$ 

#### Value

mcmc An meme object that contains the posterior sample. This object can be summarized by functions provided by the coda package. The posterior sample of the deviance D, with  $D = -2 \log(\prod_{it} P(y_{it}, N_i|...))$ , is also provided. lambda.pred If save.p is set to 0 (default), lambda.pred is the predictive posterior mean of the abundance associated to the suitability process for each prediction. If save.p is set to 1, lambda.pred is an mcmc object with sampled values of the abundance associated to the suitability process for each prediction. If save. N is set to 0 (default), N. pred is the posterior mean (rounded to the N.pred closest integer) of the latent count variable N for each observed cell. If save.N is set to 1, N. pred is an mcmc object with sampled values of the latent count variable N for each observed cell. lambda.latent Predictive posterior mean of the abundance associated to the suitability process for each observation. delta.latent Predictive posterior mean of the probability associated to the observability pro-

#### Author(s)

Ghislain Vieilledent <ghislain.vieilledent@cirad.fr>

cess for each observation.

## References

Gelfand, A. E.; Schmidt, A. M.; Wu, S.; Silander, J. A.; Latimer, A. and Rebelo, A. G. (2005) Modelling species diversity through species level hierarchical modelling. *Applied Statistics*, 54, 1-20

Latimer, A. M.; Wu, S. S.; Gelfand, A. E. and Silander, J. A. (2006) Building statistical models to analyze species distributions. *Ecological Applications*, 16, 33-50.

Royle, J. A. (2004) N-mixture models for estimating population size from spatially replicated counts. *Biometrics*, 60, 108-115.

## See Also

```
plot.mcmc, summary.mcmc
```

## **Examples**

```
## Not run:
# hSDM.Nmixture()
# Example with simulated data
#=========
#== Load libraries
library(hSDM)
#========
#== Data simulation
# Number of observation sites
nsite <- 200
#= Set seed for repeatability
seed <- 4321
#= Ecological process (suitability)
set.seed(seed)
x1 <- rnorm(nsite, 0, 1)
set.seed(2*seed)
x2 <- rnorm(nsite, 0, 1)
X <- cbind(rep(1,nsite),x1,x2)</pre>
beta.target <- c(-1,1,-1) # Target parameters
log.lambda <- X %*% beta.target</pre>
lambda <- exp(log.lambda)</pre>
set.seed(seed)
N <- rpois(nsite,lambda)</pre>
#= Number of visits associated to each observation point
set.seed(seed)
visits <- rpois(nsite,3)</pre>
```

```
visits[visits==0] <- 1</pre>
# Vector of observation points
sites <- vector()</pre>
for (i in 1:nsite) {
    sites <- c(sites,rep(i,visits[i]))</pre>
#= Observation process (detectability)
nobs <- sum(visits)</pre>
set.seed(seed)
w1 <- rnorm(nobs,0,1)
set.seed(2*seed)
w2 <- rnorm(nobs,0,1)</pre>
W <- cbind(rep(1,nobs),w1,w2)</pre>
gamma.target <- c(-1,1,-1) # Target parameters
logit.delta <- W %*% gamma.target</pre>
delta <- inv.logit(logit.delta)</pre>
set.seed(seed)
Y <- rbinom(nobs,N[sites],delta)</pre>
#= Data-sets
data.obs <- data.frame(Y,w1,w2,site=sites)</pre>
data.suit <- data.frame(x1,x2)</pre>
#== Parameter inference with hSDM
Start <- Sys.time() # Start the clock</pre>
mod.hSDM.Nmixture <- hSDM.Nmixture(# Observations</pre>
                            counts=data.obs$Y,
                            observability=~w1+w2,
                            site=data.obs$site,
                            data.observability=data.obs,
                            # Habitat
                            suitability=~x1+x2,
                            data.suitability=data.suit,
                            # Predictions
                            suitability.pred=NULL,
                            # Chains
                            burnin=5000, mcmc=5000, thin=5,
                            # Starting values
                            beta.start=0,
                            gamma.start=0,
                            # Priors
                            mubeta=0, Vbeta=1.0E6,
                            mugamma=0, Vgamma=1.0E6,
                            # Various
                            seed=1234, verbose=1,
                            save.p=0, save.N=1)
Time.hSDM <- difftime(Sys.time(),Start,units="sec") # Time difference</pre>
#= Computation time
Time.hSDM
```

```
#=======
#== Outputs
#= Parameter estimates
summary(mod.hSDM.Nmixture$mcmc)
pdf(file="Posteriors_hSDM.Nmixture.pdf")
plot(mod.hSDM.Nmixture$mcmc)
dev.off()
#= Predictions
summary(mod.hSDM.Nmixture$lambda.latent)
summary(mod.hSDM.Nmixture$delta.latent)
summary(mod.hSDM.Nmixture$lambda.pred)
pdf(file="Pred-Init.pdf")
plot(lambda,mod.hSDM.Nmixture$lambda.pred)
abline(a=0,b=1,col="red")
dev.off()
\#= MCMC for latent variable N
pdf(file="MCMC_N.pdf")
plot(mod.hSDM.Nmixture$N.pred)
dev.off()
#= Check that Ns are correctly estimated
M <- as.matrix(mod.hSDM.Nmixture$N.pred)</pre>
N.est <- apply(M,2,mean)</pre>
Y.by.site <- tapply(data.obs$Y,data.obs$site,mean) # Mean by site
pdf(file="Check_N.pdf",width=10,height=5)
par(mfrow=c(1,2))
plot(Y.by.site, N.est) ## More individuals are expected (N > Y) due to detection process
abline(a=0,b=1,col="red")
plot(N, N.est) ## N are well estimated
abline(a=0,b=1,col="red")
cor(N, N.est) ## Very close to 1
dev.off()
## End(Not run)
```

hSDM.Nmixture.iCAR

N-mixture model with CAR process

# Description

The hSDM.Nmixture.iCAR function can be used to model species distribution including different processes in a hierarchical Bayesian framework: a  $\mathcal{P}oisson$  suitability process (refering to environmental suitability explaining abundance) which takes into account the spatial dependence of the

observations, and a *Binomial* observability process (refering to various ecological and methodological issues explaining the species detection). The hSDM. Nmixture. iCAR function calls a Gibbs sampler written in C code which uses an adaptive Metropolis algorithm to estimate the conditional posterior distribution of hierarchical model's parameters.

## Usage

```
hSDM.Nmixture.iCAR(# Observations
                     counts, observability, site, data.observability,
                     # Habitat
                     suitability, data.suitability,
                     # Spatial structure
                     spatial.entity,
                     n.neighbors, neighbors,
                     # Predictions
                     suitability.pred = NULL, spatial.entity.pred = NULL,
                     # Chains
                     burnin = 5000, mcmc = 10000, thin = 10,
                     # Starting values
                     beta.start,
                     gamma.start,
                     Vrho.start,
                     # Priors
                     mubeta = 0, Vbeta = 1.0E6,
                     mugamma = 0, Vgamma = 1.0E6,
                     priorVrho = "1/Gamma"
                     shape = 0.5, rate = 0.0005,
                     Vrho.max = 1000.
                     # Various
                     seed = 1234, verbose = 1,
                     save.rho = 0, save.p = 0, save.N = 0)
```

# **Arguments**

counts A vector indicating the count (or abundance) for each observation.

observability A one-sided formula of the form  $\sim w_1 + ... + w_q$  with q terms specifying the explicative variables for the observability process.

A vector indicating the site identifier (from one to the total number of sites) for each observation. Several observations can occur at one site. A site can be a raster cell for example.

data.observability

A data frame containing the model's variables for the observability process.

suitability A one-sided formula of the form  $\sim x_1 + ... + x_p$  with p terms specifying the explicative variables for the suitability process.

data.suitability

A data frame containing the model's variables for the suitability process. The number of rows of the data frame should be equal to the total number of spatial entities.

spatial.entity A vector (of length 'nsite') indicating the spatial entity identifier for each site.

Values must be between 1 and the total number of spatial entities. Several sites can be found in one spatial entity. A spatial entity can be a raster cell for exam-

ple.

n.neighbors A vector of integers that indicates the number of neighbors (adjacent entities) of

 $each \ spatial \ entity. \ length (\verb"n.neighbors") \ indicates \ the \ total \ number \ of \ spatial$ 

entities.

neighbors A vector of integers indicating the neighbors (adjacent entities) of each spatial

entity. Must be of the form c(neighbors of entity 1, neighbors of entity 2, ..., neighbors of the last entity). Length of the neighbors vector should be equal to

sum(n.neighbors).

suitability.pred

An optional data frame in which to look for variables with which to predict. If NULL, the data frame data.suitability for observations is used.

spatial.entity.pred

An optional vector indicating the spatial entity identifier (from one to the total number of entities) for predictions. If NULL, the vector spatial.entity for

observations is used.

burnin The number of burnin iterations for the sampler.

mcmc The number of Gibbs iterations for the sampler. Total number of Gibbs iterations

is equal to burnin+mcmc. burnin+mcmc must be divisible by 10 and superior or

equal to 100 so that the progress bar can be displayed.

thin The thinning interval used in the simulation. The number of mcmc iterations

must be divisible by this value.

beta. start Starting values for  $\beta$  parameters of the suitability process. This can either be a

scalar or a p-length vector.

gamma.start Starting values for  $\beta$  parameters of the observability process. This can either be

a scalar or a q-length vector.

Vrho. start Positive scalar indicating the starting value for the variance of the spatial random

effects

mubeta Means of the priors for the  $\beta$  parameters of the suitability process. mubeta must

be either a scalar or a p-length vector. If mubeta takes a scalar value, then that value will serve as the prior mean for all of the betas. The default value is set to

0 for an uninformative prior.

Vbeta Variances of the Normal priors for the  $\beta$  parameters of the suitability process.

Vbeta must be either a scalar or a p-length vector. If Vbeta takes a scalar value, then that value will serve as the prior variance for all of the betas. The default

variance is large and set to 1.0E6 for an uninformative flat prior.

mugamma Means of the Normal priors for the  $\gamma$  parameters of the observability process.

mugamma must be either a scalar or a p-length vector. If mugamma takes a scalar value, then that value will serve as the prior mean for all of the gammas. The

default value is set to 0 for an uninformative prior.

Vgamma Variances of the Normal priors for the  $\gamma$  parameters of the observability process.

Vgamma must be either a scalar or a p-length vector. If Vgamma takes a scalar value, then that value will serve as the prior variance for all of the gammas. The

default variance is large and set to 1.0E6 for an uninformative flat prior.

priorVrho	Type of prior for the variance of the spatial random effects. Can be set to a fixed positive scalar, or to an inverse-gamma distribution ("1/Gamma") with parameters shape and rate, or to a uniform distribution ("Uniform") on the interval [0,Vrho.max]. Default set to "1/Gamma".
shape	The shape parameter for the Gamma prior on the precision of the spatial random effects. Default value is shape=0.05 for uninformative prior.
rate	The rate (1/scale) parameter for the Gamma prior on the precision of the spatial random effects. Default value is rate=0.0005 for uninformative prior.
Vrho.max	Upper bound for the uniform prior of the spatial random effect variance. Default set to 1000.
seed	The seed for the random number generator. Default set to 1234.
verbose	A switch $(0,1)$ which determines whether or not the progress of the sampler is printed to the screen. Default is 1: a progress bar is printed, indicating the step (in $\%$ ) reached by the Gibbs sampler.
save.rho	A switch (0,1) which determines whether or not the sampled values for rhos are saved. Default is 0: the posterior mean is computed and returned in the rho.pred vector. Be careful, setting save.rho to 1 might require a large amount of memory.
save.p	A switch $(0,1)$ which determines whether or not the sampled values for predictions are saved. Default is 0: the posterior mean is computed and returned in the lambda.pred vector. Be careful, setting save.p to 1 might require a large amount of memory.
save.N	A switch $(0,1)$ which determines whether or not the sampled values for the latent count variable N for each observed cells are saved. Default is 0: the mean (rounded to the closest integer) is computed and returned in the N. pred vector. Be careful, setting save. N to 1 might require a large amount of memory.

# Details

The model integrates two processes, an ecological process associated to the abundance of the species due to habitat suitability and an observation process that takes into account the fact that the probability of detection of the species is inferior to one. The ecological process includes an intrinsic conditional autoregressive model (iCAR) model for spatial autocorrelation between observations, assuming that the abundance of the species at one site depends on the abundance of the species on neighboring sites.

# **Ecological process:**

$$N_i \sim \mathcal{P}oisson(\lambda_i)$$
  
 $log(\lambda_i) = X_i\beta + \rho_i$ 

 $\rho_i$ : spatial random effect

# **Spatial autocorrelation:**

An intrinsic conditional autoregressive model (iCAR) is assumed:

$$\rho_i \sim \mathcal{N}ormal(\mu_i, V_{\rho}/n_i)$$

 $\mu_i$ : mean of  $\rho_{i'}$  in the neighborhood of i.

 $V_{\rho}$ : variance of the spatial random effects.

 $n_i$ : number of neighbors for spatial entity i.

# **Observation process:**

$$y_{it} \sim \mathcal{B}inomial(N_i, \delta_{it})$$
  
 $logit(\delta_{it}) = W_{it}\gamma$ 

#### Value

mcmc

lambda.pred

rized by functions provided by the coda package. The posterior sample of the deviance D, with  $D=-2\log(\prod_{it}P(y_{it},N_i|...))$ , is also provided. If save.rho is set to 0 (default), rho.pred is the predictive posterior mean of the spatial random effect associated to each spatial entity. If save.rho is set to 1, rho.pred is an mcmc object with sampled values for each spatial random effect associated to each spatial entity.

If save.p is set to 0 (default), lambda.pred is the predictive posterior mean of the abundance associated to the suitability process for each prediction. If save.p is set to 1, lambda.pred is an mcmc object with sampled values of the

An meme object that contains the posterior sample. This object can be summa-

abundance associated to the suitability process for each prediction.

N. pred If save. N is set to 0 (default), N. pred is the posterior mean (rounded to the

closest integer) of the latent count variable N for each observed cell. If save.N is set to 1, N. pred is an mcmc object with sampled values of the latent count

variable N for each observed cell.

lambda.latent Predictive posterior mean of the abundance associated to the suitability process

for each observation.

delta.latent Predictive posterior mean of the probability associated to the observability pro-

cess for each observation.

#### Author(s)

Ghislain Vieilledent <ghislain.vieilledent@cirad.fr>

# References

Gelfand, A. E.; Schmidt, A. M.; Wu, S.; Silander, J. A.; Latimer, A. and Rebelo, A. G. (2005) Modelling species diversity through species level hierarchical modelling. *Applied Statistics*, 54, 1-20.

Latimer, A. M.; Wu, S. S.; Gelfand, A. E. and Silander, J. A. (2006) Building statistical models to analyze species distributions. *Ecological Applications*, 16, 33-50.

Royle, J. A. (2004) N-mixture models for estimating population size from spatially replicated counts, *Biometrics*, 60, 108-115.

#### See Also

plot.mcmc, summary.mcmc

## **Examples**

```
## Not run:
# hSDM.Nmixture.iCAR()
# Example with simulated data
#=========
#== Load libraries
library(hSDM)
library(raster)
library(sp)
#== Multivariate normal distribution
rmvn <- function(n, mu = 0, V = matrix(1), seed=1234) {
   p <- length(mu)</pre>
    if (any(is.na(match(dim(V), p)))) {
        stop("Dimension problem!")
   D <- chol(V)
    set.seed(seed)
    \texttt{t}(\texttt{matrix}(\texttt{rnorm}(\texttt{n*p}),\texttt{ncol=p})\%*\%\texttt{D+rep}(\texttt{mu},\texttt{rep}(\texttt{n},\texttt{p})))
}
#========
#== Data simulation
#= Set seed for repeatability
seed <- 4321
#= Landscape
xLand <- 20
yLand <- 20
Landscape <- raster(ncol=xLand,nrow=yLand,crs='+proj=utm +zone=1')</pre>
Landscape[] <- 0
extent(Landscape) <- c(0,xLand,0,yLand)</pre>
coords <- coordinates(Landscape)</pre>
ncells <- ncell(Landscape)</pre>
#= Neighbors
neighbors.mat <- adjacent(Landscape, cells=c(1:ncells), directions=8, pairs=TRUE, sorted=TRUE)</pre>
n.neighbors <- as.data.frame(table(as.factor(neighbors.mat[,1])))[,2]</pre>
adj <- neighbors.mat[,2]</pre>
#= Generate symmetric adjacency matrix, A
A <- matrix(0,ncells,ncells)
index.start <- 1</pre>
for (i in 1:ncells) {
```

```
index.end <- index.start+n.neighbors[i]-1</pre>
    A[i,adj[c(index.start:index.end)]] <- 1
    index.start <- index.end+1</pre>
}
#= Spatial effects
Vrho.target <- 5</pre>
d <- 1 # Spatial dependence parameter = 1 for intrinsic CAR
Q \leftarrow diag(n.neighbors)-d*A + diag(.0001,ncells) # Add small constant to make Q non-singular
covrho <- Vrho.target*solve(Q) # Covariance of rhos</pre>
set.seed(seed)
rho <- c(rmvn(1,mu=rep(0,ncells),V=covrho,seed=seed)) # Spatial Random Effects</pre>
rho <- rho-mean(rho) # Centering rhos on zero</pre>
#= Raster and plot spatial effects
r.rho <- rasterFromXYZ(cbind(coords,rho))</pre>
plot(r.rho)
#= Sample the observation sites in the landscape
nsite <- 150
set.seed(seed)
x.coord <- runif(nsite,0,xLand)</pre>
set.seed(2*seed)
y.coord <- runif(nsite,0,yLand)</pre>
sites.sp <- SpatialPoints(coords=cbind(x.coord,y.coord))</pre>
cells <- extract(Landscape, sites.sp, cell=TRUE)[,1]</pre>
#= Ecological process (suitability)
set.seed(seed)
x1 <- rnorm(nsite,0,1)</pre>
set.seed(2*seed)
x2 <- rnorm(nsite,0,1)</pre>
X <- cbind(rep(1,nsite),x1,x2)</pre>
beta.target <- c(-1,1,-1)
log.lambda <- X %*% beta.target + rho[cells]</pre>
lambda <- exp(log.lambda)</pre>
set.seed(seed)
N <- rpois(nsite,lambda)</pre>
#= Relative importance of spatial random effects
RImp <- mean(abs(rho[cells])/abs(X %*% beta.target))</pre>
RImp
#= Number of visits associated to each observation point
set.seed(seed)
visits <- rpois(nsite,3)</pre>
visits[visits==0] <- 1</pre>
# Vector of observation points
sites <- vector()</pre>
for (i in 1:nsite) {
    sites <- c(sites,rep(i,visits[i]))</pre>
```

```
#= Observation process (detectability)
nobs <- sum(visits)</pre>
set.seed(seed)
w1 <- rnorm(nobs,0,1)
set.seed(2*seed)
w2 <- rnorm(nobs,0,1)</pre>
W <- cbind(rep(1,nobs),w1,w2)</pre>
gamma.target < c(-1,1,-1)
logit.delta <- W %*% gamma.target</pre>
delta <- inv.logit(logit.delta)</pre>
set.seed(seed)
Y <- rbinom(nobs,N[sites],delta)</pre>
#= Data-sets
data.obs <- data.frame(Y,w1,w2,site=sites)</pre>
data.suit <- data.frame(x1,x2,cell=cells)</pre>
#== Parameter inference with hSDM
Start <- Sys.time() # Start the clock</pre>
mod.hSDM.Nmixture.iCAR <- hSDM.Nmixture.iCAR(# Observations</pre>
                            counts=data.obs$Y,
                            observability=~w1+w2,
                            site=data.obs$site,
                            data.observability=data.obs,
                            # Habitat
                            suitability=~x1+x2, data.suitability=data.suit,
                            # Spatial structure
                            spatial.entity=data.suit$cell,
                            n.neighbors=n.neighbors, neighbors=adj,
                            # Predictions
                            suitability.pred=NULL,
                            spatial.entity.pred=NULL,
                            # Chains
                            burnin=5000, mcmc=5000, thin=5,
                            # Starting values
                            beta.start=0,
                            gamma.start=0,
                            Vrho.start=1,
                            # Priors
                            mubeta=0, Vbeta=1.0E6,
                            mugamma=0, Vgamma=1.0E6,
                            priorVrho="1/Gamma",
                            shape=0.5, rate=0.005,
                            Vrho.max=10,
                            # Various
                            seed=1234, verbose=1,
                            save.rho=1, save.p=0, save.N=1)
Time.hSDM <- difftime(Sys.time(),Start,units="sec") # Time difference</pre>
#= Computation time
Time.hSDM
```

```
#=======
#== Outputs
#= Parameter estimates
summary(mod.hSDM.Nmixture.iCAR$mcmc)
pdf(file="Posteriors_hSDM.Nmixture.iCAR.pdf")
plot(mod.hSDM.Nmixture.iCAR$mcmc)
dev.off()
#= Predictions
summary(mod.hSDM.Nmixture.iCAR$lambda.latent)
summary(mod.hSDM.Nmixture.iCAR$delta.latent)
summary(mod.hSDM.Nmixture.iCAR$lambda.pred)
pdf(file="Pred-Init.pdf")
plot(lambda,mod.hSDM.Nmixture.iCAR$lambda.pred)
abline(a=0,b=1,col="red")
dev.off()
\#= MCMC for latent variable N
pdf(file="MCMC_N.pdf")
plot(mod.hSDM.Nmixture.iCAR$N.pred)
dev.off()
#= Check that Ns are corretly estimated
M <- as.matrix(mod.hSDM.Nmixture.iCAR$N.pred)</pre>
N.est <- apply(M,2,mean)</pre>
Y.by.site <- tapply(data.obs$Y,data.obs$site,mean) # Mean by site
pdf(file="Check_N.pdf",width=10,height=5)
par(mfrow=c(1,2))
plot(Y.by.site, N.est) ## More individuals are expected (N > Y) due to detection process
abline(a=0,b=1,col="red")
plot(N, N.est) ## N are well estimated
abline(a=0,b=1,col="red")
cor(N, N.est) ## Very close to 1
dev.off()
#= Summary plots for spatial random effects
# rho.pred
rho.pred <- apply(mod.hSDM.Nmixture.iCAR$rho.pred,2,mean)</pre>
r.rho.pred <- rasterFromXYZ(cbind(coords,rho.pred))</pre>
# plot
pdf(file="Summary_hSDM.Nmixture.iCAR.pdf")
par(mfrow=c(2,2))
# rho target
plot(r.rho, main="rho target")
plot(sites.sp,add=TRUE)
# rho estimated
plot(r.rho.pred, main="rho estimated")
# correlation and "shrinkage"
Levels.cells <- sort(unique(cells))</pre>
```

hSDM.Nmixture.K

N-mixture model with K, the maximal theoretical abundance

# Description

The hSDM.Nmixture.K function can be used to model species distribution including different processes in a hierarchical Bayesian framework: a  $\mathcal{P}oisson$  suitability process (refering to environmental suitability explaining abundance) and a  $\mathcal{B}inomial$  observability process (refering to various ecological and methodological issues explaining species detection). The hSDM.Nmixture.K function calls a Gibbs sampler written in C code which uses an adaptive Metropolis algorithm to estimate the conditional posterior distribution of hierarchical model's parameters. K is the maximal theoretical abundance sensus Royle 2004.

## Usage

```
hSDM.Nmixture.K(# Observations
                        counts, observability, site, data.observability,
                        # Habitat
                        suitability, data.suitability,
                        # Predictions
                        suitability.pred = NULL,
                        # Chains
                        burnin = 5000, mcmc = 10000, thin = 10,
                        # Starting values
                        beta.start,
                        gamma.start,
                        # Priors
                        mubeta = 0, Vbeta = 1.0E6,
                        mugamma = 0, Vgamma = 1.0E6,
                        # Various
                       Κ,
                        seed = 1234, verbose = 1,
                        save.p = 0)
```

#### **Arguments**

counts A vector indicating the count (or abundance) for each observation.

observability A one-sided formula of the form  $\sim w_1 + ... + w_q$  with q terms specifying the

explicative variables for the observability process.

site A vector indicating the site identifier (from one to the total number of sites) for

each observation. Several observations can occur at one site. A site can be a

raster cell for example.

data.observability

A data frame containing the model's variables for the observability process.

suitability A one-sided formula of the form  $\sim x_1 + ... + x_p$  with p terms specifying the

explicative variables for the suitability process.

data.suitabilitv

A data frame containing the model's variables for the suitability process.

suitability.pred

An optional data frame in which to look for variables with which to predict. If

NULL, the observations are used.

burnin The number of burnin iterations for the sampler.

mcmc The number of Gibbs iterations for the sampler. Total number of Gibbs iterations

is equal to burnin+mcmc. burnin+mcmc must be divisible by 10 and superior or

equal to 100 so that the progress bar can be displayed.

thin The thinning interval used in the simulation. The number of mcmc iterations

must be divisible by this value.

beta. start Starting values for  $\beta$  parameters of the suitability process. This can either be a

scalar or a p-length vector.

gamma.start Starting values for  $\beta$  parameters of the observability process. This can either be

a scalar or a q-length vector.

mubeta Means of the priors for the  $\beta$  parameters of the suitability process. mubeta must

be either a scalar or a p-length vector. If mubeta takes a scalar value, then that value will serve as the prior mean for all of the betas. The default value is set to

0 for an uninformative prior.

Vbeta Variances of the Normal priors for the  $\beta$  parameters of the suitability process.

Vbeta must be either a scalar or a p-length vector. If Vbeta takes a scalar value, then that value will serve as the prior variance for all of the betas. The default

variance is large and set to 1.0E6 for an uninformative flat prior.

mugamma Means of the Normal priors for the  $\gamma$  parameters of the observability process.

mugamma must be either a scalar or a p-length vector. If mugamma takes a scalar value, then that value will serve as the prior mean for all of the gammas. The

default value is set to 0 for an uninformative prior.

Vgamma Variances of the Normal priors for the  $\gamma$  parameters of the observability process.

Vgamma must be either a scalar or a p-length vector. If Vgamma takes a scalar value, then that value will serve as the prior variance for all of the gammas. The

default variance is large and set to 1.0E6 for an uninformative flat prior.

K Maximal theoretical abundance sensus Royle 2004. It corresponds to the integer upper index of integration for N-mixture. This should be set high enough so that it does not affect the parameter estimates. Note that computation time will increase with K.

seed The seed for the random number generator. Default set to 1234.

verbose A switch (0,1) which determines whether or not the progress of the sampler is

printed to the screen. Default is 1: a progress bar is printed, indicating the step

(in %) reached by the Gibbs sampler.

save. p A switch (0,1) which determines whether or not the sampled values for predic-

tions are saved. Default is 0: the posterior mean is computed and returned in the lambda.pred vector. Be careful, setting save.p to 1 might require a large

amount of memory.

#### **Details**

The model integrates two processes, an ecological process associated to the abundance of the species due to habitat suitability and an observation process that takes into account the fact that the probability of detection of the species is inferior to one.

# **Ecological process:**

$$N_i \sim \mathcal{P}oisson(\lambda_i)$$

$$log(\lambda_i) = X_i \beta$$

# **Observation process:**

$$y_{it} \sim \mathcal{B}inomial(N_i, \delta_{it})$$

$$logit(\delta_{it}) = W_{it}\gamma$$

# Value

mcmc An mcmc object that contains the posterior sample. This object can be summa-

rized by functions provided by the coda package. The posterior sample of the

deviance D, with  $D = -2 \log(\prod_{i,t} P(y_{i,t}, N_i|...))$ , is also provided.

lambda.pred If save.p is set to 0 (default), lambda.pred is the predictive posterior mean

of the abundance associated to the suitability process for each prediction. If save.p is set to 1, lambda.pred is an mcmc object with sampled values of the

abundance associated to the suitability process for each prediction.

lambda.latent Predictive posterior mean of the abundance associated to the suitability process

for each observation.

delta.latent Predictive posterior mean of the probability associated to the observability pro-

cess for each observation.

# Author(s)

Ghislain Vieilledent <ghislain.vieilledent@cirad.fr>

## References

Gelfand, A. E.; Schmidt, A. M.; Wu, S.; Silander, J. A.; Latimer, A. and Rebelo, A. G. (2005) Modelling species diversity through species level hierarchical modelling. *Applied Statistics*, 54, 1-20

Latimer, A. M.; Wu, S. S.; Gelfand, A. E. and Silander, J. A. (2006) Building statistical models to analyze species distributions. *Ecological Applications*, 16, 33-50.

Royle, J. A. (2004) N-mixture models for estimating population size from spatially replicated counts. *Biometrics*, 60, 108-115.

## See Also

```
plot.mcmc, summary.mcmc
```

## **Examples**

```
## Not run:
# hSDM.Nmixture.K()
# Example with simulated data
#=========
#== Load libraries
library(hSDM)
#========
#== Data simulation
# Number of observation sites
nsite <- 200
#= Set seed for repeatability
seed <- 4321
#= Ecological process (suitability)
set.seed(seed)
x1 <- rnorm(nsite, 0, 1)
set.seed(2*seed)
x2 <- rnorm(nsite, 0, 1)
X <- cbind(rep(1,nsite),x1,x2)</pre>
beta.target <- c(-1,1,-1) # Target parameters
log.lambda <- X %*% beta.target</pre>
lambda <- exp(log.lambda)</pre>
set.seed(seed)
N <- rpois(nsite,lambda)</pre>
#= Number of visits associated to each observation point
set.seed(seed)
visits <- rpois(nsite,3)</pre>
```

```
visits[visits==0] <- 1</pre>
# Vector of observation points
sites <- vector()</pre>
for (i in 1:nsite) {
    sites <- c(sites,rep(i,visits[i]))</pre>
#= Observation process (detectability)
nobs <- sum(visits)</pre>
set.seed(seed)
w1 <- rnorm(nobs,0,1)
set.seed(2*seed)
w2 <- rnorm(nobs,0,1)</pre>
W <- cbind(rep(1,nobs),w1,w2)</pre>
gamma.target <- c(-1,1,-1) # Target parameters
logit.delta <- W %*% gamma.target</pre>
delta <- inv.logit(logit.delta)</pre>
set.seed(seed)
Y <- rbinom(nobs,N[sites],delta)</pre>
#= Data-sets
data.obs <- data.frame(Y,w1,w2,site=sites)</pre>
data.suit <- data.frame(x1,x2)</pre>
#== Parameter inference with hSDM
Start <- Sys.time() # Start the clock</pre>
mod.hSDM.Nmixture.K <- hSDM.Nmixture.K(# Observations</pre>
                            counts=data.obs$Y,
                            observability=~w1+w2,
                            site=data.obs$site,
                            data.observability=data.obs,
                            # Habitat
                            suitability=~x1+x2,
                            data.suitability=data.suit,
                            # Predictions
                            suitability.pred=NULL,
                            # Chains
                            burnin=5000, mcmc=5000, thin=5,
                            # Starting values
                            beta.start=0,
                            gamma.start=0,
                            # Priors
                            mubeta=0, Vbeta=1.0E6,
                            mugamma=0, Vgamma=1.0E6,
                            # Various
                            K=max(data.obs$Y)*2,
                            seed=1234, verbose=1,
                            save.p=0)
Time.hSDM <- difftime(Sys.time(),Start,units="sec") # Time difference</pre>
#= Computation time
```

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```
Time.hSDM
#== Outputs
#= Parameter estimates
summary(mod.hSDM.Nmixture.K$mcmc)
pdf(file="Posteriors_hSDM.Nmixture.K.pdf")
plot(mod.hSDM.Nmixture.K$mcmc)
dev.off()
#= Predictions
summary(mod.hSDM.Nmixture.K$lambda.latent)
summary(mod.hSDM.Nmixture.K$delta.latent)
summary(mod.hSDM.Nmixture.K$lambda.pred)
pdf(file="Pred-Init.K.pdf")
plot(lambda,mod.hSDM.Nmixture.K$lambda.pred)
abline(a=0,b=1,col="red")
dev.off()
## End(Not run)
```

hSDM.poisson

Poisson log regression model

#### **Description**

The hSDM.poisson function performs a Poisson log regression in a Bayesian framework. The function calls a Gibbs sampler written in C code which uses an adaptive Metropolis algorithm to estimate the conditional posterior distribution of model's parameters.

# Usage

```
hSDM.poisson(counts, suitability, data, suitability.pred = NULL,
burnin = 5000, mcmc = 10000, thin = 10, beta.start, mubeta = 0, Vbeta =
1e+06, seed = 1234, verbose = 1, save.p = 0)
```

#### **Arguments**

counts A vector indicating the count (or abundance) for each observation.

suitability A one-sided formula of the form '~x1+...+xp' with p terms specifying the ex-

plicative covariates for the suitability process of the model.

data A data frame containing the model's explicative variables.

suitability.pred

An optional data frame in which to look for variables with which to predict. If NULL, the observations are used.

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burnin The number of burnin iterations for the sampler.

mcmc The number of Gibbs iterations for the sampler. Total number of Gibbs iterations

is equal to burnin+mcmc. burnin+mcmc must be divisible by 10 and superior or

equal to 100 so that the progress bar can be displayed.

thin The thinning interval used in the simulation. The number of meme iterations

must be divisible by this value.

beta. start Starting values for beta parameters of the suitability process. If beta. start

takes a scalar value, then that value will serve for all of the betas.

mubeta Means of the priors for the  $\beta$  parameters of the suitability process. mubeta must

be either a scalar or a p-length vector. If mubeta takes a scalar value, then that value will serve as the prior mean for all of the betas. The default value is set to

0 for an uninformative prior.

Vbeta Variances of the Normal priors for the  $\beta$  parameters of the suitability process.

Vbeta must be either a scalar or a p-length vector. If Vbeta takes a scalar value, then that value will serve as the prior variance for all of the betas. The default

variance is large and set to 1.0E6 for an uninformative flat prior.

seed The seed for the random number generator. Default to 1234.

verbose A switch (0,1) which determines whether or not the progress of the sampler is

printed to the screen. Default is 1: a progress bar is printed, indicating the step

(in %) reached by the Gibbs sampler.

save.p A switch (0,1) which determines whether or not the sampled values for predic-

tions are saved. Default is 0: the posterior mean is computed and returned in the lambda.pred vector. Be careful, setting save.p to 1 might require a large

amount of memory.

### **Details**

We model the abundance of the species as a function of environmental variables.

## **Ecological process:**

$$y_i \sim Poisson(\lambda_i)$$

$$log(\lambda_i) = X_i \beta$$

#### Value

mcmc An mcmc object that contains the posterior sample. This object can be summa-

rized by functions provided by the coda package. The posterior sample of the

deviance D, with  $D = -2 \log(\prod_i P(y_i, n_i | \beta))$ , is also provided.

lambda.pred If save.p is set to 0 (default), lambda.pred is the predictive posterior mean

of the abundance associated to the suitability process for each prediction. If save.p is set to 1, lambda.pred is an mcmc object with sampled values of the

abundance associated to the suitability process for each prediction.

lambda.latent Predictive posterior mean of the abundance associated to the suitability process

for each observation.

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### Author(s)

Ghislain Vieilledent <ghislain.vieilledent@cirad.fr>

#### References

Latimer, A. M.; Wu, S. S.; Gelfand, A. E. and Silander, J. A. (2006) Building statistical models to analyze species distributions. *Ecological Applications*, 16, 33-50.

Gelfand, A. E.; Schmidt, A. M.; Wu, S.; Silander, J. A.; Latimer, A. and Rebelo, A. G. (2005) Modelling species diversity through species level hierarchical modelling. *Applied Statistics*, 54, 1-20.

#### See Also

```
plot.mcmc, summary.mcmc
```

### **Examples**

```
## Not run:
# hSDM.poisson()
# Example with simulated data
#========
#== Load libraries
library(hSDM)
#========
#== Data simulation
#= Number of sites
nsite <- 200
#= Set seed for repeatability
seed <- 1234
#= Ecological process (suitability)
set.seed(seed)
x1 <- rnorm(nsite,0,1)</pre>
set.seed(2*seed)
x2 <- rnorm(nsite, 0, 1)
X <- cbind(rep(1,nsite),x1,x2)</pre>
beta.target <- c(-1,1,-1)
log.lambda <- X %*% beta.target</pre>
lambda <- exp(log.lambda)</pre>
set.seed(seed)
Y <- rpois(nsite,lambda)</pre>
#= Data-sets
```

```
data.obs <- data.frame(Y,x1,x2)</pre>
#== Site-occupancy model
mod.hSDM.poisson <- hSDM.poisson(counts=data.obs$Y,</pre>
                                  suitability=~x1+x2,
                                  data=data.obs,
                                  suitability.pred=NULL,
                                  burnin=1000, mcmc=1000, thin=1,
                                  beta.start=0,
                                  mubeta=0, Vbeta=1.0E6,
                                  seed=1234, verbose=1,
                                  save.p=0)
#== Outputs
#= Parameter estimates
summary(mod.hSDM.poisson$mcmc)
pdf(file="Posteriors_hSDM.poisson.pdf")
plot(mod.hSDM.poisson$mcmc)
dev.off()
#== glm resolution to compare
mod.glm <- glm(Y~x1+x2,family="poisson",data=data.obs)</pre>
summary(mod.glm)
#= Predictions
summary(mod.hSDM.poisson$lambda.latent)
summary(mod.hSDM.poisson$lambda.pred)
pdf(file="Pred-Init.pdf")
plot(lambda, mod. hSDM.poisson$lambda.pred)
abline(a=0,b=1,col="red")
dev.off()
## End(Not run)
```

hSDM.poisson.iCAR

Poisson log regression model with CAR process

# **Description**

The hSDM.poisson.iCAR function performs a Poisson log regression in a hierarchical Bayesian framework. The suitability process includes a spatial correlation process. The spatial correlation is modelled using an intrinsic CAR model. The hSDM.poisson.iCAR function calls a Gibbs sampler written in C code which uses an adaptive Metropolis algorithm to estimate the conditional posterior distribution of hierarchical model's parameters.

# Usage

```
hSDM.poisson.iCAR(counts, suitability, spatial.entity, data, n.neighbors, neighbors, suitability.pred=NULL, spatial.entity.pred=NULL, burnin = 5000, mcmc = 10000, thin = 10, beta.start, Vrho.start, mubeta = 0, Vbeta = 1e+06, priorVrho = "1/Gamma", shape = 0.5, rate = 0.0005, Vrho.max=1000, seed = 1234, verbose = 1, save.rho = 0, save.p = 0)
```

### **Arguments**

counts A vector indicating the count (or abundance) for each observation.

suitability A one-sided formula of the form  $\sim x_1 + ... + x_p$  with p terms specifying the

explicative variables for the suitability process.

spatial.entity A vector indicating the spatial entity identifier (from one to the total number

of entities) for each observation. Several observations can occur in one spatial

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entity. A spatial entity can be a raster cell for example.

data A data frame containing the model's variables.

n.neighbors A vector of integers that indicates the number of neighbors (adjacent entities) of

each spatial entity. length(n.neighbors) indicates the total number of spatial

entities.

neighbors A vector of integers indicating the neighbors (adjacent entities) of each spatial

entity. Must be of the form c(neighbors of entity 1, neighbors of entity 2, ..., neighbors of the last entity). Length of the neighbors vector should be equal to

sum(n.neighbors).

suitability.pred

An optional data frame in which to look for variables with which to predict. If

NULL, the observations are used.

spatial.entity.pred

An optional vector indicating the spatial entity identifier (from one to the total number of entities) for predictions. If NULL, the vector spatial.entity for

observations is used.

burnin The number of burnin iterations for the sampler.

mcmc The number of Gibbs iterations for the sampler. Total number of Gibbs iterations

is equal to burnin+mcmc. burnin+mcmc must be divisible by 10 and superior or

equal to 100 so that the progress bar can be displayed.

thin The thinning interval used in the simulation. The number of mcmc iterations

must be divisible by this value.

beta. start Starting values for  $\beta$  parameters of the suitability process. This can either be a

scalar or a p-length vector.

Vrho. start Positive scalar indicating the starting value for the variance of the spatial random

effects.

mubeta Means of the priors for the  $\beta$  parameters of the suitability process. mubeta must

be either a scalar or a p-length vector. If mubeta takes a scalar value, then that value will serve as the prior mean for all of the betas. The default value is set to

0 for an uninformative prior.

Vbeta	Variances of the Normal priors for the $\beta$ parameters of the suitability process. Vbeta must be either a scalar or a p-length vector. If Vbeta takes a scalar value, then that value will serve as the prior variance for all of the betas. The default variance is large and set to 1.0E6 for an uninformative flat prior.
priorVrho	Type of prior for the variance of the spatial random effects. Can be set to a fixed positive scalar, or to an inverse-gamma distribution ("1/Gamma") with parameters shape and rate, or to a uniform distribution ("Uniform") on the interval [0,Vrho.max]. Default set to "1/Gamma".
shape	The shape parameter for the Gamma prior on the precision of the spatial random effects. Default value is shape=0.05 for uninformative prior.
rate	The rate (1/scale) parameter for the Gamma prior on the precision of the spatial random effects. Default value is rate=0.0005 for uninformative prior.
Vrho.max	Upper bound for the uniform prior of the spatial random effect variance. Default set to 1000.
seed	The seed for the random number generator. Default set to 1234.
verbose	A switch (0,1) which determines whether or not the progress of the sampler is printed to the screen. Default is 1: a progress bar is printed, indicating the step (in %) reached by the Gibbs sampler.
save.rho	A switch (0,1) which determines whether or not the sampled values for rhos are saved. Default is 0: the posterior mean is computed and returned in the rho.pred vector. Be careful, setting save.rho to 1 might require a large amount of memory.
save.p	A switch $(0,1)$ which determines whether or not the sampled values for predictions are saved. Default is 0: the posterior mean is computed and returned in the lambda.pred vector. Be careful, setting save.p to 1 might require a large amount of memory.

#### **Details**

We model an ecological process where the abundance of the species is explained by habitat suitability. The ecological process includes an intrinsic conditional autoregressive (iCAR) model for spatial autocorrelation between observations, assuming that the probability of presence of the species at one site depends on the probability of presence of the species on neighboring sites.

## **Ecological process:**

$$y_i \sim \mathcal{P}oisson(\lambda_i, t_i)$$
  
 $log(\lambda_i) = X_i\beta + \rho_{j(i)}$ 

 $\rho_i$ : spatial random effect

j(i): index of the spatial entity for observation i.

# **Spatial autocorrelation:**

An intrinsic conditional autoregressive model (iCAR) is assumed:

$$\rho_j \sim \mathcal{N}ormal(\mu_j, V_\rho/n_j)$$

 $\mu_j$ : mean of  $\rho_{j'}$  in the neighborhood of j.

 $V_{\rho}$ : variance of the spatial random effects.

 $n_i$ : number of neighbors for spatial entity j.

### Value

mcmc An mcmc object that contains the posterior sample. This object can be summa-

rized by functions provided by the coda package. The posterior sample of the

deviance D, with  $D = -2 \log(\prod_i P(y_i|...))$ , is also provided.

rho.pred If save.rho is set to 0 (default), rho.pred is the predictive posterior mean of

the spatial random effect associated to each spatial entity. If save.rho is set to 1, rho.pred is an mcmc object with sampled values for each spatial random

effect associated to each spatial entity.

lambda.pred If save.p is set to 0 (default), lambda.pred is the predictive posterior mean

of the abundance associated to the suitability process for each prediction. If save.p is set to 1, lambda.pred is an mcmc object with sampled values of the

abundance associated to the suitability process for each prediction.

lambda.latent Predictive posterior mean of the abundance associated to the suitability process

for each observation.

#### Author(s)

Ghislain Vieilledent <ghislain.vieilledent@cirad.fr>

#### References

Gelfand, A. E.; Schmidt, A. M.; Wu, S.; Silander, J. A.; Latimer, A. and Rebelo, A. G. (2005) Modelling species diversity through species level hierarchical modelling. *Applied Statistics*, 54, 1-20.

Latimer, A. M.; Wu, S. S.; Gelfand, A. E. and Silander, J. A. (2006) Building statistical models to analyze species distributions. *Ecological Applications*, 16, 33-50.

Lichstein, J. W.; Simons, T. R.; Shriner, S. A. & Franzreb, K. E. (2002) Spatial autocorrelation and autoregressive models in ecology *Ecological Monographs*, 72, 445-463.

Diez, J. M. & Pulliam, H. R. (2007) Hierarchical analysis of species distributions and abundance across environmental gradients *Ecology*, 88, 3144-3152.

#### See Also

```
plot.mcmc, summary.mcmc
```

## **Examples**

```
library(raster)
library(sp)
#== Multivariate normal distribution
rmvn \leftarrow function(n, mu = 0, V = matrix(1), seed=1234) {
   p <- length(mu)</pre>
   if (any(is.na(match(dim(V), p)))) {
       stop("Dimension problem!")
    }
   D <- chol(V)
   set.seed(seed)
    t(matrix(rnorm(n*p),ncol=p)%*%D+rep(mu,rep(n,p)))
}
#========
#== Data simulation
#= Set seed for repeatability
seed <- 1234
#= Landscape
xLand <- 30
yLand <- 30
Landscape <- raster(ncol=xLand,nrow=yLand,crs='+proj=utm +zone=1')</pre>
Landscape[] <- 0
extent(Landscape) <- c(0,xLand,0,yLand)</pre>
coords <- coordinates(Landscape)</pre>
ncells <- ncell(Landscape)</pre>
#= Neighbors
neighbors.mat <- adjacent(Landscape, cells=c(1:ncells), directions=8, pairs=TRUE, sorted=TRUE)</pre>
n.neighbors <- as.data.frame(table(as.factor(neighbors.mat[,1])))[,2]</pre>
adj <- neighbors.mat[,2]</pre>
#= Generate symmetric adjacency matrix, A
A <- matrix(0,ncells,ncells)
index.start <- 1</pre>
for (i in 1:ncells) {
    index.end <- index.start+n.neighbors[i]-1</pre>
   A[i,adj[c(index.start:index.end)]] <- 1
    index.start <- index.end+1</pre>
}
#= Spatial effects
Vrho.target <- 5</pre>
d <- 1 # Spatial dependence parameter = 1 for intrinsic CAR
Q <- diag(n.neighbors)-d*A + diag(.0001,ncells) # Add small constant to make Q non-singular
covrho <- Vrho.target*solve(Q) # Covariance of rhos</pre>
set.seed(seed)
rho <- rho-mean(rho) # Centering rhos on zero</pre>
```

```
#= Raster and plot spatial effects
r.rho <- rasterFromXYZ(cbind(coords,rho))</pre>
plot(r.rho)
#= Sample the observation sites in the landscape
nsite <- 250
set.seed(seed)
x.coord <- runif(nsite,0,xLand)</pre>
set.seed(2*seed)
y.coord <- runif(nsite,0,yLand)</pre>
sites.sp <- SpatialPoints(coords=cbind(x.coord,y.coord))</pre>
cells <- extract(Landscape, sites.sp, cell=TRUE)[,1]</pre>
#= Ecological process (suitability)
set.seed(seed)
x1 <- rnorm(nsite,0,1)</pre>
set.seed(2*seed)
x2 <- rnorm(nsite, 0, 1)
X <- cbind(rep(1,nsite),x1,x2)</pre>
beta.target <- c(-1,1,-1)
log.lambda <- X %*% beta.target + rho[cells]</pre>
lambda <- exp(log.lambda)</pre>
set.seed(seed)
Y <- rpois(nsite,lambda)</pre>
#= Relative importance of spatial random effects
RImp <- mean(abs(rho[cells])/abs(X %*% beta.target))</pre>
RImp
#= Data-sets
data.obs <- data.frame(Y,x1,x2,cell=cells)</pre>
#== Site-occupancy model
Start <- Sys.time() # Start the clock</pre>
mod.hSDM.poisson.iCAR <- hSDM.poisson.iCAR(counts=data.obs$Y,</pre>
                                             suitability=~x1+x2,
                                             spatial.entity=data.obs$cell,
                                             data=data.obs,
                                             n.neighbors=n.neighbors,
                                             neighbors=adj,
                                             suitability.pred=NULL,
                                             spatial.entity.pred=NULL,
                                             burnin=5000, mcmc=5000, thin=5,
                                             beta.start=0,
                                             Vrho.start=1,
                                             mubeta=0, Vbeta=1.0E6,
                                             priorVrho="1/Gamma",
                                             shape=0.5, rate=0.0005,
                                             seed=1234, verbose=1,
                                             save.rho=1, save.p=0)
Time.hSDM <- difftime(Sys.time(),Start,units="sec") # Time difference</pre>
```

```
#= Computation time
Time.hSDM
#=======
#== Outputs
#= Parameter estimates
summary(mod.hSDM.poisson.iCAR$mcmc)
pdf("Posteriors_hSDM.poisson.iCAR.pdf")
plot(mod.hSDM.poisson.iCAR$mcmc)
dev.off()
#= Predictions
summary(mod.hSDM.poisson.iCAR$lambda.latent)
summary(mod.hSDM.poisson.iCAR$lambda.pred)
pdf(file="Pred-Init.pdf")
plot(lambda,mod.hSDM.poisson.iCAR$lambda.pred)
abline(a=0,b=1,col="red")
dev.off()
#= Summary plots for spatial random effects
# rho.pred
rho.pred <- apply(mod.hSDM.poisson.iCAR$rho.pred,2,mean)</pre>
r.rho.pred <- rasterFromXYZ(cbind(coords,rho.pred))</pre>
# plot
pdf(file="Summary_hSDM.poisson.iCAR.pdf")
par(mfrow=c(2,2))
# rho target
plot(r.rho, main="rho target")
plot(sites.sp,add=TRUE)
# rho estimated
plot(r.rho.pred, main="rho estimated")
# correlation and "shrinkage"
Levels.cells <- sort(unique(cells))</pre>
plot(rho[-Levels.cells], rho.pred[-Levels.cells],
     xlim=range(rho),
     ylim=range(rho),
     xlab="rho target",
     ylab="rho estimated")
points(rho[Levels.cells],rho.pred[Levels.cells],pch=16,col="blue")
legend(x=-3,y=4,legend="Visited cells",col="blue",pch=16,bty="n")
abline(a=0,b=1,col="red")
dev.off()
## End(Not run)
```

hSDM.siteocc

Site occupancy model

## **Description**

The hSDM.siteocc function can be used to model species distribution including different processes in a hierarchical Bayesian framework: a *Bernoulli* suitability process (refering to environmental suitability) and a *Bernoulli* observability process (refering to various ecological and methodological issues explaining the species detection). The hSDM.siteocc function calls a Gibbs sampler written in C code which uses a Metropolis algorithm to estimate the conditional posterior distribution of hierarchical model's parameters.

## Usage

```
hSDM.siteocc(# Observations
                     presence, observability, site, data.observability,
                     # Habitat
                     suitability, data.suitability,
                     # Predictions
                     suitability.pred = NULL,
                     # Chains
                     burnin = 1000, mcmc = 1000, thin = 1,
                     # Starting values
                     beta.start,
                     gamma.start,
                     # Priors
                     mubeta = 0, Vbeta = 1.0E6,
                     mugamma = 0, Vgamma = 1.0E6,
                     # Various
                     seed = 1234, verbose = 1,
                     save.p = 0)
```

## **Arguments**

presence A vector indicating the presence/absence for each observation.

observability A one-sided formula of the form  $\sim w_1 + ... + w_q$  with q terms specifying the

explicative variables for the observability process.

A vector indicating the site identifier (from one to the total number of sites) for

each observation. Several observations can occur at one site. A site can be a

raster cell for example.

data.observability

A data frame containing the model's variables for the observability process.

suitability A one-sided formula of the form  $\sim x_1 + ... + x_p$  with p terms specifying the

explicative variables for the suitability process.

data.suitability

A data frame containing the model's variables for the suitability process.

suitability.pred

An optional data frame in which to look for variables with which to predict. If

NULL, the observations are used.

burnin The number of burnin iterations for the sampler.

The number of Gibbs iterations for the sampler. Total number of Gibbs iterations mcmc

is equal to burnin+mcmc. burnin+mcmc must be divisible by 10 and superior or

equal to 100 so that the progress bar can be displayed.

thin The thinning interval used in the simulation. The number of mcmc iterations

must be divisible by this value.

beta.start Starting values for  $\beta$  parameters of the suitability process. This can either be a

scalar or a p-length vector.

gamma.start Starting values for  $\beta$  parameters of the observability process. This can either be

a scalar or a q-length vector.

mubeta Means of the priors for the  $\beta$  parameters of the suitability process. mubeta must

> be either a scalar or a p-length vector. If mubeta takes a scalar value, then that value will serve as the prior mean for all of the betas. The default value is set to

0 for an uninformative prior.

Vbeta Variances of the Normal priors for the  $\beta$  parameters of the suitability process.

> Vbeta must be either a scalar or a p-length vector. If Vbeta takes a scalar value, then that value will serve as the prior variance for all of the betas. The default

variance is large and set to 1.0E6 for an uninformative flat prior.

mugamma Means of the Normal priors for the  $\gamma$  parameters of the observability process.

> mugamma must be either a scalar or a p-length vector. If mugamma takes a scalar value, then that value will serve as the prior mean for all of the gammas. The

default value is set to 0 for an uninformative prior.

Vgamma Variances of the Normal priors for the  $\gamma$  parameters of the observability process.

> Vgamma must be either a scalar or a p-length vector. If Vgamma takes a scalar value, then that value will serve as the prior variance for all of the gammas. The

default variance is large and set to 1.0E6 for an uninformative flat prior.

seed The seed for the random number generator. Default set to 1234.

verbose A switch (0,1) which determines whether or not the progress of the sampler is

printed to the screen. Default is 1: a progress bar is printed, indicating the step

(in %) reached by the Gibbs sampler.

A switch (0,1) which determines whether or not the sampled values for predicsave.p

> tions are saved. Default is 0: the posterior mean is computed and returned in the lambda.pred vector. Be careful, setting save.p to 1 might require a large

amount of memory.

# **Details**

The model integrates two processes, an ecological process associated to the presence or absence of the species due to habitat suitability and an observation process that takes into account the fact that the probability of detection of the species is inferior to one.

### **Ecological process:**

 $z_i \sim \mathcal{B}ernoulli(\theta_i)$ 

$$logit(\theta_i) = X_i\beta$$

## **Observation process:**

$$y_{it} \sim \mathcal{B}ernoulli(z_i * \delta_{it})$$
  
 $logit(\delta_{it}) = W_{it}\gamma$ 

#### Value

An meme object that contains the posterior sample. This object can be summarized by functions provided by the coda package. The posterior sample of the deviance D, with  $D = -2\log(\prod_{it}P(y_{it},N_i|...))$ , is also provided. If save pisset to 0 (default), theta pred is the predictive posterior mean of the probability associated to the suitability process for each prediction. If save p is set to 1, theta pred is an meme object with sampled values of the probability associated to the suitability process for each prediction. Predictive posterior mean of the probability associated to the suitability process for each site. Predictive posterior mean of the probability associated to the observability process for each site.

cess for each observation.

### Author(s)

Ghislain Vieilledent <ghislain.vieilledent@cirad.fr>

#### References

MacKenzie, D. I.; Nichols, J. D.; Lachman, G. B.; Droege, S.; Andrew Royle, J. and Langtimm, C. A. (2002) Estimating site occupancy rates when detection probabilities are less than one. *Ecology*, 83, 2248-2255.

## See Also

plot.mcmc, summary.mcmc

### **Examples**

```
#= Number of observation sites
nsite <- 200
#= Set seed for repeatability
seed <- 4321
#= Ecological process (suitability)
set.seed(seed)
x1 <- rnorm(nsite,0,1)</pre>
set.seed(2*seed)
x2 <- rnorm(nsite,0,1)</pre>
X <- cbind(rep(1,nsite),x1,x2)</pre>
beta.target <- c(-1,1,-1) # Target parameters
logit.theta <- X %*% beta.target</pre>
theta <- inv.logit(logit.theta)</pre>
set.seed(seed)
Z <- rbinom(nsite,1,theta)</pre>
#= Number of visits associated to each observation point
set.seed(seed)
visits <- rpois(nsite,3)</pre>
visits[visits==0] <- 1</pre>
# Vector of observation points
sites <- vector()</pre>
for (i in 1:nsite) {
    sites <- c(sites,rep(i,visits[i]))</pre>
}
#= Observation process (detectability)
nobs <- sum(visits)</pre>
set.seed(seed)
w1 <- rnorm(nobs,0,1)
set.seed(2*seed)
w2 <- rnorm(nobs,0,1)</pre>
W <- cbind(rep(1,nobs),w1,w2)</pre>
gamma.target <- c(-1,1,-1) # Target parameters
logit.delta <- W %*% gamma.target</pre>
delta <- inv.logit(logit.delta)</pre>
set.seed(seed)
Y <- rbinom(nobs,1,delta*Z[sites])</pre>
#= Data-sets
data.obs <- data.frame(Y,w1,w2,site=sites)</pre>
data.suit <- data.frame(x1,x2)</pre>
#== Parameter inference with hSDM
Start <- Sys.time() # Start the clock</pre>
mod.hSDM.siteocc <- hSDM.siteocc(# Observations</pre>
                                  presence=data.obs$Y,
```

```
observability=~w1+w2,
                                 site=data.obs$site,
                                 data.observability=data.obs,
                                 # Habitat
                                 suitability=~x1+x2,
                                 data.suitability=data.suit,
                                 # Predictions
                                 suitability.pred=NULL,
                                 # Chains
                                 burnin=2000, mcmc=2000, thin=2,
                                 # Starting values
                                 beta.start=0,
                                 gamma.start=0,
                                 # Priors
                                 mubeta=0, Vbeta=1.0E6,
                                 mugamma=0, Vgamma=1.0E6,
                                 # Various
                                 seed=1234, verbose=1, save.p=0)
Time.hSDM <- difftime(Sys.time(),Start,units="sec") # Time difference</pre>
#= Computation time
Time.hSDM
#======
#== Outputs
#= Parameter estimates
summary(mod.hSDM.siteocc$mcmc)
pdf(file="Posteriors_hSDM.siteocc.pdf")
plot(mod.hSDM.siteocc$mcmc)
dev.off()
#= Predictions
summary(mod.hSDM.siteocc$theta.latent)
summary(mod.hSDM.siteocc$delta.latent)
summary(mod.hSDM.siteocc$theta.pred)
pdf(file="Pred-Init.pdf")
plot(theta,mod.hSDM.siteocc$theta.pred)
abline(a=0,b=1,col="red")
dev.off()
## End(Not run)
```

### **Description**

The hSDM.siteocc.iCAR function can be used to model species distribution including different processes in a hierarchical Bayesian framework: a *Bernoulli* suitability process (refering to environmental suitability) which takes into account the spatial dependence of the observations, and a *Bernoulli* observability process (refering to various ecological and methodological issues explaining the species detection). The hSDM.siteocc.iCAR function calls a Gibbs sampler written in C code which uses an adaptive Metropolis algorithm to estimate the conditional posterior distribution of hierarchical model's parameters.

### Usage

```
hSDM.siteocc.iCAR(# Observations
                          presence, observability, site, data.observability,
                          # Habitat
                          suitability, data.suitability,
                          # Spatial structure
                          spatial.entity,
                          n.neighbors, neighbors,
                          # Predictions
                          suitability.pred = NULL, spatial.entity.pred = NULL,
                          # Chains
                         burnin = 1000, mcmc = 1000, thin = 1,
                          # Starting values
                         beta.start,
                          gamma.start,
                          Vrho.start,
                          # Priors
                         mubeta = 0, Vbeta = 1.0E6,
                         mugamma = 0, Vgamma = 1.0E6,
                         priorVrho = "1/Gamma",
                          shape = 0.5, rate = 0.0005,
                          Vrho.max = 1000,
                          # Various
                          seed = 1234, verbose = 1,
                          save.rho = 0, save.p = 0)
```

### **Arguments**

presence A vector indicating the presence/absence for each observation.

observability A one-sided formula of the form  $\sim w_1 + ... + w_q$  with q terms specifying the

explicative variables for the observability process.

site A vector indicating the site identifier (from one to the total number of sites) for

each observation. Several observations can occur at one site. A site can be a

raster cell for example.

data.observability

A data frame containing the model's variables for the observability process.

suitability A one-sided formula of the form  $\sim x_1 + ... + x_p$  with p terms specifying the

explicative variables for the suitability process.

data.suitability

A data frame containing the model's variables for the suitability process.

spatial.entity A vector (of length 'nsite') indicating the spatial entity identifier for each site.

Values must be between 1 and the total number of spatial entities. Several sites can be found in one spatial entity. A spatial entity can be a raster cell for exam-

ple.

n.neighbors A vector of integers that indicates the number of neighbors (adjacent entities) of

each spatial entity. length(n.neighbors) indicates the total number of spatial

entities.

neighbors A vector of integers indicating the neighbors (adjacent entities) of each spatial

entity. Must be of the form c(neighbors of entity 1, neighbors of entity 2, ..., neighbors of the last entity). Length of the neighbors vector should be equal to

sum(n.neighbors).

suitability.pred

An optional data frame in which to look for variables with which to predict. If

NULL, the observations are used.

spatial.entity.pred

An optional vector indicating the spatial entity identifier (from one to the total

number of entities) for predictions. If NULL, the vector spatial.entity for

observations is used.

burnin The number of burnin iterations for the sampler.

mcmc The number of Gibbs iterations for the sampler. Total number of Gibbs iterations

is equal to burnin+mcmc. burnin+mcmc must be divisible by 10 and superior or

equal to 100 so that the progress bar can be displayed.

thin The thinning interval used in the simulation. The number of mcmc iterations

must be divisible by this value.

beta. start Starting values for  $\beta$  parameters of the suitability process. This can either be a

scalar or a p-length vector.

gamma.start Starting values for  $\beta$  parameters of the observability process. This can either be

a scalar or a q-length vector.

Vrho. start Positive scalar indicating the starting value for the variance of the spatial random

effects.

mubeta Means of the priors for the  $\beta$  parameters of the suitability process. mubeta must

be either a scalar or a p-length vector. If mubeta takes a scalar value, then that value will serve as the prior mean for all of the betas. The default value is set to

0 for an uninformative prior.

Vbeta Variances of the Normal priors for the  $\beta$  parameters of the suitability process.

Vbeta must be either a scalar or a p-length vector. If Vbeta takes a scalar value, then that value will serve as the prior variance for all of the betas. The default

variance is large and set to 1.0E6 for an uninformative flat prior.

mugamma Means of the Normal priors for the  $\gamma$  parameters of the observability process.

mugamma must be either a scalar or a p-length vector. If mugamma takes a scalar value, then that value will serve as the prior mean for all of the gammas. The

default value is set to 0 for an uninformative prior.

Vgamma	Variances of the Normal priors for the $\gamma$ parameters of the observability process. Vgamma must be either a scalar or a p-length vector. If Vgamma takes a scalar value, then that value will serve as the prior variance for all of the gammas. The default variance is large and set to 1.0E6 for an uninformative flat prior.
priorVrho	Type of prior for the variance of the spatial random effects. Can be set to a fixed positive scalar, or to an inverse-gamma distribution ("1/Gamma") with parameters shape and rate, or to a uniform distribution ("Uniform") on the interval [0,Vrho.max]. Default set to "1/Gamma".
shape	The shape parameter for the Gamma prior on the precision of the spatial random effects. Default value is shape=0.05 for uninformative prior.
rate	The rate (1/scale) parameter for the Gamma prior on the precision of the spatial random effects. Default value is rate=0.0005 for uninformative prior.
Vrho.max	Upper bound for the uniform prior of the spatial random effect variance. Default set to 1000.
seed	The seed for the random number generator. Default set to 1234.
verbose	A switch $(0,1)$ which determines whether or not the progress of the sampler is printed to the screen. Default is 1: a progress bar is printed, indicating the step (in %) reached by the Gibbs sampler.
save.rho	A switch (0,1) which determines whether or not the sampled values for rhos are saved. Default is 0: the posterior mean is computed and returned in the rho.pred vector. Be careful, setting save.rho to 1 might require a large amount of memory.
save.p	A switch $(0,1)$ which determines whether or not the sampled values for predictions are saved. Default is 0: the posterior mean is computed and returned in the theta.pred vector. Be careful, setting save.p to 1 might require a large amount of memory.

# **Details**

The model integrates two processes, an ecological process associated to the presence or absence of the species due to habitat suitability and an observation process that takes into account the fact that the probability of detection of the species is inferior to one. The ecological process includes an intrinsic conditional autoregressive model (iCAR) model for spatial autocorrelation between observations, assuming that the probability of presence of the species at one site depends on the probability of presence of the species on neighboring sites.

# **Ecological process:**

$$z_i \sim \mathcal{B}ernoulli(\theta_i)$$
  
 $logit(\theta_i) = X_i\beta + \rho_{j(i)}$ 

 $\rho_j$ : spatial random effect

j(i): index of the spatial entity for observation i.

# **Spatial autocorrelation:**

An intrinsic conditional autoregressive model (iCAR) is assumed:

$$\rho_i \sim \mathcal{N}ormal(\mu_i, V_{\rho}/n_i)$$

 $\mu_i$ : mean of  $\rho_{i'}$  in the neighborhood of j.

 $V_{\rho}$ : variance of the spatial random effects.

 $n_i$ : number of neighbors for spatial entity j.

### **Observation process:**

$$y_{it} \sim \mathcal{B}ernoulli(z_i * \delta_{it})$$
  
 $logit(\delta_{it}) = W_{it}\gamma$ 

#### Value

mcmc An mcmc object that contains the posterior sample. This object can be summa-

rized by functions provided by the coda package. The posterior sample of the

deviance D, with  $D = -2\log(\prod_i P(y_i, z_i|...))$ , is also provided.

rho.pred If save.rho is set to 0 (default), rho.pred is the predictive posterior mean of

the spatial random effect associated to each spatial entity. If save.rho is set to 1, rho.pred is an mcmc object with sampled values for each spatial random

effect associated to each spatial entity.

theta.pred If save.p is set to 0 (default), theta.pred is the predictive posterior mean of the

probability associated to the suitability process for each prediction. If save.p is set to 1, theta.pred is an mcmc object with sampled values of the probability

associated to the suitability process for each prediction.

theta.latent Predictive posterior mean of the probability associated to the suitability process

for each site.

delta.latent Predictive posterior mean of the probability associated to the observability pro-

cess for each observation.

#### Author(s)

Ghislain Vieilledent <ghislain.vieilledent@cirad.fr>

#### References

Diez, J. M. & Pulliam, H. R. (2007) Hierarchical analysis of species distributions and abundance across environmental gradients *Ecology*, 88, 3144-3152.

Gelfand, A. E.; Schmidt, A. M.; Wu, S.; Silander, J. A.; Latimer, A. and Rebelo, A. G. (2005) Modelling species diversity through species level hierarchical modelling. *Applied Statistics*, 54, 1-20.

Latimer, A. M.; Wu, S. S.; Gelfand, A. E. and Silander, J. A. (2006) Building statistical models to analyze species distributions. *Ecological Applications*, 16, 33-50.

Lichstein, J. W.; Simons, T. R.; Shriner, S. A. & Franzreb, K. E. (2002) Spatial autocorrelation and autoregressive models in ecology *Ecological Monographs*, 72, 445-463.

MacKenzie, D. I.; Nichols, J. D.; Lachman, G. B.; Droege, S.; Andrew Royle, J. and Langtimm, C. A. (2002) Estimating site occupancy rates when detection probabilities are less than one. *Ecology*, 83, 2248-2255.

### See Also

```
plot.mcmc, summary.mcmc
```

## **Examples**

```
## Not run:
# hSDM.siteocc.iCAR()
# Example with simulated data
#========
#== Load libraries
library(hSDM)
library(raster)
library(sp)
#== Multivariate normal distribution
rmvn <- function(n, mu = 0, V = matrix(1), seed=1234) {
   p <- length(mu)</pre>
   if (any(is.na(match(dim(V), p)))) {
       stop("Dimension problem!")
   D <- chol(V)
   set.seed(seed)
   t(matrix(rnorm(n*p),ncol=p)%*%D+rep(mu,rep(n,p)))
}
#=========
#== Data simulation
#= Set seed for repeatability
seed <- 1234
#= Landscape
xLand <- 30
yLand <- 30
Landscape <- raster(ncol=xLand,nrow=yLand,crs='+proj=utm +zone=1')</pre>
Landscape[] <- 0
extent(Landscape) <- c(0,xLand,0,yLand)</pre>
coords <- coordinates(Landscape)</pre>
ncells <- ncell(Landscape)</pre>
#= Neighbors
neighbors.mat <- adjacent(Landscape, cells=c(1:ncells), directions=8, pairs=TRUE, sorted=TRUE)</pre>
n.neighbors <- as.data.frame(table(as.factor(neighbors.mat[,1])))[,2]</pre>
adj <- neighbors.mat[,2]</pre>
#= Generate symmetric adjacency matrix, A
```

```
A <- matrix(0,ncells,ncells)
index.start <- 1</pre>
for (i in 1:ncells) {
    index.end <- index.start+n.neighbors[i]-1</pre>
    A[i,adj[c(index.start:index.end)]] <- 1
    index.start <- index.end+1</pre>
}
#= Spatial effects
Vrho.target <- 5</pre>
d <- 1 \# Spatial dependence parameter = 1 for intrinsic CAR
Q \leftarrow diag(n.neighbors)-d*A + diag(.0001,ncells) \# Add small constant to make <math>Q non-singular
covrho <- Vrho.target*solve(Q) # Covariance of rhos</pre>
set.seed(seed)
rho <- c(rmvn(1,mu=rep(0,ncells), V=covrho,seed=seed)) # Spatial Random Effects</pre>
rho <- rho-mean(rho) # Centering rhos on zero</pre>
#= Raster and plot spatial effects
r.rho <- rasterFromXYZ(cbind(coords,rho))</pre>
plot(r.rho)
#= Sample the observation sites in the landscape
nsite <- 250
set.seed(seed)
x.coord <- runif(nsite,0,xLand)</pre>
set.seed(2*seed)
y.coord <- runif(nsite,0,yLand)</pre>
sites.sp <- SpatialPoints(coords=cbind(x.coord,y.coord))</pre>
cells <- extract(Landscape, sites.sp, cell=TRUE)[,1]</pre>
#= Ecological process (suitability)
set.seed(seed)
x1 <- rnorm(nsite, 0, 1)
set.seed(2*seed)
x2 <- rnorm(nsite, 0, 1)
X <- cbind(rep(1,nsite),x1,x2)</pre>
beta.target <- c(-1,1,-1)
logit.theta <- X %*% beta.target + rho[cells]</pre>
theta <- inv.logit(logit.theta)</pre>
set.seed(seed)
Z <- rbinom(nsite,1,theta)</pre>
#= Relative importance of spatial random effects
RImp <- mean(abs(rho[cells])/abs(X %*% beta.target))</pre>
RImp
#= Number of visits associated to each observation point
set.seed(seed)
visits <- rpois(nsite,3)</pre>
visits[visits==0] <- 1</pre>
# Vector of observation points
sites <- vector()</pre>
for (i in 1:nsite) {
```

```
sites <- c(sites,rep(i,visits[i]))</pre>
}
#= Observation process (detectability)
nobs <- sum(visits)</pre>
set.seed(seed)
w1 <- rnorm(nobs,0,1)
set.seed(2*seed)
w2 <- rnorm(nobs,0,1)</pre>
W <- cbind(rep(1,nobs),w1,w2)</pre>
gamma.target <- c(-1,1,-1)
logit.delta <- W %*% gamma.target</pre>
delta <- inv.logit(logit.delta)</pre>
set.seed(seed)
Y <- rbinom(nobs,1,delta*Z[sites])</pre>
#= Data-sets
data.obs <- data.frame(Y,w1,w2,site=sites)</pre>
data.suit <- data.frame(x1,x2,cell=cells)</pre>
#== Parameter inference with hSDM
Start <- Sys.time() # Start the clock</pre>
mod.hSDM.siteocc.iCAR <- hSDM.siteocc.iCAR(# Observations</pre>
                                             presence=data.obs$Y,
                                             observability=~w1+w2,
                                             site=data.obs$site,
                                             data.observability=data.obs,
                                             # Habitat
                                           suitability=~x1+x2, data.suitability=data.suit,
                                             # Spatial structure
                                             spatial.entity=data.suit$cell,
                                             n.neighbors=n.neighbors, neighbors=adj,
                                             # Predictions
                                             suitability.pred=NULL,
                                             spatial.entity.pred=NULL,
                                             # Chains
                                             burnin=10000, mcmc=5000, thin=5,
                                             # Starting values
                                             beta.start=0,
                                             gamma.start=0,
                                             Vrho.start=1,
                                             # Priors
                                             mubeta=0, Vbeta=1.0E6,
                                             mugamma=0, Vgamma=1.0E6,
                                             priorVrho="Uniform",
                                             Vrho.max=10,
                                             # Various
                                             seed=1234, verbose=1,
                                             save.rho=1, save.p=0)
Time.hSDM <- difftime(Sys.time(),Start,units="sec") # Time difference</pre>
```

```
#= Computation time
Time.hSDM
#=======
#== Outputs
#= Parameter estimates
summary(mod.hSDM.siteocc.iCAR$mcmc)
pdf("Posteriors_hSDM.siteocc.iCAR.pdf")
plot(mod.hSDM.siteocc.iCAR$mcmc)
dev.off()
#= Predictions
summary(mod.hSDM.siteocc.iCAR$theta.latent)
summary(mod.hSDM.siteocc.iCAR$delta.latent)
summary(mod.hSDM.siteocc.iCAR$theta.pred)
pdf(file="Pred-Init.pdf")
plot(theta,mod.hSDM.siteocc.iCAR$theta.pred)
abline(a=0,b=1,col="red")
dev.off()
#= Summary plots for spatial random effects
# rho.pred
rho.pred <- apply(mod.hSDM.siteocc.iCAR$rho.pred,2,mean)</pre>
r.rho.pred <- rasterFromXYZ(cbind(coords,rho.pred))</pre>
pdf(file="Summary_hSDM.siteocc.iCAR.pdf")
par(mfrow=c(2,2))
# rho target
plot(r.rho, main="rho target")
plot(sites.sp,add=TRUE)
# rho estimated
plot(r.rho.pred, main="rho estimated")
# correlation and "shrinkage"
Levels.cells <- sort(unique(cells))</pre>
plot(rho[-Levels.cells], rho.pred[-Levels.cells],
     xlim=range(rho),
     ylim=range(rho),
     xlab="rho target",
     ylab="rho estimated")
points(rho[Levels.cells],rho.pred[Levels.cells],pch=16,col="blue")
legend(x=-3,y=4,legend="Visited cells",col="blue",pch=16,bty="n")
abline(a=0,b=1,col="red")
dev.off()
## End(Not run)
```

hSDM.ZIB

ZIB (Zero-Inflated Binomial) model

# Description

The hSDM.ZIB function can be used to model species distribution including different processes in a hierarchical Bayesian framework: a  $\mathcal{B}ernoulli$  suitability process (refering to environmental suitability) and a  $\mathcal{B}inomial$  observability process (refering to various ecological and methodological issues explaining the species detection). The hSDM.ZIB function calls a Gibbs sampler written in C code which uses a Metropolis algorithm to estimate the conditional posterior distribution of hierarchical model's parameters.

# Usage

```
hSDM.ZIB(presences, trials, suitability, observability, data, suitability.pred=NULL, burnin = 5000, mcmc = 10000, thin = 10, beta.start, gamma.start, mubeta = 0, Vbeta = 1e+06, mugamma = 0, Vgamma = 1e+06, seed = 1234, verbose = 1, save.p = 0)
```

### **Arguments**

presences

presences	To vector indicating the number of successes (of presences) for each observation.	
trials	A vector indicating the number of trials for each observation. $t_i$ should be superior to zero and superior or equal to $y_i$ , the number of successes for observation $i$ .	
suitability	A one-sided formula of the form $\sim x_1++x_p$ with $p$ terms specifying the explicative variables for the suitability process.	
observability	A one-sided formula of the form $\sim w_1++w_q$ with $q$ terms specifying the explicative variables for the observability process.	
data	A data frame containing the model's variables.	
suitability.pred		
	An optional data frame in which to look for variables with which to predict. If NULL, the observations are used.	
burnin	The number of burnin iterations for the sampler.	
mcmc	The number of Gibbs iterations for the sampler. Total number of Gibbs iterations is equal to burnin+mcmc. burnin+mcmc must be divisible by 10 and superior or equal to 100 so that the progress bar can be displayed.	
thin	The thinning interval used in the simulation. The number of mcmc iterations must be divisible by this value.	
beta.start	Starting values for $\beta$ parameters of the suitability process. This can either be a scalar or a $p\text{-length}$ vector.	
gamma.start	Starting values for $\beta$ parameters of the observability process. This can either be a scalar or a $q\text{-length}$ vector.	

A vector indicating the number of successes (or presences) for each observation.

mubeta Means of the priors for the  $\beta$  parameters of the suitability process. mubeta must be either a scalar or a p-length vector. If mubeta takes a scalar value, then that value will serve as the prior mean for all of the betas. The default value is set to 0 for an uninformative prior.

Variances of the Normal priors for the  $\beta$  parameters of the suitability process. Vbeta must be either a scalar or a p-length vector. If Vbeta takes a scalar value, then that value will serve as the prior variance for all of the betas. The default

variance is large and set to 1.0E6 for an uninformative flat prior.

Means of the Normal priors for the  $\gamma$  parameters of the observability process. mugamma must be either a scalar or a p-length vector. If mugamma takes a scalar

value, then that value will serve as the prior mean for all of the gammas. The

default value is set to 0 for an uninformative prior.

Vgamma Variances of the Normal priors for the  $\gamma$  parameters of the observability process.

Vgamma must be either a scalar or a p-length vector. If Vgamma takes a scalar value, then that value will serve as the prior variance for all of the gammas. The

default variance is large and set to 1.0E6 for an uninformative flat prior.

seed The seed for the random number generator. Default set to 1234.

verbose A switch (0,1) which determines whether or not the progress of the sampler is

printed to the screen. Default is 1: a progress bar is printed, indicating the step

(in %) reached by the Gibbs sampler.

save.p A switch (0,1) which determines whether or not the sampled values for predic-

tions are saved. Default is 0: the posterior mean is computed and returned in the prob.p.pred vector. Be careful, setting save.p to 1 might require a large

amount of memory.

## Details

Vbeta

mugamma

The model integrates two processes, an ecological process associated to the presence or absence of the species due to habitat suitability and an observation process that takes into account the fact that the probability of detection of the species is inferior to one.

## **Ecological process:**

$$z_i \sim \mathcal{B}ernoulli(\theta_i)$$
  
 $logit(\theta_i) = X_i\beta$ 

#### **Observation process:**

$$y_i \sim \mathcal{B}inomial(z_i * \delta_i, t_i)$$
  
 $logit(\delta_i) = W_i \gamma$ 

## Value

mcmc An mcmc object that contains the posterior sample. This object can be summa-

rized by functions provided by the coda package. The posterior sample of the

deviance D, with  $D = -2 \log(\prod_i P(y_i, z_i|...))$ , is also provided.

prob.p.pred If save.p is set to 0 (default), prob.p.pred is the predictive posterior mean

of the probability associated to the suitability process for each prediction. If save.p is set to 1, prob.p.pred is an mcmc object with sampled values of the

probability associated to the suitability process for each prediction.

prob.p.latent Predictive posterior mean of the probability associated to the suitability process for each observation.prob.q.latent Predictive posterior mean of the probability associated to the observability process for each observation.

### Author(s)

Ghislain Vieilledent <ghislain.vieilledent@cirad.fr>

### References

Gelfand, A. E.; Schmidt, A. M.; Wu, S.; Silander, J. A.; Latimer, A. and Rebelo, A. G. (2005) Modelling species diversity through species level hierarchical modelling. *Applied Statistics*, 54, 1-20.

Latimer, A. M.; Wu, S. S.; Gelfand, A. E. and Silander, J. A. (2006) Building statistical models to analyze species distributions. *Ecological Applications*, 16, 33-50.

MacKenzie, D. I.; Nichols, J. D.; Lachman, G. B.; Droege, S.; Andrew Royle, J. and Langtimm, C. A. (2002) Estimating site occupancy rates when detection probabilities are less than one. *Ecology*, 83, 2248-2255.

#### See Also

```
plot.mcmc, summary.mcmc
```

# **Examples**

```
## Not run:
# hSDM.ZIB()
# Example with simulated data
#=======
#== Preambule
library(hSDM)
#========
#== Data simulation
# Set seed for repeatability
seed <- 1234
# Number of observations
nobs <- 1000
# Target parameters
beta.target <- matrix(c(0.2, 0.5, 0.5), ncol=1)
gamma.target <- matrix(c(1),ncol=1)</pre>
```

```
## Uncomment if you want covariates on the observability process
## gamma.target <- matrix(c(0.2,0.5,0.5),ncol=1)
# Covariates for "suitability" process
set.seed(seed)
X1 <- rnorm(n=nobs,0,1)</pre>
set.seed(2*seed)
X2 <- rnorm(n=nobs,0,1)</pre>
X <- cbind(rep(1,nobs),X1,X2)</pre>
# Covariates for "observability" process
W <- cbind(rep(1,nobs))</pre>
## Uncomment if you want covariates on the observability process
## set.seed(3*seed)
## W1 <- rnorm(n=nobs,0,1)
## set.seed(4*seed)
## W2 <- rnorm(n=nobs,0,1)
## W <- cbind(rep(1,nobs),W1,W2)
#== Simulating latent variables
# Suitability
logit.theta.1 <- X %*% beta.target</pre>
theta.1 <- inv.logit(logit.theta.1)</pre>
set.seed(seed)
y.1 <- rbinom(nobs,1,theta.1)</pre>
# Observability
set.seed(seed)
trials <- rpois(nobs,5) # Number of trial associated to each observation</pre>
trials[trials==0] <- 1</pre>
logit.theta.2 <- W %*% gamma.target</pre>
theta.2 <- inv.logit(logit.theta.2)</pre>
set.seed(seed)
y.2 <- rbinom(nobs,trials,theta.2)</pre>
#== Simulating response variable
Y \leftarrow y.2*y.1
#== Data-set
Data <- data.frame(Y,trials,X1,X2)</pre>
## Uncomment if you want covariates on the observability process
## Data <- data.frame(Y,trials,X1,X2,W1,W2)</pre>
#== ZIB model
mod.hSDM.ZIB <- hSDM.ZIB(presences=Data$Y,</pre>
                          trials=Data$trials,
                          suitability=~X1+X2,
                          observability=~1, #=~1+W1+W2 if covariates
                          data=Data,
                          suitability.pred=NULL,
```

```
burnin=1000, mcmc=1000, thin=5,
                         beta.start=0,
                         gamma.start=0,
                         mubeta=0, Vbeta=1.0E6,
                         mugamma=0, Vgamma=1.0E6,
                         seed=1234, verbose=1,
                         save.p=0)
#=======
#== Outputs
pdf(file="Posteriors_hSDM.ZIB.pdf")
plot(mod.hSDM.ZIB$mcmc)
dev.off()
summary(mod.hSDM.ZIB$prob.p.latent)
summary(mod.hSDM.ZIB$prob.q.latent)
summary(mod.hSDM.ZIB$prob.p.pred)
## End(Not run)
```

hSDM.ZIB.iCAR

ZIB (Zero-Inflated Binomial) model with CAR process

### **Description**

The hSDM.ZIB.iCAR function can be used to model species distribution including different processes in a hierarchical Bayesian framework: a  $\mathcal{B}ernoulli$  suitability process (refering to environmental suitability) which takes into account the spatial dependence of the observations, and a  $\mathcal{B}inomial$  observability process (refering to various ecological and methodological issues explaining the species detection). The hSDM.ZIB.iCAR function calls a Gibbs sampler written in C code which uses an adaptive Metropolis algorithm to estimate the conditional posterior distribution of hierarchical model's parameters.

## Usage

```
hSDM.ZIB.iCAR(presences, trials, suitability, observability, spatial.entity, data, n.neighbors, neighbors, suitability.pred=NULL, spatial.entity.pred=NULL, burnin = 5000, mcmc = 10000, thin = 10, beta.start, gamma.start, Vrho.start, mubeta = 0, Vbeta = 1e+06, mugamma = 0, Vgamma = 1e+06, priorVrho = "1/Gamma", shape = 0.5, rate = 0.0005, Vrho.max=1000, seed = 1234, verbose = 1, save.rho = 0, save.p = 0)
```

# **Arguments**

presences

A vector indicating the number of successes (or presences) for each observation.

trials A vector indicating the number of trials for each observation.  $t_i$  should be superior to zero and superior or equal to  $y_i$ , the number of successes for observation

suitability A one-sided formula of the form  $\sim x_1 + ... + x_p$  with p terms specifying the explicative variables for the suitability process.

observability A one-sided formula of the form  $\sim w_1 + ... + w_q$  with q terms specifying the explicative variables for the observability process.

spatial.entity A vector indicating the spatial entity identifier (from one to the total number of entities) for each observation. Several observations can occur in one spatial entity. A spatial entity can be a raster cell for example.

A data frame containing the model's variables. data

n.neighbors A vector of integers that indicates the number of neighbors (adjacent entities) of each spatial entity. length(n.neighbors) indicates the total number of spatial entities.

> A vector of integers indicating the neighbors (adjacent entities) of each spatial entity. Must be of the form c(neighbors of entity 1, neighbors of entity 2, ..., neighbors of the last entity). Length of the neighbors vector should be equal to sum(n.neighbors).

suitability.pred

An optional data frame in which to look for variables with which to predict. If NULL, the observations are used.

spatial.entity.pred

An optional vector indicating the spatial entity identifier (from one to the total number of entities) for predictions. If NULL, the vector spatial.entity for observations is used.

burnin The number of burnin iterations for the sampler.

mcmc The number of Gibbs iterations for the sampler. Total number of Gibbs iterations is equal to burnin+mcmc. burnin+mcmc must be divisible by 10 and superior or equal to 100 so that the progress bar can be displayed.

The thinning interval used in the simulation. The number of mcmc iterations thin must be divisible by this value.

beta.start Starting values for  $\beta$  parameters of the suitability process. This can either be a scalar or a p-length vector.

gamma.start Starting values for  $\beta$  parameters of the observability process. This can either be a scalar or a q-length vector.

> Positive scalar indicating the starting value for the variance of the spatial random effects.

Means of the priors for the  $\beta$  parameters of the suitability process. mubeta must be either a scalar or a p-length vector. If mubeta takes a scalar value, then that value will serve as the prior mean for all of the betas. The default value is set to 0 for an uninformative prior.

Variances of the Normal priors for the  $\beta$  parameters of the suitability process. Vbeta must be either a scalar or a p-length vector. If Vbeta takes a scalar value, then that value will serve as the prior variance for all of the betas. The default variance is large and set to 1.0E6 for an uninformative flat prior.

neighbors

Vrho.start

mubeta

Vbeta

Means of the Normal priors for the $\gamma$ parameters of the observability process. mugamma must be either a scalar or a p-length vector. If mugamma takes a scalar value, then that value will serve as the prior mean for all of the gammas. The default value is set to 0 for an uninformative prior.
Variances of the Normal priors for the $\gamma$ parameters of the observability process. Vgamma must be either a scalar or a p-length vector. If Vgamma takes a scalar value, then that value will serve as the prior variance for all of the gammas. The default variance is large and set to 1.0E6 for an uninformative flat prior.
Type of prior for the variance of the spatial random effects. Can be set to a fixed positive scalar, or to an inverse-gamma distribution ("1/Gamma") with parameters shape and rate, or to a uniform distribution ("Uniform") on the interval $[0,Vrho.max]$ . Default set to "1/Gamma".
The shape parameter for the Gamma prior on the precision of the spatial random effects. Default value is shape=0.05 for uninformative prior.
The rate (1/scale) parameter for the Gamma prior on the precision of the spatial random effects. Default value is $rate=0.0005$ for uninformative prior.
Upper bound for the uniform prior of the spatial random effect variance. Default set to $1000$ .
The seed for the random number generator. Default set to 1234.
A switch $(0,1)$ which determines whether or not the progress of the sampler is printed to the screen. Default is 1: a progress bar is printed, indicating the step (in $\%$ ) reached by the Gibbs sampler.
A switch $(0,1)$ which determines whether or not the sampled values for rhos are saved. Default is 0: the posterior mean is computed and returned in the rho.pred vector. Be careful, setting save.rho to 1 might require a large amount of memory.
A switch $(0,1)$ which determines whether or not the sampled values for predictions are saved. Default is 0: the posterior mean is computed and returned in the prob.p.pred vector. Be careful, setting save.p to 1 might require a large amount of memory.

## **Details**

The model integrates two processes, an ecological process associated to the presence or absence of the species due to habitat suitability and an observation process that takes into account the fact that the probability of detection of the species is inferior to one. The ecological process includes an intrinsic conditional autoregressive model (iCAR) model for spatial autocorrelation between observations, assuming that the probability of presence of the species at one site depends on the probability of presence of the species on neighboring sites.

# **Ecological process:**

$$z_i \sim \mathcal{B}ernoulli(\theta_i)$$
  
 $logit(\theta_i) = X_i\beta + \rho_{j(i)}$ 

 $\rho_i$ : spatial random effect

j(i): index of the spatial entity for observation i.

#### **Spatial autocorrelation:**

An intrinsic conditional autoregressive model (iCAR) is assumed:

$$\rho_j \sim \mathcal{N}ormal(\mu_j, V_\rho/n_j)$$

 $\mu_j$ : mean of  $\rho_{j'}$  in the neighborhood of j.

 $V_{\rho}$ : variance of the spatial random effects.

 $n_i$ : number of neighbors for spatial entity j.

## **Observation process:**

$$y_i \sim \mathcal{B}inomial(z_i * \delta_i, t_i)$$
  
$$logit(\delta_i) = W_i \gamma$$

#### Value

mcmc An mcmc object that contains the posterior sample. This object can be summa-

rized by functions provided by the coda package. The posterior sample of the

deviance D, with  $D = -2\log(\prod_i P(y_i, z_i|...))$ , is also provided.

rho.pred If save.rho is set to 0 (default), rho.pred is the predictive posterior mean of

the spatial random effect associated to each spatial entity. If save.rho is set to 1, rho.pred is an mcmc object with sampled values for each spatial random

effect associated to each spatial entity.

prob.p.pred If save.p is set to 0 (default), prob.p.pred is the predictive posterior mean

of the probability associated to the suitability process for each prediction. If save.p is set to 1, prob.p.pred is an mcmc object with sampled values of the

probability associated to the suitability process for each prediction.

prob.p.latent Predictive posterior mean of the probability associated to the suitability process

for each observation.

prob.q.latent Predictive posterior mean of the probability associated to the observability pro-

cess for each observation.

#### Author(s)

Ghislain Vieilledent <ghislain.vieilledent@cirad.fr>

#### References

Gelfand, A. E.; Schmidt, A. M.; Wu, S.; Silander, J. A.; Latimer, A. and Rebelo, A. G. (2005) Modelling species diversity through species level hierarchical modelling. *Applied Statistics*, 54, 1-20.

Latimer, A. M.; Wu, S. S.; Gelfand, A. E. and Silander, J. A. (2006) Building statistical models to analyze species distributions. *Ecological Applications*, 16, 33-50.

MacKenzie, D. I.; Nichols, J. D.; Lachman, G. B.; Droege, S.; Andrew Royle, J. and Langtimm, C. A. (2002) Estimating site occupancy rates when detection probabilities are less than one. *Ecology*, 83, 2248-2255.

### See Also

```
plot.mcmc, summary.mcmc
```

## **Examples**

```
## Not run:
# hSDM.ZIB.iCAR()
# Example with simulated data
#=======
#== Preambule
library(hSDM)
library(raster)
library(sp)
library(mvtnorm)
#========
#== Data simulation
# Set seed for repeatability
seed <- 1234
# Target parameters
beta.target <- matrix(c(0.2,0.5,0.5),ncol=1)
gamma.target <- matrix(c(1),ncol=1)</pre>
## Uncomment if you want covariates on the observability process
## gamma.target <- matrix(c(0.2,0.5,0.5),ncol=1)</pre>
Vrho.target <- 1 # Spatial Variance</pre>
Landscape <- raster(ncol=20,nrow=20,crs='+proj=utm +zone=1')</pre>
ncell <- ncell(Landscape)</pre>
# Neighbors
neighbors.mat <- adjacent(Landscape, cells=c(1:ncell), directions=8, pairs=TRUE, sorted=TRUE)</pre>
n.neighbors <- as.data.frame(table(as.factor(neighbors.mat[,1])))[,2]</pre>
adj <- neighbors.mat[,2]</pre>
# Generate symmetric adjacency matrix, A
A <- matrix(0,ncell,ncell)
index.start <- 1</pre>
for (i in 1:ncell) {
    index.end <- index.start+n.neighbors[i]-1</pre>
   A[i,adj[c(index.start:index.end)]] <- 1
    index.start <- index.end+1</pre>
}
# Spatial effects
```

```
d <- 1 # Spatial dependence parameter = 1 for intrinsic CAR
Q <- diag(n.neighbors)-d*A + diag(.0001,ncell) # Add small constant to make Q non-singular
covrho <- Vrho.target*solve(Q) # Covariance of rhos</pre>
set.seed(seed)
rho <- c(rmvnorm(1,sigma=covrho)) # Spatial Random Effects</pre>
rho <- rho-mean(rho) # Centering rhos on zero</pre>
# Visited cells
n.visited <- 150 # Compare with 400, 350 and 100 for example
set.seed(seed)
visited.cells <- sort(sample(1:ncell,n.visited,replace=FALSE)) # Draw visited cells at random
notvisited.cells <- c(1:ncell)[-visited.cells]</pre>
# Number of observations
nobs <- 300
# Cell vector
set.seed(seed)
cells <- c(visited.cells,sample(visited.cells,nobs-n.visited,replace=TRUE))</pre>
coords <- xyFromCell(Landscape,cells) # Get coordinates</pre>
# Covariates for "suitability" process
set.seed(seed)
X1.cell <- rnorm(n=ncell,0,1)</pre>
set.seed(2*seed)
X2.cell <- rnorm(n=ncell,0,1)</pre>
X1 <- X1.cell[cells]</pre>
X2 <- X2.cell[cells]</pre>
X <- cbind(rep(1,nobs),X1,X2)</pre>
# Covariates for "observability" process
W <- cbind(rep(1,nobs))</pre>
## Uncomment if you want covariates on the observability process
## set.seed(3*seed)
## W1 <- rnorm(n=nobs,0,1)
## set.seed(4*seed)
## W2 <- rnorm(n=nobs,0,1)
## W <- cbind(rep(1,nobs),W1,W2)
#== Simulating latent variables
# Suitability
logit.theta.1 <- vector()</pre>
for (n in 1:nobs) {
  logit.theta.1[n] <- X[n,]%*%beta.target+rho[cells[n]]</pre>
theta.1 <- inv.logit(logit.theta.1)</pre>
set.seed(seed)
y.1 <- rbinom(nobs,1,theta.1)</pre>
# Observability
set.seed(seed)
trials <- rpois(nobs,5) # Number of trial associated to each observation
```

```
trials[trials==0] <- 1</pre>
logit.theta.2 <- W%*%gamma.target</pre>
theta.2 <- inv.logit(logit.theta.2)</pre>
set.seed(seed)
y.2 <- rbinom(nobs,trials,theta.2)</pre>
#== Simulating response variable
Y < -y.2*y.1
#== Data-set
Data <- data.frame(Y,trials,cells,X1,X2)</pre>
## Uncomment if you want covariates on the observability process
## Data <- data.frame(Y,trials,cells,X1,X2,W1,W2)</pre>
Data <- SpatialPointsDataFrame(coords=coords,data=Data)</pre>
plot(Data)
#== Data-set for predictions (suitability on each spatial cell)
Data.pred <- data.frame(X1=X1.cell,X2=X2.cell,cells=c(1:ncell))</pre>
#== Site-occupancy model
mod.hSDM.ZIB.iCAR <- hSDM.ZIB.iCAR(presences=Data$Y,</pre>
                                    trials=Data$trials,
                                    suitability=~X1+X2,
                                    observability=~1,
                                    spatial.entity=Data$cells,
                                    data=Data,
                                    n.neighbors=n.neighbors,
                                    neighbors=adj,
                                    ## suitability.pred=NULL,
                                    ## spatial.entity.pred=NULL,
                                    suitability.pred=Data.pred,
                                    spatial.entity.pred=Data.pred$cells,
                                    burnin=5000, mcmc=5000, thin=5,
                                    beta.start=0,
                                    gamma.start=0,
                                    Vrho.start=10,
                                    priorVrho="1/Gamma",
                                    #priorVrho="Uniform",
                                    #priorVrho=10,
                                    mubeta=0, Vbeta=1.0E6,
                                    mugamma=0, Vgamma=1.0E6,
                                    shape=0.5, rate=0.0005,
                                    #Vrho.max=1000,
                                    seed=1234, verbose=1,
                                    save.rho=1, save.p=0)
#=======
#== Outputs
#= Parameter estimates
summary(mod.hSDM.ZIB.iCAR$mcmc)
```

hSDM.ZIB.iCAR.alteration

```
#= MCMC and posteriors
pdf(file="Posteriors_hSDM.ZIB.iCAR.pdf")
plot(mod.hSDM.ZIB.iCAR$mcmc)
dev.off()
pdf(file="Posteriors.rho_hSDM.ZIB.iCAR.pdf")
plot(mod.hSDM.ZIB.iCAR$rho.pred)
dev.off()
#= Summary plots
# rho
r.rho <- r.rho.pred <- r.visited <- Landscape</pre>
r.rho[] <- rho
rho.pred <- apply(mod.hSDM.ZIB.iCAR$rho.pred,2,mean)</pre>
r.rho.pred[] <- rho.pred</pre>
r.visited[] <- 0
r.visited[visited.cells] <- 1</pre>
# prob.p
r.prob.p <- Landscape</pre>
r.prob.p[] <- mod.hSDM.ZIB.iCAR$prob.p.pred</pre>
pdf(file="Summary_hSDM.ZIB.iCAR.pdf")
par(mfrow=c(3,2))
plot(r.rho, main="rho target")
plot(r.visited,main="Visited cells and presences")
plot(Data[Y>0,],add=TRUE,pch=16,cex=0.5)
plot(r.rho.pred, main="rho estimated")
plot(rho[visited.cells],rho.pred[visited.cells],
     xlab="rho target",
     ylab="rho estimated")
points(rho[notvisited.cells],rho.pred[notvisited.cells],pch=16,col="blue")
legend(x=-4,y=3.5,legend="Unvisited cells",col="blue",pch=16,bty="n")
abline(a=0,b=1,col="red")
plot(r.prob.p,main="Proba of presence")
plot(Data[Y>0,],add=TRUE,pch=16,cex=0.5)
dev.off()
## End(Not run)
```

hSDM.ZIB.iCAR.alteration

ZIB (Zero-Inflated Binomial) model with CAR process taking into account site alteration

## **Description**

The hSDM.ZIB.iCAR.alteration function can be used to model species distribution including different processes in a hierarchical Bayesian framework: (i) a *Bernoulli* suitability process (refering to environmental suitability) which takes into account the spatial dependence of the observations, (ii) an alteration process (refering to anthropogenic disturbances), and (iii) a *Binomial* observability process (refering to various ecological and methodological issues explaining the species detection). The hSDM.ZIB.iCAR.alteration function calls a Gibbs sampler written in C code which uses an adaptive Metropolis algorithm to estimate the conditional posterior distribution of hierarchical model's parameters.

## Usage

```
hSDM.ZIB.iCAR.alteration(presences, trials, suitability, observability, spatial.entity, alteration, data, n.neighbors, neighbors, suitability.pred=NULL, spatial.entity.pred=NULL, burnin = 5000, mcmc = 10000, thin = 10, beta.start, gamma.start, Vrho.start, mubeta = 0, Vbeta = 1e+06, mugamma = 0, Vgamma = 1e+06, priorVrho = "1/Gamma", shape = 0.5, rate = 0.0005, Vrho.max=1000, seed = 1234, verbose = 1, save.rho = 0, save.p = 0)
```

## **Arguments**

presences	A vector indicating the number of successes (or presences) for each observation.	
trials	A vector indicating the number of trials for each observation. $t_i$ should be superior to zero and superior or equal to $y_i$ , the number of successes for observation $i$ .	
suitability	A one-sided formula of the form $\sim x_1++x_p$ with $p$ terms specifying the explicative variables for the suitability process.	
observability	A one-sided formula of the form $\sim w_1++w_q$ with $q$ terms specifying the explicative variables for the observability process.	
spatial.entity	A vector indicating the spatial entity identifier (from one to the total number of entities) for each observation. Several observations can occur in one spatial entity. A spatial entity can be a raster cell for example.	
alteration	A vector indicating the proportion of area in the spatial cell which is transformed (by anthropogenic activities for example) for each observation. Must be between 0 and 1.	
data	A data frame containing the model's variables.	
n.neighbors	A vector of integers that indicates the number of neighbors (adjacent entities) of each spatial entity. length(n.neighbors) indicates the total number of spatial entities.	
neighbors	A vector of integers indicating the neighbors (adjacent entities) of each spatial entity. Must be of the form c(neighbors of entity 1, neighbors of entity 2,, neighbors of the last entity). Length of the neighbors vector should be equal to sum(n.neighbors).	
suitability.pred		

NULL, the observations are used.

An optional data frame in which to look for variables with which to predict. If

spatial.entity.pred

An optional vector indicating the spatial entity identifier (from one to the total number of entities) for predictions. If NULL, the vector spatial.entity for observations is used.

burnin The number of burnin iterations for the sampler.

mcmc The number of Gibbs iterations for the sampler. Total number of Gibbs iterations is equal to burnin+mcmc. burnin+mcmc must be divisible by 10 and superior or

equal to 100 so that the progress bar can be displayed.

thin The thinning interval used in the simulation. The number of mcmc iterations

must be divisible by this value.

beta. start Starting values for  $\beta$  parameters of the suitability process. This can either be a

scalar or a p-length vector.

gamma.start Starting values for  $\beta$  parameters of the observability process. This can either be

a scalar or a q-length vector.

Vrho. start Positive scalar indicating the starting value for the variance of the spatial random

effects.

mubeta Means of the priors for the  $\beta$  parameters of the suitability process. mubeta must

be either a scalar or a p-length vector. If mubeta takes a scalar value, then that value will serve as the prior mean for all of the betas. The default value is set to

0 for an uninformative prior.

Vbeta Variances of the Normal priors for the  $\beta$  parameters of the suitability process.

Vbeta must be either a scalar or a p-length vector. If Vbeta takes a scalar value, then that value will serve as the prior variance for all of the betas. The default

variance is large and set to 1.0E6 for an uninformative flat prior.

mugamma Means of the Normal priors for the  $\gamma$  parameters of the observability process.

mugamma must be either a scalar or a p-length vector. If mugamma takes a scalar value, then that value will serve as the prior mean for all of the gammas. The

default value is set to 0 for an uninformative prior.

Vgamma Variances of the Normal priors for the  $\gamma$  parameters of the observability process.

Vgamma must be either a scalar or a p-length vector. If Vgamma takes a scalar value, then that value will serve as the prior variance for all of the gammas. The

default variance is large and set to 1.0E6 for an uninformative flat prior.

priorVrho Type of prior for the variance of the spatial random effects. Can be set to a fixed

positive scalar, or to an inverse-gamma distribution ("1/Gamma") with parameters shape and rate, or to a uniform distribution ("Uniform") on the interval

[0,Vrho.max]. Default set to "1/Gamma".

shape The shape parameter for the Gamma prior on the precision of the spatial random

effects. Default value is shape=0.05 for uninformative prior.

rate The rate (1/scale) parameter for the Gamma prior on the precision of the spatial

random effects. Default value is rate=0.0005 for uninformative prior.

Vrho.max Upper bound for the uniform prior of the spatial random effect variance. Default

set to 1000.

seed The seed for the random number generator. Default set to 1234.

verbose A switch (0,1) which determines whether or not the progress of the sampler is

printed to the screen. Default is 1: a progress bar is printed, indicating the step

(in %) reached by the Gibbs sampler.

save.rho A switch (0,1) which determines whether or not the sampled values for rhos

are saved. Default is 0: the posterior mean is computed and returned in the rho.pred vector. Be careful, setting save.rho to 1 might require a large amount

of memory.

save.p A switch (0,1) which determines whether or not the sampled values for predic-

tions are saved. Default is 0: the posterior mean is computed and returned in the prob.p.pred vector. Be careful, setting save.p to 1 might require a large

amount of memory.

#### **Details**

The model integrates two processes, an ecological process associated to the presence or absence of the species due to habitat suitability and an observation process that takes into account the fact that the probability of detection of the species is inferior to one. The ecological process includes an intrinsic conditional autoregressive model (iCAR) model for spatial autocorrelation between observations, assuming that the probability of presence of the species at one site depends on the probability of presence of the species on neighboring sites.

# **Ecological process:**

$$z_i \sim \mathcal{B}ernoulli(\theta_i)$$

$$logit(\theta_i) = X_i\beta + \rho_{j(i)}$$

 $\rho_i$ : spatial random effect

j(i): index of the spatial entity for observation i.

#### **Spatial autocorrelation:**

An intrinsic conditional autoregressive model (iCAR) is assumed:

$$\rho_j \sim \mathcal{N}ormal(\mu_j, V_\rho/n_j)$$

 $\mu_j$ : mean of  $\rho_{j'}$  in the neighborhood of j.

 $V_{\rho}$ : variance of the spatial random effects.

 $n_i$ : number of neighbors for spatial entity j.

## **Observation process:**

$$y_i \sim \mathcal{B}inomial(z_i * \delta_i, t_i)$$

$$logit(\delta_i) = W_i \gamma$$

# Value

mcmc An mcmc object that contains the posterior sample. This object can be summa-

rized by functions provided by the coda package. The posterior sample of the

deviance D, with  $D = -2 \log(\prod_i P(y_i, z_i|...))$ , is also provided.

rho.pred If save.rho is set to 0 (default), rho.pred is the predictive posterior mean of

the spatial random effect associated to each spatial entity. If save.rho is set to 1, rho.pred is an mcmc object with sampled values for each spatial random

effect associated to each spatial entity.

prob.p.pred	If save.p is set to 0 (default), prob.p.pred is the predictive posterior mean of the probability associated to the suitability process for each prediction. If save.p is set to 1, prob.p.pred is an mcmc object with sampled values of the probability associated to the suitability process for each prediction.
prob.p.latent	Predictive posterior mean of the probability associated to the suitability process for each observation.
prob.q.latent	Predictive posterior mean of the probability associated to the observability pro-

cess for each observation.

# Author(s)

Ghislain Vieilledent <ghislain.vieilledent@cirad.fr>

## References

Gelfand, A. E.; Schmidt, A. M.; Wu, S.; Silander, J. A.; Latimer, A. and Rebelo, A. G. (2005) Modelling species diversity through species level hierarchical modelling. *Applied Statistics*, 54, 1-20.

Latimer, A. M.; Wu, S. S.; Gelfand, A. E. and Silander, J. A. (2006) Building statistical models to analyze species distributions. *Ecological Applications*, 16, 33-50.

MacKenzie, D. I.; Nichols, J. D.; Lachman, G. B.; Droege, S.; Andrew Royle, J. and Langtimm, C. A. (2002) Estimating site occupancy rates when detection probabilities are less than one. *Ecology*, 83, 2248-2255.

#### See Also

```
plot.mcmc, summary.mcmc
```

# **Examples**

```
# Target parameters
beta.target <- matrix(c(0.2,0.5,0.5),ncol=1)
gamma.target <- matrix(c(1),ncol=1)</pre>
## Uncomment if you want covariates on the observability process
## gamma.target <- matrix(c(0.2,0.5,0.5),ncol=1)</pre>
Vrho.target <- 1 # Spatial Variance</pre>
# Landscape
Landscape <- raster(ncol=20,nrow=20,crs='+proj=utm +zone=1')</pre>
ncell <- ncell(Landscape)</pre>
# Neighbors
neighbors.mat <- adjacent(Landscape, cells=c(1:ncell), directions=8, pairs=TRUE, sorted=TRUE)</pre>
n.neighbors <- as.data.frame(table(as.factor(neighbors.mat[,1])))[,2]</pre>
adj <- neighbors.mat[,2]</pre>
# Generate symmetric adjacency matrix, A
A <- matrix(0,ncell,ncell)
index.start <- 1</pre>
for (i in 1:ncell) {
    index.end <- index.start+n.neighbors[i]-1</pre>
    A[i,adj[c(index.start:index.end)]] <- 1
    index.start <- index.end+1</pre>
}
# Spatial effects
d <- 1 # Spatial dependence parameter = 1 for intrinsic CAR
Q <- diag(n.neighbors)-d*A + diag(.0001,ncell) # Add small constant to make Q non-singular
covrho <- Vrho.target*solve(Q) # Covariance of rhos</pre>
set.seed(seed)
rho <- c(rmvnorm(1,sigma=covrho)) # Spatial Random Effects</pre>
rho <- rho-mean(rho) # Centering rhos on zero</pre>
# Visited cells
n.visited <- 150 # Compare with 400, 350 and 100 for example
set.seed(seed)
visited.cells <- sort(sample(1:ncell,n.visited,replace=FALSE)) # Draw visited cells at random
notvisited.cells <- c(1:ncell)[-visited.cells]</pre>
# Number of observations
nobs <- 300
# Cell vector
set.seed(seed)
cells <- c(visited.cells,sample(visited.cells,nobs-n.visited,replace=TRUE))</pre>
coords <- xyFromCell(Landscape,cells) # Get coordinates</pre>
# Covariates for "suitability" process
set.seed(seed)
X1.cell <- rnorm(n=ncell,0,1)</pre>
set.seed(2*seed)
X2.cell <- rnorm(n=ncell,0,1)</pre>
```

```
X1 <- X1.cell[cells]</pre>
X2 <- X2.cell[cells]</pre>
X <- cbind(rep(1,nobs),X1,X2)</pre>
# Alteration
U <- runif(n=nobs,min=0,max=1)</pre>
# Covariates for "observability" process
W <- cbind(rep(1,nobs))</pre>
## Uncomment if you want covariates on the observability process
## set.seed(3*seed)
## W1 <- rnorm(n=nobs,0,1)
## set.seed(4*seed)
## W2 <- rnorm(n=nobs,0,1)
## W <- cbind(rep(1,nobs),W1,W2)
#== Simulating latent variables
# Suitability
logit.theta.1 <- vector()</pre>
for (n in 1:nobs) {
  logit.theta.1[n] <- X[n,]%*%beta.target+rho[cells[n]]</pre>
}
theta.1 <- inv.logit(logit.theta.1)</pre>
set.seed(seed)
y.1 <- rbinom(nobs,1,theta.1)</pre>
# Alteration
u <- rbinom(nobs,1,U)</pre>
# Observability
set.seed(seed)
trials <- rpois(nobs,5) # Number of trial associated to each observation
trials[trials==0] <- 1</pre>
logit.theta.2 <- W%*%gamma.target</pre>
theta.2 <- inv.logit(logit.theta.2)</pre>
set.seed(seed)
y.2 <- rbinom(nobs,trials,theta.2)</pre>
#== Simulating response variable
Y <- y.2*(1-u)*y.1
#== Data-set
Data <- data.frame(Y,trials,cells,X1,X2,U)</pre>
## Uncomment if you want covariates on the observability process
## Data <- data.frame(Y,trials,cells,X1,X2,W1,W2,U)</pre>
Data <- SpatialPointsDataFrame(coords=coords,data=Data)</pre>
plot(Data)
#== Data-set for predictions (suitability on each spatial cell)
Data.pred <- data.frame(X1=X1.cell,X2=X2.cell,cells=c(1:ncell))</pre>
```

```
#== Site-occupancy model
mod.hSDM.ZIB.iCAR.alteration <- hSDM.ZIB.iCAR.alteration(presences=Data$Y,</pre>
                                                 trials=Data$trials,
                                                 suitability=~X1+X2,
                                                 observability=~1,
                                                 spatial.entity=Data$cells,
                                                 alteration=Data$U,
                                                 data=Data,
                                                 n.neighbors=n.neighbors,
                                                 neighbors=adj,
                                                 ## suitability.pred=NULL,
                                                 ## spatial.entity.pred=NULL,
                                                 suitability.pred=Data.pred,
                                                 spatial.entity.pred=Data.pred$cells,
                                                 burnin=5000, mcmc=5000, thin=5,
                                                 beta.start=0,
                                                 gamma.start=0,
                                                 Vrho.start=10,
                                                 priorVrho="1/Gamma",
                                                 #priorVrho="Uniform",
                                                 #priorVrho=10,
                                                 mubeta=0, Vbeta=1.0E6,
                                                 mugamma=0, Vgamma=1.0E6,
                                                 shape=0.5, rate=0.0005,
                                                 #Vrho.max=1000,
                                                 seed=1234, verbose=1,
                                                 save.rho=1, save.p=0)
#=======
#== Outputs
#= Parameter estimates
summary(mod.hSDM.ZIB.iCAR.alteration$mcmc)
#= MCMC and posteriors
pdf(file="Posteriors_hSDM.ZIB.iCAR.alteration.pdf")
plot(mod.hSDM.ZIB.iCAR.alteration$mcmc)
dev.off()
pdf(file="Posteriors.rho_hSDM.ZIB.iCAR.alteration.pdf")
plot(mod.hSDM.ZIB.iCAR.alteration$rho.pred)
dev.off()
#= Summary plots
# rho
r.rho <- r.rho.pred <- r.visited <- Landscape</pre>
r.rho[] <- rho
rho.pred <- apply(mod.hSDM.ZIB.iCAR.alteration$rho.pred,2,mean)</pre>
r.rho.pred[] <- rho.pred</pre>
r.visited[] <- 0</pre>
r.visited[visited.cells] <- 1</pre>
```

```
# prob.p
r.prob.p <- Landscape</pre>
r.prob.p[] <- mod.hSDM.ZIB.iCAR.alteration$prob.p.pred</pre>
pdf(file="Summary_hSDM.ZIB.iCAR.alteration.pdf")
par(mfrow=c(3,2))
plot(r.rho, main="rho target")
plot(r.visited,main="Visited cells and presences")
plot(Data[Y>0,],add=TRUE,pch=16,cex=0.5)
plot(r.rho.pred, main="rho estimated")
plot(rho[visited.cells], rho.pred[visited.cells],
     xlab="rho target",
     ylab="rho estimated")
points(rho[notvisited.cells],rho.pred[notvisited.cells],pch=16,col="blue")
legend(x=-4,y=3.5,legend="Unvisited cells",col="blue",pch=16,bty="n")
abline(a=0,b=1,col="red")
plot(r.prob.p,main="Proba of presence")
plot(Data[Y>0,],add=TRUE,pch=16,cex=0.5)
dev.off()
## End(Not run)
```

hSDM.ZIP

ZIP (Zero-Inflated Poisson) model

# Description

The hSDM.ZIP function can be used to model species distribution including different processes in a hierarchical Bayesian framework: a  $\mathcal{B}ernoulli$  suitability process (refering to various ecological variables explaining environmental suitability or not) and a  $\mathcal{P}oisson$  abundance process (refering to various ecological variables explaining the species abundance when the habitat is suitable). The hSDM.ZIP function calls a Gibbs sampler written in C code which uses a Metropolis algorithm to estimate the conditional posterior distribution of hierarchical model's parameters.

#### Usage

```
hSDM.ZIP(counts, suitability, abundance, data, suitability.pred=NULL, burnin = 5000, mcmc = 10000, thin = 10, beta.start, gamma.start, mubeta = 0, Vbeta = 1e+06, mugamma = 0, Vgamma = 1e+06, seed = 1234, verbose = 1, save.p = 0)
```

# Arguments

counts A vector indicating the count for each observation.

suitability A one-sided formula of the form  $\sim x_1 + ... + x_p$  with p terms specifying the

explicative variables for the suitability process.

abundance A one-sided formula of the form  $\sim w_1 + ... + w_q$  with q terms specifying the

explicative variables for the abundance process.

data A data frame containing the model's variables.

suitability.pred

An optional data frame in which to look for variables with which to predict. If

NULL, the observations are used.

burnin The number of burnin iterations for the sampler.

mcmc The number of Gibbs iterations for the sampler. Total number of Gibbs iterations

is equal to burnin+mcmc. burnin+mcmc must be divisible by 10 and superior or

equal to 100 so that the progress bar can be displayed.

thin The thinning interval used in the simulation. The number of mcmc iterations

must be divisible by this value.

beta. start Starting values for  $\beta$  parameters of the suitability process. This can either be a

scalar or a *p*-length vector.

gamma.start Starting values for  $\beta$  parameters of the abundance process. This can either be a

scalar or a q-length vector.

mubeta Means of the priors for the  $\beta$  parameters of the suitability process. mubeta must

be either a scalar or a p-length vector. If mubeta takes a scalar value, then that value will serve as the prior mean for all of the betas. The default value is set to

0 for an uninformative prior.

Vbeta Variances of the Normal priors for the  $\beta$  parameters of the suitability process.

Vbeta must be either a scalar or a p-length vector. If Vbeta takes a scalar value, then that value will serve as the prior variance for all of the betas. The default

variance is large and set to 1.0E6 for an uninformative flat prior.

mugamma Means of the Normal priors for the  $\gamma$  parameters of the abundance process.

mugamma must be either a scalar or a p-length vector. If mugamma takes a scalar value, then that value will serve as the prior mean for all of the gammas. The

default value is set to 0 for an uninformative prior.

Vgamma Variances of the Normal priors for the  $\gamma$  parameters of the abundance process.

Vgamma must be either a scalar or a p-length vector. If Vgamma takes a scalar value, then that value will serve as the prior variance for all of the gammas. The

default variance is large and set to 1.0E6 for an uninformative flat prior.

seed The seed for the random number generator. Default set to 1234.

verbose A switch (0,1) which determines whether or not the progress of the sampler is

printed to the screen. Default is 1: a progress bar is printed, indicating the step

(in %) reached by the Gibbs sampler.

save. p A switch (0,1) which determines whether or not the sampled values for predic-

tions are saved. Default is 0: the posterior mean is computed and returned in the prob.p.pred vector. Be careful, setting save.p to 1 might require a large

amount of memory.

#### **Details**

The model integrates two processes, an ecological process associated to habitat suitability (habitat is suitable or not for the species) and an abundance process that takes into account ecological variables explaining the species abundance when the habitat is suitable.

#### **Suitability process:**

$$z_i \sim \mathcal{B}ernoulli(\theta_i)$$
  
 $logit(\theta_i) = X_i\beta$ 

## Abundance process:

$$y_i \sim \mathcal{P}oisson(z_i * \lambda_i)$$
  
$$log(\lambda_i) = W_i \gamma$$

#### Value

An meme object that contains the posterior sample. This object can be summarized by functions provided by the code posterior. The posterior sample of the

rized by functions provided by the coda package. The posterior sample of the

deviance D, with  $D = -2 \log(\prod_i P(y_i, z_i | ...))$ , is also provided.

prob.p.pred If save.p is set to 0 (default), prob.p.pred is the predictive posterior mean

of the probability associated to the suitability process for each prediction. If save.p is set to 1, prob.p.pred is an mcmc object with sampled values of the

probability associated to the suitability process for each prediction.

prob.p.latent Predictive posterior mean of the probability associated to the suitability process

for each observation.

prob.q.latent Predictive posterior mean of the probability associated to the abundance process

for each observation.

## Author(s)

Ghislain Vieilledent <ghislain.vieilledent@cirad.fr>

# References

Flores, O.; Rossi, V. and Mortier, F. (2009) Autocorrelation offsets zero-inflation in models of tropical saplings density. *Ecological Modelling*, 220, 1797-1809.

Gelfand, A. E.; Schmidt, A. M.; Wu, S.; Silander, J. A.; Latimer, A. and Rebelo, A. G. (2005) Modelling species diversity through species level hierarchical modelling. *Applied Statistics*, 54, 1-20.

Latimer, A. M.; Wu, S. S.; Gelfand, A. E. and Silander, J. A. (2006) Building statistical models to analyze species distributions. *Ecological Applications*, 16, 33-50.

# See Also

```
plot.mcmc, summary.mcmc
```

# **Examples**

## Not run:

# hSDM.ZIP()

# Example with simulated data

```
#=======
#== Preambule
library(hSDM)
#=========
#== Data simulation
# Set seed for repeatability
seed <- 1234
# Number of observations
nobs <- 1000
# Target parameters
beta.target <- matrix(c(0.2,0.5,0.5),ncol=1)
gamma.target <- matrix(c(1),ncol=1)</pre>
## Uncomment if you want covariates on the abundance process
## gamma.target <- matrix(c(0.2,0.5,0.5),ncol=1)
# Covariates for "suitability" process
set.seed(seed)
X1 <- rnorm(n=nobs,0,1)</pre>
set.seed(2*seed)
X2 <- rnorm(n=nobs,0,1)</pre>
X <- cbind(rep(1,nobs),X1,X2)</pre>
# Covariates for "abundance" process
W <- cbind(rep(1,nobs))</pre>
## Uncomment if you want covariates on the abundance process
## set.seed(3*seed)
## W1 <- rnorm(n=nobs,0,1)
## set.seed(4*seed)
## W2 <- rnorm(n=nobs,0,1)
## W <- cbind(rep(1,nobs),W1,W2)
#== Simulating latent variables
# Suitability
logit.theta <- X %*% beta.target</pre>
theta <- inv.logit(logit.theta)</pre>
set.seed(seed)
y.1 <- rbinom(nobs,1,theta)
# Abundance
set.seed(seed)
log.lambda <- W %*% gamma.target</pre>
lambda <- exp(log.lambda)</pre>
set.seed(seed)
y.2 <- rpois(nobs,lambda)</pre>
#== Simulating response variable
```

```
Y < -y.2*y.1
#== Data-set
Data <- data.frame(Y,X1,X2)</pre>
## Uncomment if you want covariates on the abundance process
## Data <- data.frame(Y,X1,X2,W1,W2)</pre>
#== ZIP model
mod.hSDM.ZIP <- hSDM.ZIP(counts=Data$Y,</pre>
                         suitability=~X1+X2,
                         abundance=~1, #=~1+W1+W2 if covariates
                         data=Data,
                         suitability.pred=NULL,
                         burnin=1000, mcmc=1000, thin=5,
                         beta.start=0,
                         gamma.start=0,
                         mubeta=0, Vbeta=1.0E6,
                         mugamma=0, Vgamma=1.0E6,
                         seed=1234, verbose=1,
                         save.p=0)
#== Outputs
pdf(file="Posteriors_hSDM.ZIP.pdf")
plot(mod.hSDM.ZIP$mcmc)
dev.off()
summary(mod.hSDM.ZIP$prob.p.latent)
summary(mod.hSDM.ZIP$prob.q.latent)
summary(mod.hSDM.ZIP$prob.p.pred)
## End(Not run)
```

hSDM.ZIP.iCAR

ZIP (Zero-Inflated Poisson) model with CAR process

# Description

The hSDM.ZIP.iCAR function can be used to model species distribution including different processes in a hierarchical Bayesian framework: a  $\mathcal{B}ernoulli$  suitability process (refering to various ecological variables explaining environmental suitability or not) which takes into account the spatial dependence of the observations, and a  $\mathcal{P}oisson$  abundance process (refering to various ecological variables explaining the species abundance when the habitat is suitable). The hSDM.ZIP.iCAR function calls a Gibbs sampler written in C code which uses an adaptive Metropolis algorithm to estimate the conditional posterior distribution of hierarchical model's parameters.

#### Usage

```
hSDM.ZIP.iCAR(counts, suitability, abundance, spatial.entity, data, n.neighbors, neighbors, suitability.pred=NULL, spatial.entity.pred=NULL, burnin = 5000, mcmc = 10000, thin = 10, beta.start, gamma.start, Vrho.start, mubeta = 0, Vbeta = 1e+06, mugamma = 0, Vgamma = 1e+06, priorVrho = "1/Gamma", shape = 0.5, rate = 0.0005, Vrho.max=1000, seed = 1234, verbose = 1, save.rho = 0, save.p = 0)
```

# **Arguments**

counts A vector indicating the count for each observation.

suitability A one-sided formula of the form  $\sim x_1 + ... + x_p$  with p terms specifying the

explicative variables for the suitability process.

abundance A one-sided formula of the form  $\sim w_1 + ... + w_q$  with q terms specifying the

explicative variables for the abundance process.

spatial.entity A vector indicating the spatial entity identifier (from one to the total number

of entities) for each observation. Several observations can occur in one spatial

entity. A spatial entity can be a raster cell for example.

data A data frame containing the model's variables.

n.neighbors A vector of integers that indicates the number of neighbors (adjacent entities) of

each spatial entity. length(n.neighbors) indicates the total number of spatial

entities.

neighbors A vector of integers indicating the neighbors (adjacent entities) of each spatial

entity. Must be of the form c(neighbors of entity 1, neighbors of entity 2, ..., neighbors of the last entity). Length of the neighbors vector should be equal to

sum(n.neighbors).

suitability.pred

An optional data frame in which to look for variables with which to predict. If

NULL, the observations are used.

spatial.entity.pred

An optional vector indicating the spatial entity identifier (from one to the total

 $number\ of\ entities)\ for\ predictions.\ If\ NULL,\ the\ vector\ spatial.\ entity\ for$ 

observations is used.

burnin The number of burnin iterations for the sampler.

mcmc The number of Gibbs iterations for the sampler. Total number of Gibbs iterations

is equal to burnin+mcmc. burnin+mcmc must be divisible by 10 and superior or

equal to 100 so that the progress bar can be displayed.

thin The thinning interval used in the simulation. The number of mcmc iterations

must be divisible by this value.

beta. start Starting values for  $\beta$  parameters of the suitability process. This can either be a

scalar or a p-length vector.

gamma.start Starting values for  $\beta$  parameters of the observability process. This can either be

a scalar or a q-length vector.

Vrho. start Positive scalar indicating the starting value for the variance of the spatial random

effects.

mubeta Means of the priors for the  $\beta$  parameters of the suitability process. mubeta must be either a scalar or a p-length vector. If mubeta takes a scalar value, then that value will serve as the prior mean for all of the betas. The default value is set to 0 for an uninformative prior. Vbeta Variances of the Normal priors for the  $\beta$  parameters of the suitability process. Vbeta must be either a scalar or a p-length vector. If Vbeta takes a scalar value, then that value will serve as the prior variance for all of the betas. The default variance is large and set to 1.0E6 for an uninformative flat prior. Means of the Normal priors for the  $\gamma$  parameters of the observability process. mugamma mugamma must be either a scalar or a p-length vector. If mugamma takes a scalar value, then that value will serve as the prior mean for all of the gammas. The default value is set to 0 for an uninformative prior. Vgamma Variances of the Normal priors for the  $\gamma$  parameters of the observability process. Vgamma must be either a scalar or a p-length vector. If Vgamma takes a scalar value, then that value will serve as the prior variance for all of the gammas. The default variance is large and set to 1.0E6 for an uninformative flat prior. priorVrho Type of prior for the variance of the spatial random effects. Can be set to a fixed positive scalar, or to an inverse-gamma distribution ("1/Gamma") with parameters shape and rate, or to a uniform distribution ("Uniform") on the interval [0,Vrho.max]. Default set to "1/Gamma". shape The shape parameter for the Gamma prior on the precision of the spatial random effects. Default value is shape=0.05 for uninformative prior. rate The rate (1/scale) parameter for the Gamma prior on the precision of the spatial random effects. Default value is rate=0.0005 for uninformative prior. Vrho.max Upper bound for the uniform prior of the spatial random effect variance. Default set to 1000. The seed for the random number generator. Default set to 1234. seed verbose A switch (0,1) which determines whether or not the progress of the sampler is printed to the screen. Default is 1: a progress bar is printed, indicating the step (in %) reached by the Gibbs sampler. save.rho A switch (0,1) which determines whether or not the sampled values for rhos are saved. Default is 0: the posterior mean is computed and returned in the rho.pred vector. Be careful, setting save.rho to 1 might require a large amount of memory. save.p A switch (0,1) which determines whether or not the sampled values for predictions are saved. Default is 0: the posterior mean is computed and returned in the prob.p.pred vector. Be careful, setting save.p to 1 might require a large amount of memory.

#### **Details**

The model integrates two processes, an ecological process associated to habitat suitability (habitat is suitable or not for the species) and an abundance process that takes into account ecological variables explaining the species abundance when the habitat is suitable. The suitability process includes an intrinsic conditional autoregressive model (iCAR) model for spatial autocorrelation between

observations, assuming that the suitability at one site depends on the suitability on neighboring sites.

# **Suitability process:**

$$z_i \sim \mathcal{B}ernoulli(\theta_i)$$

$$logit(\theta_i) = X_i\beta + \rho_{j(i)}$$

 $\rho_i$ : spatial random effect

j(i): index of the spatial entity for observation i.

# **Spatial autocorrelation:**

An intrinsic conditional autoregressive model (iCAR) is assumed:

$$\rho_j \sim \mathcal{N}ormal(\mu_j, V_\rho/n_j)$$

 $\mu_j$ : mean of  $\rho_{j'}$  in the neighborhood of j.

 $V_{\rho}$ : variance of the spatial random effects.

 $n_i$ : number of neighbors for spatial entity j.

# **Abundance process:**

$$y_i \sim Poisson(z_i * \lambda_i)$$

$$log(\lambda_i) = W_i \gamma$$

# Value

mcmc An mcmc object that contains the posterior sample. This object can be summa-

rized by functions provided by the coda package. The posterior sample of the

deviance D, with  $D = -2 \log(\prod_i P(y_i, z_i | ...))$ , is also provided.

rho.pred If save.rho is set to 0 (default), rho.pred is the predictive posterior mean of

the spatial random effect associated to each spatial entity. If save.rho is set to 1, rho.pred is an mcmc object with sampled values for each spatial random

effect associated to each spatial entity.

prob.p.pred If save.p is set to 0 (default), prob.p.pred is the predictive posterior mean

of the probability associated to the suitability process for each prediction. If save.p is set to 1, prob.p.pred is an mcmc object with sampled values of the

probability associated to the suitability process for each prediction.

prob.p.latent Predictive posterior mean of the probability associated to the suitability process

for each observation.

prob.q.latent Predictive posterior mean of the probability associated to the observability pro-

cess for each observation.

# Author(s)

Ghislain Vieilledent <ghislain.vieilledent@cirad.fr>

## References

Flores, O.; Rossi, V. and Mortier, F. (2009) Autocorrelation offsets zero-inflation in models of tropical saplings density. *Ecological Modelling*, 220, 1797-1809.

Gelfand, A. E.; Schmidt, A. M.; Wu, S.; Silander, J. A.; Latimer, A. and Rebelo, A. G. (2005) Modelling species diversity through species level hierarchical modelling. *Applied Statistics*, 54, 1-20.

Latimer, A. M.; Wu, S. S.; Gelfand, A. E. and Silander, J. A. (2006) Building statistical models to analyze species distributions. *Ecological Applications*, 16, 33-50.

#### See Also

```
plot.mcmc, summary.mcmc
```

## **Examples**

```
## Not run:
# hSDM.ZIP.iCAR()
# Example with simulated data
#=======
#== Preambule
library(hSDM)
library(raster)
library(sp)
library(mvtnorm)
#========
#== Data simulation
# Set seed for repeatability
seed <- 1234
# Target parameters
beta.target <- matrix(c(0.2, 0.5, 0.5), ncol=1)
gamma.target <- matrix(c(1),ncol=1)</pre>
## Uncomment if you want covariates on the observability process
## gamma.target <- matrix(c(0.2,0.5,0.5),ncol=1)</pre>
Vrho.target <- 1 # Spatial Variance</pre>
# Landscape
Landscape <- raster(ncol=20,nrow=20,crs='+proj=utm +zone=1')</pre>
ncell <- ncell(Landscape)</pre>
# Neighbors
neighbors.mat <- adjacent(Landscape, cells=c(1:ncell), directions=8, pairs=TRUE, sorted=TRUE)</pre>
n.neighbors <- as.data.frame(table(as.factor(neighbors.mat[,1])))[,2]</pre>
adj <- neighbors.mat[,2]</pre>
```

```
# Generate symmetric adjacency matrix, A
A <- matrix(0,ncell,ncell)
index.start <- 1</pre>
for (i in 1:ncell) {
    index.end <- index.start+n.neighbors[i]-1</pre>
    A[i,adj[c(index.start:index.end)]] <- 1
    index.start <- index.end+1</pre>
}
# Spatial effects
d <- 1 \# Spatial dependence parameter = 1 for intrinsic CAR
Q <- diag(n.neighbors)-d*A + diag(.0001,ncell) # Add small constant to make Q non-singular
covrho <- Vrho.target*solve(Q) # Covariance of rhos</pre>
set.seed(seed)
rho <- c(rmvnorm(1,sigma=covrho)) # Spatial Random Effects</pre>
rho <- rho-mean(rho) # Centering rhos on zero</pre>
# Visited cells
n.visited <- 150 # Compare with 400, 350 and 100 for example
set.seed(seed)
visited.cells <- sort(sample(1:ncell,n.visited,replace=FALSE)) # Draw visited cells at random
notvisited.cells <- c(1:ncell)[-visited.cells]</pre>
# Number of observations
nobs <- 300
# Cell vector
set.seed(seed)
cells <- c(visited.cells,sample(visited.cells,nobs-n.visited,replace=TRUE))</pre>
coords <- xyFromCell(Landscape,cells) # Get coordinates</pre>
# Covariates for "suitability" process
set.seed(seed)
X1.cell <- rnorm(n=ncell,0,1)</pre>
set.seed(2*seed)
X2.cell <- rnorm(n=ncell,0,1)</pre>
X1 <- X1.cell[cells]</pre>
X2 \leftarrow X2.cell[cells]
X <- cbind(rep(1,nobs),X1,X2)</pre>
# Covariates for "abundance" process
W <- cbind(rep(1,nobs))</pre>
## Uncomment if you want covariates on the observability process
## set.seed(3*seed)
## W1 <- rnorm(n=nobs,0,1)
## set.seed(4*seed)
## W2 <- rnorm(n=nobs,0,1)
## W <- cbind(rep(1,nobs),W1,W2)
#== Simulating latent variables
# Suitability
```

```
logit.theta <- vector()</pre>
for (n in 1:nobs) {
  logit.theta[n] \leftarrow X[n,]%*%beta.target+rho[cells[n]]
}
theta <- inv.logit(logit.theta)</pre>
set.seed(seed)
y.1 <- rbinom(nobs,1,theta)</pre>
# Abundance
set.seed(seed)
log.lambda <- W %*% gamma.target</pre>
lambda <- exp(log.lambda)</pre>
set.seed(seed)
y.2 <- rpois(nobs,lambda)
#== Simulating response variable
Y \leftarrow y.2*y.1
#== Data-set
Data <- data.frame(Y,cells,X1,X2)</pre>
## Uncomment if you want covariates on the observability process
## Data <- data.frame(Y,cells,X1,X2,W1,W2)</pre>
Data <- SpatialPointsDataFrame(coords=coords,data=Data)</pre>
plot(Data)
#== Data-set for predictions (suitability on each spatial cell)
Data.pred <- data.frame(X1=X1.cell, X2=X2.cell, cells=c(1:ncell))</pre>
#== ZIP model with CAR
mod.hSDM.ZIP.iCAR <- hSDM.ZIP.iCAR(counts=Data$Y,</pre>
                                      suitability=~X1+X2,
                                      abundance=~1,
                                      spatial.entity=Data$cells,
                                      data=Data,
                                      n.neighbors=n.neighbors,
                                      neighbors=adj,
                                      suitability.pred=Data.pred,
                                      spatial.entity.pred=Data.pred$cells,
                                      burnin=5000, mcmc=5000, thin=5,
                                      beta.start=0,
                                      gamma.start=0,
                                      Vrho.start=10,
                                      priorVrho="1/Gamma",
                                      #priorVrho="Uniform",
                                      #priorVrho=10,
                                      mubeta=0, Vbeta=1.0E6,
                                      mugamma=0, Vgamma=1.0E6,
                                      shape=0.5, rate=0.0005,
                                      #Vrho.max=1000,
                                      seed=1234, verbose=1,
                                      save.rho=1, save.p=0)
```

```
#=======
#== Outputs
#= Parameter estimates
summary(mod.hSDM.ZIP.iCAR$mcmc)
#= MCMC and posteriors
pdf(file="Posteriors_hSDM.ZIP.iCAR.pdf")
plot(mod.hSDM.ZIP.iCAR$mcmc)
dev.off()
pdf(file="Posteriors.rho_hSDM.ZIP.iCAR.pdf")
plot(mod.hSDM.ZIP.iCAR$rho.pred)
dev.off()
#= Summary plots
# rho
r.rho <- r.rho.pred <- r.visited <- Landscape</pre>
r.rho[] <- rho
rho.pred <- apply(mod.hSDM.ZIP.iCAR$rho.pred,2,mean)</pre>
r.rho.pred[] <- rho.pred</pre>
r.visited[] <- 0
r.visited[visited.cells] <- tapply(Data$Y,Data$cells,mean)</pre>
# prob.p
r.prob.p <- Landscape</pre>
r.prob.p[] <- mod.hSDM.ZIP.iCAR$prob.p.pred</pre>
pdf(file="Summary_hSDM.ZIP.iCAR.pdf")
par(mfrow=c(3,2))
plot(r.rho, main="rho target")
plot(r.visited,main="Visited cells and counts")
plot(Data,add=TRUE,pch=16,cex=0.5)
plot(r.rho.pred, main="rho estimated")
plot(rho[visited.cells],rho.pred[visited.cells],
     xlab="rho target",
     ylab="rho estimated")
points(rho[notvisited.cells],rho.pred[notvisited.cells],pch=16,col="blue")
legend(x=-4,y=3.5,legend="Unvisited cells",col="blue",pch=16,bty="n")
abline(a=0,b=1,col="red")
plot(r.prob.p,main="Predicted counts")
plot(Data,add=TRUE,pch=16,cex=0.5)
dev.off()
## End(Not run)
```

hSDM.ZIP.iCAR.alteration

ZIP (Zero-Inflated Poisson) model with CAR process taking into account site alteration

# **Description**

The hSDM.ZIP.iCAR.alteration function can be used to model species distribution including different processes in a hierarchical Bayesian framework: (i) a Bernoulli suitability process (refering to various ecological variables explaining environmental suitability or not) which takes into account the spatial dependence of the observations, (ii) an alteration process (refering to anthropogenic disturbances), and (iii) a Poisson abundance process (refering to various ecological variables explaining the species abundance when the habitat is suitable). The hSDM.ZIP.iCAR.alteration function calls a Gibbs sampler written in C code which uses an adaptive Metropolis algorithm to estimate the conditional posterior distribution of hierarchical model's parameters.

# Usage

```
hSDM.ZIP.iCAR.alteration(counts, suitability, abundance, spatial.entity, alteration, data, n.neighbors, neighbors, suitability.pred=NULL, spatial.entity.pred=NULL, burnin = 5000, mcmc = 10000, thin = 10, beta.start, gamma.start, Vrho.start, mubeta = 0, Vbeta = 1e+06, mugamma = 0, Vgamma = 1e+06, priorVrho = "1/Gamma", shape = 0.5, rate = 0.0005, Vrho.max=1000, seed = 1234, verbose = 1, save.rho = 0, save.p = 0)
```

# **Arguments**

È	guments				
	counts	A vector indicating the count for each observation.			
	suitability	A one-sided formula of the form $\sim x_1++x_p$ with $p$ terms specifying the explicative variables for the suitability process.			
	abundance	A one-sided formula of the form $\sim w_1++w_q$ with $q$ terms specifying the explicative variables for the abundance process.			
	spatial.entity	A vector indicating the spatial entity identifier (from one to the total number of entities) for each observation. Several observations can occur in one spatial entity. A spatial entity can be a raster cell for example.			
	alteration	A vector indicating the proportion of area in the spatial cell which is transformed (by anthropogenic activities for example) for each observation. Must be between 0 and 1.			
	data	A data frame containing the model's variables.			
	n.neighbors	A vector of integers that indicates the number of neighbors (adjacent entities) of each spatial entity. length(n.neighbors) indicates the total number of spatial entities.			
	neighbors	A vector of integers indicating the neighbors (adjacent entities) of each spatial entity. Must be of the form c(neighbors of entity 1, neighbors of entity 2,, neighbors of the last entity). Length of the neighbors vector should be equal to			

sum(n.neighbors).

suitability.pred

An optional data frame in which to look for variables with which to predict. If NULL, the observations are used.

spatial.entity.pred

An optional vector indicating the spatial entity identifier (from one to the total number of entities) for predictions. If NULL, the vector spatial.entity for observations is used.

burnin The number of burnin iterations for the sampler.

mcmc The number of Gibbs iterations for the sampler. Total number of Gibbs iterations

is equal to burnin+mcmc. burnin+mcmc must be divisible by 10 and superior or

equal to 100 so that the progress bar can be displayed.

thin The thinning interval used in the simulation. The number of mcmc iterations

must be divisible by this value.

beta. start Starting values for  $\beta$  parameters of the suitability process. This can either be a

scalar or a p-length vector.

gamma.start Starting values for  $\beta$  parameters of the observability process. This can either be

a scalar or a q-length vector.

Vrho. start Positive scalar indicating the starting value for the variance of the spatial random

effects.

mubeta Means of the priors for the  $\beta$  parameters of the suitability process. mubeta must

be either a scalar or a p-length vector. If mubeta takes a scalar value, then that value will serve as the prior mean for all of the betas. The default value is set to

0 for an uninformative prior.

Vbeta Variances of the Normal priors for the  $\beta$  parameters of the suitability process.

Vbeta must be either a scalar or a p-length vector. If Vbeta takes a scalar value, then that value will serve as the prior variance for all of the betas. The default

variance is large and set to 1.0E6 for an uninformative flat prior.

mugamma Means of the Normal priors for the  $\gamma$  parameters of the observability process.

mugamma must be either a scalar or a p-length vector. If mugamma takes a scalar value, then that value will serve as the prior mean for all of the gammas. The

default value is set to 0 for an uninformative prior.

Vgamma Variances of the Normal priors for the  $\gamma$  parameters of the observability process.

Vgamma must be either a scalar or a p-length vector. If Vgamma takes a scalar value, then that value will serve as the prior variance for all of the gammas. The

default variance is large and set to 1.0E6 for an uninformative flat prior.

priorVrho Type of prior for the variance of the spatial random effects. Can be set to a fixed

positive scalar, or to an inverse-gamma distribution ("1/Gamma") with parameters shape and rate, or to a uniform distribution ("Uniform") on the interval

[0,Vrho.max]. Default set to "1/Gamma".

shape The shape parameter for the Gamma prior on the precision of the spatial random

effects. Default value is shape=0.05 for uninformative prior.

rate The rate (1/scale) parameter for the Gamma prior on the precision of the spatial

random effects. Default value is rate=0.0005 for uninformative prior.

Vrho.max Upper bound for the uniform prior of the spatial random effect variance. Default

set to 1000.

seed The seed for the random number generator. Default set to 1234.

verbose A switch (0,1) which determines whether or not the progress of the sampler is

printed to the screen. Default is 1: a progress bar is printed, indicating the step

(in %) reached by the Gibbs sampler.

save.rho A switch (0,1) which determines whether or not the sampled values for rhos

are saved. Default is 0: the posterior mean is computed and returned in the rho.pred vector. Be careful, setting save.rho to 1 might require a large amount

of memory.

save.p A switch (0,1) which determines whether or not the sampled values for predic-

tions are saved. Default is 0: the posterior mean is computed and returned in the prob.p.pred vector. Be careful, setting save.p to 1 might require a large

amount of memory.

#### **Details**

The model integrates two processes, an ecological process associated to the presence or absence of the species due to habitat suitability and an observation process that takes into account the fact that the probability of detection of the species is inferior to one. The ecological process includes an intrinsic conditional autoregressive model (iCAR) model for spatial autocorrelation between observations, assuming that the probability of presence of the species at one site depends on the probability of presence of the species on neighboring sites.

# **Ecological process:**

$$z_i \sim \mathcal{B}ernoulli(\theta_i)$$

$$logit(\theta_i) = X_i\beta + \rho_{i(i)}$$

 $\rho_i$ : spatial random effect

j(i): index of the spatial entity for observation i.

# **Spatial autocorrelation:**

An intrinsic conditional autoregressive model (iCAR) is assumed:

$$\rho_j \sim \mathcal{N}ormal(\mu_j, V_\rho/n_j)$$

 $\mu_j$ : mean of  $\rho_{j'}$  in the neighborhood of j.

 $V_{\rho}$ : variance of the spatial random effects.

 $n_j$ : number of neighbors for spatial entity j.

#### **Observation process:**

$$y_i \sim \mathcal{B}inomial(z_i * \delta_i, t_i)$$

$$logit(\delta_i) = W_i \gamma$$

# Value

mcmc

An meme object that contains the posterior sample. This object can be summarized by functions provided by the coda package. The posterior sample of the deviance D, with  $D = -2\log(\prod_i P(y_i, z_i|...))$ , is also provided.

rho.pred If save.rho is set to 0 (default), rho.pred is the predictive posterior mean of the spatial random effect associated to each spatial entity. If save.rho is set to 1, rho.pred is an mcmc object with sampled values for each spatial random effect associated to each spatial entity.

prob.p.pred If save.p is set to 0 (default), prob.p.pred is the predictive posterior mean of the probability associated to the suitability process for each prediction. If save.p is set to 1, prob.p.pred is an mcmc object with sampled values of the probability associated to the suitability process for each prediction.

prob.p.latent Predictive posterior mean of the probability associated to the suitability process for each observation.

Prod.q.latent Predictive posterior mean of the probability associated to the observability pro-

#### Author(s)

Ghislain Vieilledent <ghislain.vieilledent@cirad.fr>

cess for each observation.

#### References

Flores, O.; Rossi, V. and Mortier, F. (2009) Autocorrelation offsets zero-inflation in models of tropical saplings density. *Ecological Modelling*, 220, 1797-1809.

Gelfand, A. E.; Schmidt, A. M.; Wu, S.; Silander, J. A.; Latimer, A. and Rebelo, A. G. (2005) Modelling species diversity through species level hierarchical modelling. *Applied Statistics*, 54, 1-20.

Latimer, A. M.; Wu, S. S.; Gelfand, A. E. and Silander, J. A. (2006) Building statistical models to analyze species distributions. *Ecological Applications*, 16, 33-50.

#### See Also

plot.mcmc, summary.mcmc

# **Examples**

```
#== Data simulation
# Set seed for repeatability
seed <- 1234
# Target parameters
beta.target <- matrix(c(0.2,0.5,0.5),ncol=1)
gamma.target <- matrix(c(1),ncol=1)</pre>
## Uncomment if you want covariates on the observability process
## gamma.target <- matrix(c(0.2,0.5,0.5),ncol=1)</pre>
Vrho.target <- 1 # Spatial Variance</pre>
# Landscape
Landscape <- raster(ncol=20,nrow=20,crs='+proj=utm +zone=1')</pre>
ncell <- ncell(Landscape)</pre>
# Neighbors
neighbors.mat <- adjacent(Landscape, cells=c(1:ncell), directions=8, pairs=TRUE, sorted=TRUE)</pre>
n.neighbors <- as.data.frame(table(as.factor(neighbors.mat[,1])))[,2]</pre>
adj <- neighbors.mat[,2]</pre>
# Generate symmetric adjacency matrix, A
A <- matrix(0,ncell,ncell)
index.start <- 1</pre>
for (i in 1:ncell) {
    index.end <- index.start+n.neighbors[i]-1</pre>
    A[i,adj[c(index.start:index.end)]] <- 1
    index.start <- index.end+1</pre>
}
# Spatial effects
d <- 1 \# Spatial dependence parameter = 1 for intrinsic CAR
Q <- diag(n.neighbors)-d*A + diag(.0001,ncell) # Add small constant to make Q non-singular
covrho <- Vrho.target*solve(Q) # Covariance of rhos</pre>
set.seed(seed)
rho <- c(rmvnorm(1,sigma=covrho)) # Spatial Random Effects</pre>
rho <- rho-mean(rho) # Centering rhos on zero</pre>
# Visited cells
n.visited <- 150 # Compare with 400, 350 and 100 for example
set.seed(seed)
visited.cells <- sort(sample(1:ncell,n.visited,replace=FALSE)) # Draw visited cells at random
notvisited.cells <- c(1:ncell)[-visited.cells]</pre>
# Number of observations
nobs <- 300
# Cell vector
set.seed(seed)
cells <- c(visited.cells,sample(visited.cells,nobs-n.visited,replace=TRUE))</pre>
coords <- xyFromCell(Landscape,cells) # Get coordinates</pre>
# Covariates for "suitability" process
```

```
set.seed(seed)
X1.cell <- rnorm(n=ncell,0,1)</pre>
set.seed(2*seed)
X2.cell <- rnorm(n=ncell,0,1)</pre>
X1 <- X1.cell[cells]</pre>
X2 <- X2.cell[cells]</pre>
X <- cbind(rep(1,nobs),X1,X2)</pre>
# Alteration
U <- runif(n=nobs,min=0,max=1)
# Covariates for "abundance" process
W <- cbind(rep(1,nobs))</pre>
## Uncomment if you want covariates on the observability process
## set.seed(3*seed)
## W1 <- rnorm(n=nobs,0,1)
## set.seed(4*seed)
## W2 <- rnorm(n=nobs,0,1)
## W <- cbind(rep(1,nobs),W1,W2)
#== Simulating latent variables
# Suitability
logit.theta <- vector()</pre>
for (n in 1:nobs) {
  logit.theta[n] <- X[n,]%*%beta.target+rho[cells[n]]</pre>
theta <- inv.logit(logit.theta)</pre>
set.seed(seed)
y.1 <- rbinom(nobs,1,theta)
# Alteration
u <- rbinom(nobs,1,U)</pre>
# Abundance
set.seed(seed)
log.lambda <- W %*% gamma.target</pre>
lambda <- exp(log.lambda)</pre>
set.seed(seed)
y.2 <- rpois(nobs,lambda)
#== Simulating response variable
Y \leftarrow y.2*(1-u)*y.1
#== Data-set
Data <- data.frame(Y,cells,X1,X2,U)</pre>
## Uncomment if you want covariates on the observability process
## Data <- data.frame(Y,cells,X1,X2,W1,W2,U)</pre>
Data <- SpatialPointsDataFrame(coords=coords,data=Data)</pre>
plot(Data)
#== Data-set for predictions (suitability on each spatial cell)
Data.pred <- data.frame(X1=X1.cell, X2=X2.cell, cells=c(1:ncell))</pre>
```

```
#== Site-occupancy model
mod.hSDM.ZIP.iCAR.alteration <- hSDM.ZIP.iCAR.alteration(counts=Data$Y,</pre>
                                                suitability=~X1+X2,
                                                 abundance=~1,
                                                 spatial.entity=Data$cells,
                                                 alteration=Data$U,
                                                 data=Data,
                                                n.neighbors=n.neighbors,
                                                 neighbors=adj,
                                                 ## suitability.pred=NULL,
                                                 ## spatial.entity.pred=NULL,
                                                 suitability.pred=Data.pred,
                                                 spatial.entity.pred=Data.pred$cells,
                                                 burnin=5000, mcmc=5000, thin=5,
                                                beta.start=0,
                                                 gamma.start=0,
                                                 Vrho.start=10,
                                                 priorVrho="1/Gamma",
                                                 #priorVrho="Uniform",
                                                 #priorVrho=10,
                                                 mubeta=0, Vbeta=1.0E6,
                                                 mugamma=0, Vgamma=1.0E6,
                                                 shape=0.5, rate=0.0005,
                                                 #Vrho.max=1000,
                                                 seed=1234, verbose=1,
                                                 save.rho=1, save.p=0)
#======
#== Outputs
#= Parameter estimates
summary(mod.hSDM.ZIP.iCAR.alteration$mcmc)
#= MCMC and posteriors
pdf(file="Posteriors_hSDM.ZIP.iCAR.alteration.pdf")
plot(mod.hSDM.ZIP.iCAR.alteration$mcmc)
dev.off()
pdf(file="Posteriors.rho_hSDM.ZIP.iCAR.alteration.pdf")
plot(mod.hSDM.ZIP.iCAR.alteration$rho.pred)
dev.off()
#= Summary plots
# rho
r.rho <- r.rho.pred <- r.visited <- Landscape</pre>
r.rho[] <- rho
rho.pred <- apply(mod.hSDM.ZIP.iCAR.alteration$rho.pred,2,mean)</pre>
r.rho.pred[] <- rho.pred</pre>
r.visited[] <- 0
```

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```
r.visited[visited.cells] <- tapply(Data$Y,Data$cells,mean)</pre>
# prob.p
r.prob.p <- Landscape</pre>
r.prob.p[] <- mod.hSDM.ZIP.iCAR.alteration$prob.p.pred</pre>
pdf(file="Summary_hSDM.ZIP.iCAR.alteration.pdf")
par(mfrow=c(3,2))
plot(r.rho, main="rho target")
plot(r.visited,main="Visited cells and counts")
plot(Data,add=TRUE,pch=16,cex=0.5)
plot(r.rho.pred, main="rho estimated")
plot(rho[visited.cells], rho.pred[visited.cells],
     xlab="rho target",
     ylab="rho estimated")
points(rho[notvisited.cells],rho.pred[notvisited.cells],pch=16,col="blue")
legend(x=-4,y=3.5,legend="Unvisited cells",col="blue",pch=16,bty="n")
abline(a=0,b=1,col="red")
plot(r.prob.p,main="Predicted counts")
plot(Data,add=TRUE,pch=16,cex=0.5)
dev.off()
## End(Not run)
```

logit

Generalized logit and inverse logit function

## **Description**

Compute generalized logit and generalized inverse logit functions.

# Usage

```
logit(x, min = 0, max = 1)
inv.logit(x, min = 0, max = 1)
```

## **Arguments**

X	value(s) to be transformed
min	Lower end of logit interval
max	Upper end of logit interval

#### **Details**

The generalized logit function takes values on [min, max] and transforms them to span [-Inf,Inf] it is defined as:

$$y = log(\frac{p}{(1-p)})$$

where

$$p = \frac{(x - min)}{(max - min)}$$

The generized inverse logit function provides the inverse transformation:

$$x = p'(max - min) + min$$

where

$$p' = \frac{exp(y)}{(1 + exp(y))}$$

## Value

Transformed value(s).

## Author(s)

Gregory R. Warnes <greg@warnes.net>

# **Examples**

```
## Not run:
    x <- seq(0,10, by=0.25)
    xt <- logit(x, min=0, max=10)
    cbind(x,xt)

y <- inv.logit(xt, min=0, max=10)
    cbind(x,xt,y)

## End(Not run)</pre>
```

neighbors.Latimer2006 Neighborhood data (from Latimer et al. 2006)

# **Description**

Data come from a small region including 476 one minute by one minute grid cells. This region is is a small corner of South Africa's Cape Floristic Region, and includes very high plant species diversity and a World Biosphere Reserve. The data frame can be used as an example for several functions in the hSDM package.

## Usage

```
neighbors.Latimer2006
```

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## **Format**

neighbors.Latimer2006 is a vector of 3542 integers indicating the neighbors (adjacent cells) of each spatial cell. The vector is of the form c(neighbors of cell 1, neighbors of cell 2, ..., neighbors of the last cell).

#### Source

Latimer et al. (2006) Ecological Applications, Appendix B

#### References

Latimer, A. M.; Wu, S. S.; Gelfand, A. E. and Silander, J. A. (2006) Building statistical models to analyze species distributions. *Ecological Applications*, 16, 33-50.

punc10

Occurrence data for Protea punctata Meisn. in the Cap Floristic Region

# **Description**

The species data were collected by the Protea Atlas Project of South Africa's National Botanical Institute.

# Usage

punc10

## **Format**

cfr. env is a data frame with 2934 presence-absence observation points.

Occurrence presence (1) or absence (0) of the species

1on longitude

lat latitude

# **Source**

Cory Merow's personal data

#### References

Latimer, A. M.; Wu, S. S.; Gelfand, A. E. and Silander, J. A. (2006) Building statistical models to analyze species distributions. *Ecological Applications*, 16, 33-50.

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