Package 'micEconCES'

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Description Tools for econometric analysis and economic modelling with the traditional two-input Constant Elasticity of Substitution (CES) function and with nested CES functions with three and four inputs. The econometric estimation can be done by the Kmenta approximation, or non-linear least-squares using various gradient-based or global optimisation algorithms. Some of these algorithms can constrain the parameters to certain ranges, e.g. economically meaningful values. Furthermore, the non-linear least-squares estimation can be combined with a grid-search for the rho-parameter(s).
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cesCalc

Calculate CES function

Description

Calculate the endogenous variable of a 'Constant Elasticity of Substitution' (CES) function.

The original CES function with two explanatory variables is

$$y = \gamma \exp(\lambda t) (\delta x_1^{-\rho} + (1 - \delta) x_2^{-\rho})^{-\frac{\nu}{\rho}}$$

and the non-nested CES function with N explanatory variables is

$$y = \gamma \exp(\lambda t) \left(\sum_{i=1}^{N} \delta_i x_i^{-\rho} \right)^{-\frac{\nu}{\rho}}$$

where in the latter case $\sum_{i=1}^{N} \delta_i = 1$.

In both cases, the elesticity of substitution is $s = \frac{1}{1+\rho}$.

The nested CES function with 3 explanatory variables proposed by Sato (1967) is

$$y = \gamma \, \exp(\lambda \, t) \, \left[\delta \, \left(\delta_1 \, x_1^{-\rho_1} + (1 - \delta_1) x_2^{-\rho_1} \right)^{\frac{\rho}{\rho_1}} + (1 - \delta) x_3^{-\rho} \right]^{-\frac{\nu}{\rho}}$$

and the *nested* CES function with 4 explanatory variables (a generalisation of the version proposed by Sato, 1967) is

$$y = \gamma \, \exp(\lambda \, t) \, \left[\delta \cdot \left(\delta_1 \, x_1^{-\rho_1} + (1 - \delta_1) x_2^{-\rho_1} \right)^{\frac{\rho}{\rho_1}} + (1 - \delta) \cdot \left(\delta_2 \, x_3^{-\rho_2} + (1 - \delta_2) x_4^{-\rho_2} \right)^{\frac{\rho}{\rho_2}} \right]^{-\frac{\nu}{\rho}}$$

Usage

cesCalc(xNames, data, coef, tName = NULL, nested = FALSE, rhoApprox = 5e-6)

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Arguments

xNames a vector of strings containing the names of the explanatory variables.

data data frame containing the explanatory variables.

coef numeric vector containing the coefficients of the CES: if the vector is unnamed,

the order of the coefficients must be γ , eventuelly λ , δ , ρ , and eventually ν in case of two expanatory variables, γ , eventuelly λ , δ_1,\ldots,δ_N , ρ , and eventually ν in case of the non-nested CES with N>2 explanatory variables, γ , eventuelly λ , δ_1 , δ , ρ_1 , ρ , and eventually ν in case of the nested CES with 3 explanatory variables, and γ , eventuelly λ , δ_1 , δ_2 , δ , ρ_1 , ρ_2 , ρ , and eventually ν in case of the nested CES with 4 explanatory variables, where in all cases the ν is only required if the model has variable returns to scale. If the vector is named, the names must be "gamma", "delta", "rho", and eventually "nu" in case of two expanatory variables, "gamma", "delta_1", …, "delta_N", "rho", and eventually "nu" in case of the non-nested CES with N>2 explanatory variables, and "gamma", "delta_1", "delta_2", "rho_1", "rho_2", "rho", and eventually "nu" in case of the nested CES with 4 explanatory variables, where the order is irrelevant in

all cases.

tName optional character string specifying the name of the time variable (t).

nested logical.; if FALSE (the default), the original CES for n inputs proposed by

Kmenta (1967) is used; if TRUE, the nested version of the CES for 3 or 4 inputs

proposed by Sato (1967) is used.

rhoApprox if the absolute value of the coefficient ρ , ρ_1 , or ρ_2 is smaller than or equal to this

argument, the endogenous variable is calculated using a first-order Taylor series approximation at the point $\rho=0$ (for non-nested CES functions) or a linear interpolation (for nested CES functions), because this avoids large numerical inaccuracies that frequently occur in calculations with non-linear CES functions

if ρ , ρ_1 , or ρ_2 have very small values (in absolute terms).

Value

A numeric vector with length equal to the number of rows of the data set specified in argument data.

Author(s)

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References

Kmenta, J. (1967): On Estimation of the CES Production Function. International Economic Review 8, p. 180-189.

Sato, K. (1967): A Two-Level Constant-Elasticity-of-Substitution Production Function. Review of Economic Studies 43, p. 201-218.

See Also

cesEst.

Examples

```
data( germanFarms, package = "micEcon" )
# output quantity:
germanFarms$qOutput <- germanFarms$vOutput / germanFarms$pOutput
# quantity of intermediate inputs
germanFarms$qVarInput <- germanFarms$vVarInput / germanFarms$pVarInput

## Estimate CES: Land & Labor with fixed returns to scale
cesLandLabor <- cesEst( "qOutput", c( "land", "qLabor" ), germanFarms )

## Calculate fitted values
cesCalc( c( "land", "qLabor" ), germanFarms, coef( cesLandLabor ) )

# variable returns to scale
cesLandLaborVrs <- cesEst( "qOutput", c( "land", "qLabor" ), germanFarms,
    vrs = TRUE )

## Calculate fitted values
cesCalc( c( "land", "qLabor" ), germanFarms, coef( cesLandLaborVrs ) )</pre>
```

cesEst

Estimate a CES function

Description

Estimate a Constant-Elasticity-of-Substitution (CES) function with two exogenous variables or a nested Constant-Elasticity-of-Substitution (CES) function proposed by Sato (1967) with three or four exogenous variables by Least Squares. The functional forms are shown in the documentation of function cesCalc.

Warning: The econometric estimation of a CES function is (almost) always very problematic, because very different parameter vectors could result in very similar values of the objective function (sum of squared residuals). Hence, even if the optimizer reports that the nonlinear minimization has converged, there might be another rather different parameter vector that results in a lower sum of squared residuals.

Usage

```
cesEst( yName, xNames, data, tName = NULL, vrs = FALSE, method = "LM",
    start = NULL, lower = NULL, upper = NULL, multErr = FALSE,
    rho1 = NULL, rho2, rho = NULL, returnGridAll = FALSE,
    returnGrad = FALSE, random.seed = 123,
    rhoApprox = c( y = 5e-6, gamma = 5e-6, delta = 5e-6,
        rho = 1e-3, nu = 5e-6 ),
    checkStart = TRUE, ... )
## S3 method for class 'cesEst'
```

```
print( x, digits = max(3, getOption("digits") - 3),
    ... )
```

Arguments

yName a string containing the name of the dependent variable.

xNames a vector of two, three or four character strings containing the names of the inde-

pendent variables.

data data frame containing the data.

tName optional character string specifying the name of the time variable (t).

vrs logical. Allow for variable returns to scale?

method character string indicationg the estimation method: either "Kmenta" for the

Kmenta approximation or "LM", "NM", "Nelder-Mead", "BFGS", "CG", "L-BFGS-B", "SANN", "Newton", "PORT", or "DE" for non-linear least-squares (see section

'Details').

start optional numeric vector giving the starting values of the parameters in the non-

linear estimations (see section 'Details').

lower lower bounds of the parameters (see section 'Details').

upper upper bounds of the parameters (see section 'Details').

multErr logical. If TRUE, the error term is assumed to be multiplicative, i.e. $y = \hat{y}$.

 $exp(\epsilon)$. If FALSE (the default), the error term is assumed to be additive, i.e.

 $y = \hat{y} + \epsilon$.

rho1, rho2, rho numeric scalar or vector at which the coefficients ρ_1 , ρ_2 , and/or ρ should be

fixed; if argument rho1, rho2, or rho is NULL (default), this coefficient is estimated together with the other parameters; if these arguments have more than one element, a grid search for ρ_1 , ρ_2 , and/or ρ is performed (see section 'Details').

returnGridAll logical value that indicates whether the estimates for all values of ρ obtained dur-

ing the grid search (not just the estimations with the 'best' ρ) should be returned

(ignored if argument rho is NULL or has only a single element).

returnGrad logical value that indicates whether a matrix with the gradients of the dependent

variable (i.e., y if argument multErr is FALSE and $\log(y)$ if argument multErr is TRUE) with respect to the parameters (evaluated at the estimated parameters)

should be returned.

random. seed an integer used to seed R's random number generator. This is to ensure replica-

bility when the "SANN" or "DE" method is used. Defaults to 123.

rhoApprox numeric vector with exactly 5 elements; the endogenous variable of the CES and

the derivatives with respect to its coefficients are calculated using a first-order Taylor series approximation at $\rho=0$ (non-nested CES) or by interpolation between ρ , ρ_1 , or ρ_2 equal to zero and ρ , ρ_1 , or ρ_2 equal to \pm rhoApprox (nested CES), if the absolute value of the coefficients ρ , ρ_1 , or ρ_2 is smaller than or equal to the corresponding element of this argument (see also argument rhoApprox of cesCalc); the first element determines the threshold for calculating the endogenous variable; the second element determines the threshold for calculating the derivatives with respect to γ ; the third element determines the threshold for

calculating the derivatives with respect to δ_1 , δ_2 , and δ ; the fourth element determines the threshold for calculating the derivatives with respect to ρ , ρ_1 , and ρ_2 ; the fifth element determines the threshold for calculating the derivatives with

respect to ν .

checkStart logical. If TRUE (the default), it is checked whether the starting values are in the

expected ranges for a production function.

x an object of class cesEst.

digits number of digits.

... further arguments to cesEst are passed to optim, nls.lm, nlm, nlminb, or

DEoptim; further arguments to print.cesEst are currently ignored.

Details

Estimation method

Argument method determines the estimation method. If it is "Kmenta", the CES is estimated by ordinary least squares using the Kmenta approximation; otherwise, it is estimated by non-linear least-squares. Several different optimizers can be used for the non-linear estimation. The optimization method LM (Levenberg-Marquardt, see Moré 1978) uses nls.lm for the optimization. The optimization methods NM or Nelder-Mead (Nelder and Mead 1965), BFGS (Broyden 1970, Fletcher 1970, Goldfarb 1970, Shanno 1970), CG (Conjugate Gradients based on Fletcher and Reeves 1964), L-BFGS-B (with box-constraints, Byrd, Lu, Nocedal, and Zhu 1995), and SANN (Simulated Annealing, Bélisle 1992) use optim for the optimization. The optimization method Newton (Newton-type, see Dennis and Schnabel 1983 and Schnabel, Koontz, and Weiss 1985) uses nlm for the optimization. The optimization method PORT (PORT routines, see Gay 1990) uses nlminb for the optimization. The optimization method DE (Differential Evolution, see Storn and Price 1997) uses DEoptim for the optimization. Analytical gradients are used in the LM, BFGS, CG, L-BFGS-B, Newton, and PORT method.

Starting values

Argument start should be a numeric vector. The order must be as described in the documentation of argument coef of function cesCalc. However, names of the elements are ignored. If argument start is NULL, pre-defined starting values are used. The starting value of λ (if present) is set to 0.015; the starting values of δ_1 , δ_2 , and δ (if present) are set to 0.5, the starting values of ρ_1 , ρ_2 , and ρ (if present and required) are set to 0.25 (i.e.\ elasticity of substitution = 0.8 in the two-input case), the starting value of ν (if present) is set to 1, and the starting value of γ is set to a value so that the mean of the error term is zero. Hence, in case of an additive error term (i.e. argument multErr is set to FALSE, the default) γ is set to mean(y) / mean(CES(X,start1)) and in case of a multiplicative error term (i.e. argument multErr is set to TRUE) γ is set to mean(log(y)) -mean(log(CES(X,start1))), where y is the dependent variable (defined by argument yName), X is the set of covariates (defined by arguments xNames and tName), CES() defines the (nested) CES function, and start1 is a coefficient vector with $\gamma=1$ and all other coefficients having the starting values described above.

Lower and upper bounds

Arguments lower and upper can be used to set lower and upper bounds for the estimated parameters. If these arguments are -Inf and Inf, respectively, the parameters are estimated without unconstraints. By default, arguments lower and upper are both NULL, which means that the bounds

are set automatically depending on the estimation method: In case of the L-BFGS-B, PORT, and DE method, the lower bound is 0 for γ , δ_1 , δ_2 , and δ (if present), -1 for ρ_1 , ρ_2 , and ρ (if present), and eventually 0 for ν . In case of the L-BFGS-B and PORT method, the upper bound is infinity for γ , 1 for δ_1 , δ_2 , and δ (if present), infinity for ρ_1 , ρ_2 , and ρ (if present), and eventually infinity for ν . Since the 'Differential Evulation' algorithm requires finit bounds, the upper bounds for the DE method are set to 1e10 for γ , 1 for δ_1 , δ_2 , and δ (if present), 10 for ρ_1 , ρ_2 , and ρ (if present), and eventually 10 for ν . In case of all other estimation methods, the lower and upper bounds are set to -Inf and Inf, respectively, because these methods do not support parameter constraints. Of course, the user can specify own lower and upper bounds by setting arguments lower and upper to numeric vectors that should have the same format as argument start (see above).

Grid search for ρ

If arguments rho1, rho2, and/or rho have more than one element, a one-dimensional, two-dimensional, or three-dimensionsl grid search for ρ_1 , ρ_2 , and/or ρ is performed. The remaining (free) parameters of the CES are estimated by least-squares, where ρ_1 , ρ_2 , and/or ρ are fixed consecutively at each value defined in arguments rho1, rho2, and rho, respectively. Finally the estimation with the ρ_1 , ρ_2 , and/or ρ that results in the smallest sum of squared residuals is chosen (and returned).

Random numbers

The 'state' (or 'seed') of R's random number generator is saved at the beginning of the cesEst function and restored at the end of this function so that this function does *not* affect the generation of random numbers although the random seed is set to argument random. seed and the 'SANN' and 'DE' algorithms use random numbers.

Value

cesEst returns a list of class cesEst that has following components:

coefficients estimated coefficients/parameters of the CES (including a possible fixed ρ).

ela constant elasticity/elasticities of substitution.

iter number of iterations (only for non-linear least-squares estimations).

convergence logical value indicating if the non-linear estimation has converged (only for non-

linear least-squares estimations with solvers that have a convergence criterion).

message additional information from the optimizer (only if a message was returned by

optim or nls.lm.

vcov approximate covariance matrix of the estimated parameters calculated from the

parameters of the linearized model by the Delta method (only if argument method

is "Kmenta").

cov.unscaled unscaled covariance matrix of the estimated parameters (including a possible

fixed ρ), i.e. the inverse of the cross-product of the gradient matrix evaluated at

the estimated parameters.

fitted.values the fitted values (\hat{y}).

residuals the residuals (i.e. $y - \hat{y}$ if argument multErr is FALSE (the default), and log(y) –

 $log(\hat{y})$ if argument multErr is TRUE).

rss the sum of the squared residuals (i.e. the value of the objective function of the

non-linear least-squares estimation evaluated at the estimated parameters).

call the matched call.
method argument method.
multErr argument multErr.

start starting values for the non-linear estimation (not for the Kmenta and DE method).

lower lower bounds of the parameters.

upper upper bounds of the parameters.

rho argument rho.

nls.lm object returned by nls.lm (only if argument method is "LM").

optim object returned by optim (only if argument method is "NM", "Nelder-Mead",

"BFGS", "CG", "L-BFGS-B", or "SANN")).

nlm object returned by nlm (only if argument method is "Newton").

nlminb object returned by nlminb (only if argument method is "PORT").

DEoptim object returned by DEoptim (only if argument method is "DE").

translog estimation results of the (unrestricted) translog model returned by translogEst

(only if argument method is "Kmenta").

kmenta estimation results of the Kmenta approximation (a restricted translog model)

returned by systemfit (only if argument method is "Kmenta").

testKmenta test of the restrictions implied by the Kmenta approximation (including constant

returns to scale if argument vrs is FALSE) in the unrestricted translog model returned by linear.hypothesis (only if argument method is "Kmenta").

allRhoSum data frame with summary results of the estimations with all values of ρ used in

the grid search (only if a grid search was performed); this data frame has follwing columns: rho = the value of ρ , rss = the corresponding sum of squared residuals, and (if appropriate for the method used for the estimation) convergence

= logical value indicating whether the estimation converged.

allRhoFull list of estimation results returned by cesEst for all values of ρ used in the grid

search (only if a grid search was performed and argument returnGridAll is set

to TRUE).

rho1Values, rho2Values, rhoValues

numeric vectors giving the values that are used in the grid search for the coeffi-

cients ρ_1 and ρ , respectively (only if a grid search was performed).

rssArray matrix or array of the RSS values obtained by a two-dimensional or three-

dimensional grid search for the coefficients ρ_1 (first dimension, e.g. rows of a matrix), ρ_2 , and ρ (last dimension, e.g. columns of a matrix) (only if a two-

dimensional or threedimensional grid search was performed).

grad matrix with the gradients of the dependent variable (i.e., y if argument multErr

is FALSE and $\log(y)$ if argument multErr is TRUE) with respect to the parameters evaluated at the estimated parameters (only if argument returnGrad is set to

TRUE).

Author(s)

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References

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Broyden, C.G. (1970): The Convergence of a Class of Double-rank Minimization Algorithms, Journal of the Institute of Mathematics and Its Applications 6, p. 76-90.

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Moré, J.J. (1978): The Levenberg-Marquardt algorithm: implementation and theory, in G.A. Watson (Ed.), Lecture Notes in Mathematics 630: Numerical Analysis, pp. 105-116, Springer-Verlag: Berlin.

Nelder, J.A. and Mead, R. (1965): A simplex algorithm for function minimization, Computer Journal 7, p. 308-313.

Schnabel, R.B., Koontz, J.E. and Weiss, B.E. (1985): A modular system of algorithms for unconstrained minimization, ACM Trans. Math. Software, 11, pp. 419-440.

Shanno, D.F. (1970): Conditioning of Quasi-Newton Methods for Function Minimization, Mathematics of Computation 24, p. 647-656.

Storn, R. and Price, K. (1997): Differential Evolution - A Simple and Efficient Heuristic for Global Optimization over Continuous Spaces, Journal of Global Optimization, 11(4), p. 341-359.

See Also

summary.cesEst for the summary method, plot.cesEst for plotting the results of the grid search for ρ , coef.cesEst for several further methods, cesCalc for calculations or simulations with the CES, translogEst for estimating translog functions, and quadFuncEst for estimating quadratic functions.

```
data( germanFarms, package = "micEcon" )
# output quantity:
germanFarms$qOutput <- germanFarms$vOutput / germanFarms$pOutput
# quantity of intermediate inputs
germanFarms$qVarInput <- germanFarms$vVarInput / germanFarms$pVarInput</pre>
```

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```
## CES: Land & Labor (Levenberg-Marquardt algorithm)
cesLandLabor <- cesEst( "qOutput", c( "land", "qLabor" ), germanFarms )</pre>
# variable returns to scale, increased max. number of iter. (LM algorithm)
cesLandLaborVrs <- cesEst( "qOutput", c( "land", "qLabor" ), germanFarms,</pre>
  vrs = TRUE, control = nls.lm.control( maxiter = 1000 ) )
# using the Nelder-Mead optimization method
cesLandLaborNm <- cesEst( "qOutput", c( "land", "qLabor" ), germanFarms,</pre>
   method = "NM" )
# using the BFGS optimization method
cesLandLaborBfgs <- cesEst( "qOutput", c( "land", "qLabor" ), germanFarms,</pre>
   method = "BFGS" )
# using the L-BFGS-B optimization method with constrained parameters
cesLandLaborBfgsCon <- cesEst( "qOutput", c( "land", "qLabor" ),</pre>
   germanFarms, method = "L-BFGS-B" )
# using the CG optimization method
cesLandLaborSann <- cesEst( "qOutput", c( "land", "qLabor" ), germanFarms,</pre>
   method = "CG" )
# using the SANN optimization method
# (with decreased number of iteration to decrease execution time)
cesLandLaborSann <- cesEst( "qOutput", c( "land", "qLabor" ), germanFarms,</pre>
   method = "SANN", control = list( maxit = 1000 ) )
# using the Kmenta approximation
cesLandLaborKmenta <- cesEst( "qOutput", c( "land", "qLabor" ), germanFarms,</pre>
   method = "Kmenta" )
# using the PORT optimization routine with unconstrained parameters
cesLandLaborPortCon <- cesEst( "qOutput", c( "land", "qLabor" ),</pre>
   germanFarms, vrs = TRUE, method = "PORT", lower = -Inf, upper = Inf )
# using the PORT optimization routine with constrained parameters and VRS
cesLandLaborPortCon <- cesEst( "qOutput", c( "land", "qLabor" ),</pre>
   germanFarms, vrs = TRUE, method = "PORT" )
# using the Differential Evolution optimization method
# (with decreased number of iteration to decrease execution time)
cesLandLaborDe <- cesEst( "qOutput", c( "land", "qLabor" ), germanFarms,</pre>
   method = "DE", control = DEoptim.control( itermax = 50 ) )
## estimation with a grid search for rho (using the LM algorithm)
cesLandInt <- cesEst( "qOutput", c( "land", "qLabor" ),</pre>
   data = germanFarms, rho = seq( from = -0.6, to = 0.9, by = 0.3 ) )
```

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Description

Methods for Objects of Class cesEst and cesEst.

Usage

```
## S3 method for class 'cesEst'
coef( object, ... )
## S3 method for class 'summary.cesEst'
coef( object, ... )
## S3 method for class 'cesEst'
fitted( object, ... )
## S3 method for class 'cesEst'
residuals( object, ... )
## S3 method for class 'cesEst'
vcov( object, ... )
```

Arguments

```
object an object of class cesEst or summary.cesEst.
... further arguments are currently ignored.
```

Value

coef.cesEst returns a vector of the estimated coefficients.

coef.summary.cesEst returns a matrix with four columns: the estimated coefficients/parameters of the CES, their standard errors, the t-statistic, and corresponding (two-sided) P-values.

fitted.cesEst returns a vector of the fitted values.

residuals.cesEst returns a vector of the residuals.

vcov.cesEst returns the variance covariance matrix of the estimated coefficients.

Author(s)

Arne Henningsen and Geraldine Henningsen

See Also

```
cesEst and summary.cesEst.
```

```
data( germanFarms, package = "micEcon" )
# output quantity:
germanFarms$qOutput <- germanFarms$vOutput / germanFarms$pOutput
# quantity of intermediate inputs
germanFarms$qVarInput <- germanFarms$vVarInput / germanFarms$pVarInput
## CES: Land & Labor</pre>
```

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```
cesLandLabor <- cesEst( "qOutput", c( "land", "qLabor" ), germanFarms )
# estimated coefficients
coef( cesLandLabor )
# estimated coefficients, their standard errors, t-statistic, P-values
coef( summary( cesLandLabor ) )
# fitted values of the estimated model
fitted( cesLandLabor )
# residuals of the estimated model
residuals( cesLandLabor )
# covariance matrix of the estimated coefficients
vcov( cesLandLabor )</pre>
```

durbinWatsonTest.cesEst

Durbin Watson Test for Estimated CES Functions

Description

Conduct a generalized Durbin-Watson-Test as suggested by White (1992) to test for serial correlation of the residuals. dwt is an abbreviation for durbinWatsonTest.

Usage

```
## S3 method for class 'cesEst'
durbinWatsonTest( model, ... )
```

Arguments

model object returned by cesEst; in the call to cesEst, argument returnGrad must be set to TRUE.further arguments are passed to durbinWatsonTest.lm.

Author(s)

Arne Henningsen

References

White, K.J. (1992): The Durbin-Watson Test for Autocorrelation in Nonlinear Models. The Review of Economics and Statistics 74(2), p. 370-373.

See Also

cesEst, durbinWatsonTest.

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Examples

GermanIndustry

Aggregated Time Series Data for the West German Industry

Description

The data frame GermanIndustry contains annual aggregated data of the entire West German industry from 1960 until 1993 as well as data of seven industrial sectors from 1970 to 1988/1992. This data set has been used by Kemfert (1998).

Usage

```
data(GermanIndustry)
```

Format

This data frame contains the following columns/variables:

year the year.

- Y output: gross value added of the West German industrial sector (in billion Deutsche Mark at prices of 1991).
- **K** capital: gross stock of fixed assets of the West German industrial sector (in billion Deutsche Mark at prices of 1991).
- A labor: total number of persons employed in the West German industrial sector (in million).
- **E** energy: final energy consumption in the West German industrial sector (in GWh).
- **C_Y** gross value added of the West German chemical industry (in billion Deutsche Mark at prices of 1991).
- C_K capital: gross stock of fixed assets of the West German chemical industry (in billion Deutsche Mark at prices of 1991).
- C_A labor: total number of persons employed in the West German chemical industry (in thouands).
- **C_E** final energy consumption in the West German chemical industry (in GWh).

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S_Y gross value added of the West German stone and earth industry (in billion Deutsche Mark at prices of 1991).

- **S_K** capital: gross stock of fixed assets of the West German stone and earth industry (in billion Deutsche Mark at prices of 1991).
- **S_A** labor: total number of persons employed in the West German stone and earth industry (in thouands).
- **S_E** final energy consumption in the West German stone and earth industry (in GWh).
- **I_Y** gross value added of the West German iron industry (in billion Deutsche Mark at prices of 1991).
- **I_K** capital: gross stock of fixed assets of the West German iron industry (in billion Deutsche Mark at prices of 1991).
- **I_A** labor: total number of persons employed in the West German iron industry (in thouands).
- **I_E** final energy consumption in the West German iron industry (in GWh).
- **N_Y** gross value added of the West German non-ferrous industry (in billion Deutsche Mark at prices of 1991).
- **N_K** capital: gross stock of fixed assets of the West German non-ferrous industry (in billion Deutsche Mark at prices of 1991).
- N_A labor: total number of persons employed in the West German non-ferrous industry (in thouands).
- **N_E** final energy consumption in the West German non-ferrous industry (in GWh).
- V_Y gross value added of the West German vehicle industry (in billion Deutsche Mark at prices of 1991).
- V_K capital: gross stock of fixed assets of the West German vehicle industry (in billion Deutsche Mark at prices of 1991).
- V_A labor: total number of persons employed in the West German vehicle industry (in thouands).
- **V_E** final energy consumption in the West German vehicle industry (in GWh).
- **P_Y** gross value added of the West German paper industry (in billion Deutsche Mark at prices of 1991).
- **P_K** capital: gross stock of fixed assets of the West German paper industry (in billion Deutsche Mark at prices of 1991).
- **P** A labor: total number of persons employed in the West German paper industry (in thouands).
- **P_E** final energy consumption in the West German paper industry (in GWh).
- **F_Y** gross value added of the West German food industry (in billion Deutsche Mark at prices of 1991).
- **F_K** capital: gross stock of fixed assets of the West German food industry (in billion Deutsche Mark at prices of 1991).
- **F_A** labor: total number of persons employed in the West German food industry (in thouands).
- **F_E** final energy consumption in the West German food industry (in GWh).

Note

Please note that Kemfert (1998) disregards the years 1973-1975 in her estimations due to economic disruptions.

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Source

German Federal Statistical Office (Statistisches Bundesamt), data taken from Kemfert (1998).

References

Kemfert, Claudia (1998): Estimated Substitution Elasticities of a Nested CES Production Funktion Approach for Germany, Energy Economics 20: 249-264 (doi:10.1016/S0140-9883(97)00014-5)

MishraCES

Mishra's (2006) CES data

Description

The MishraCES data set contains artificial production data. It has 50 observations (e.g. firms, sectors, or countries).

Usage

```
data(MishraCES)
```

Format

This data frame contains the following columns:

- No Firm number.
- Y Output quantity.
- X1 Quantity of first input.
- X2 Quantity of second input.
- X3 Quantity of third input.
- **X4** Quantity of fouth input.

Source

Mishra, SK (2006): A Note on Numerical Estimation of Sato's Two-Level CES Production Function MPRA Working Paper No. 1019, https://mpra.ub.uni-muenchen.de/1019/.

```
# load the data set
data( "MishraCES" )

# show mean values of all variables
colMeans( MishraCES )

# re-calculate the endogenous variable (see Mishra 2006)
# coefficients of the nested CES function with 4 inputs
b <- c( "gamma" = 200 * 0.5^(1/0.6), "delta_1" = 0.6, "delta_2" = 0.3,</pre>
```

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```
"delta" = 0.5, "rho_1" = 0.5, "rho_2" = -0.17, "rho" = 0.6 )
MishraCES$Y2 <- cesCalc( xNames = c( "X1", "X2", "X3", "X4" ),
    data = MishraCES, coef = b, nested = TRUE )
all.equal( MishraCES$Y, MishraCES$Y2 )</pre>
```

plot.cesEst

Plot RSSs of a CES Function Estimated by Grid Search

Description

Plot a scatter plot, where the values of ρ are on the x axis and the corresponding sums of the squared residuals obtained by a grid search for ρ are on the y axis. Estimations that did not converge are marked with red.

Note that this method can be applied only if the model was estimated by a grid search for ρ , i.e.\ cesEst was called with argument rho set to a vector of more than one values for ρ .

Usage

```
## S3 method for class 'cesEst'
plot( x, negRss = TRUE, bw = FALSE, ... )
```

Arguments

X	object returned by cesEst if it was called with argument rho set a vector containing more than one value for ρ so that a grid search was performed.
negRss	logical. Indicates whether the <i>negative</i> sum of squared residuals should be plotted in 3D plots (ignored in 2D plots).
bw	logical. Indicates whether 3D plots should be in black-and-white or colored.
	All further arguments are passed to plot.default or persp.

Author(s)

Arne Henningsen and Geraldine Henningsen

See Also

cesEst.

```
data( germanFarms, package = "micEcon" )
# output quantity:
germanFarms$qOutput <- germanFarms$vOutput / germanFarms$pOutput
# quantity of intermediate inputs
germanFarms$qVarInput <- germanFarms$vVarInput / germanFarms$pVarInput
## CES: Land & Intermediate Inputs</pre>
```

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```
cesLandInt <- cesEst( yName = "qOutput",
    xNames = c( "land", "qVarInput" ), data = germanFarms,
    rho = seq( from = -0.6, to = 0.9, by = 0.3 ) )
# plot the rhos against the sum of squared residuals
plot( cesLandInt )</pre>
```

summary.cesEst

Summarize Estimation of a CES Function

Description

summary method for objects of class cesEst.

Usage

Arguments

object an object returned by cesEst.

rSquaredLog logical. If FALSE (the default for models with additive error term), the returned

 R^2 -value measures the fraction of the explained variance of the dependent variable in natural units. If TRUE (the default for models with multiplicative error term), the returned R^2 -value measures the fraction of the explained variance of

the logarithmized dependent variable.

ela logical. If TRUE (the default), the summary method calculates the (co)variances

of the constant elasticities of substitution and the print method prints these elasticities together with corresponding summary statistics. If FALSE, the summary method does not calculate the (co)variances of the constant elasticities of sub-

stitution and the print method does not print these elasticities.

x an object returned by summary.cesEst.

digits number of digits.

... further arguments are currently ignored.

Value

summary.cesEst returns a list of class summary.cesEst that contains the elements of the provided object with with following changes or additions:

coefficients

a matrix with four columns: the estimated coefficients/parameters of the CES (including a possible fixed ρ), their standard errors, the t-statistic, and corresponding (two-sided) P-values.

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square root of the estimated (asymptotic) variance of the random error (calcusigma lated without correcting for degrees of freedom). R^2 -value, i.e. the 'fraction of variance explained by the model'. If argument r.squared rSquaredLog is TRUE, the R^2 -value measures the fraction of the explained variance of the logarithmized dependent variable. covariance matrix of the estimated parameters (including a possible fixed ρ). vcov a matrix with four columns: the estimated elasticities of substitution, their stanela dard errors, the t-statistic, and corresponding (two-sided) P-values (only if argument ela is TRUE). covariance matrix of the estimated elasticities of substitution (only if argument elaCov ela is TRUE).

Author(s)

Arne Henningsen

See Also

cesEst and cesCalc.

```
data( germanFarms, package = "micEcon" )
# output quantity:
germanFarms$qOutput <- germanFarms$vOutput / germanFarms$pOutput
# quantity of intermediate inputs
germanFarms$qVarInput <- germanFarms$vVarInput / germanFarms$pVarInput
## CES: Land & Labor
cesLandLabor <- cesEst( "qOutput", c( "land", "qLabor" ), germanFarms )
# print summary results
summary( cesLandLabor )</pre>
```

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