# Package 'psyphy'

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Type Package

Title Functions for Analyzing Psychophysical Data in R

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<b>Description</b> An assortment of functions that could be useful in analyzing data from psychophysical experiments. It includes functions for calculating d' from several different experimental designs, links for m-alternative forced-choice (mafc) data to be used with the binomial family in glm (and possibly other contexts) and self-Start functions for estimating gamma values for CRT screen calibrations.								
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psyphy-package       2         dprime.ABX       3         dprime.mAFC       4         dprime.oddity       5         dprime.SD       6         ecc2       2         glm.lambda       8         glm.WH       10         logit.2asym       12         mafc       14								

2 dprime.ABX

psyphy-	-package	Fu	nct	ion	sf	or	an	al:	yzi	'ng	g p	sy	cŀ	hoj	ph	ıys	ic	al	fu	nc	tio	ns	,					
Index																									 			25
R S	RGB	 																							 			20 21
	orobit.lambda osyfun.2asym																											

# **Description**

An assortment of functions that could be useful in analyzing data from pyschophysical experiments. It includes functions for calculating d' from several different experimental designs, links for mafc to be used with the binomial family in glm (and possibly other contexts) and a self-Start function for estimating gamma values for CRT screen calibrations.

# **Details**

Package: psyphy
Type: Package
Version: 0.0-2
Date: 2007-01-27
License: GPL

For the moment, the package contains several functions for calculating d' for a variety of psychophysical paradigms, some link functions for the binomial family in glm (and perhaps other functions) for fitting psychometric functions from mAFC experiments and a self-Start function for estimating the value of the exponent, gamma, based on the luminance calibration of the three channels of a CRT-like display.

# Author(s)

Kenneth Knoblauch < ken.knoblauch@inserm.fr>

dprime.ABX $d'$ for ABX Paradigm
----------------------------------

# **Description**

Calulate d' for ABX paradigm either assuming a differencing strategy or independent observations

dprime.ABX 3

# Usage

```
dprime.ABX(Hits, FA, zdiff, Pc.unb, method = "diff")
```

# **Arguments**

Hits numeric in [0, 1] corresponding to Hit rate

FA numeric in [0, 1] corresponding to False alarm rate

zdiff numeric. Difference of z-scores for Hit and False Alarm rates

Pc. unb numeric in [0, 1]. Proportion correct for an unbiased observer, pnorm(zdiff) method character. Specifies the model to describe the observer's criterion for dividing up

the decision space, must be either "diff" for a differencing strategy (the default)

or "IO" for independent observations.

#### **Details**

Two different strategies have been described for how the observer partitions the decision space in the ABX paradigm, either based on Independent Observations of each stimulus or on a differencing strategy. The differencing strategy is the default. d' can be calculated either from the H and FA rates, from the difference of z-scores or from the probability correct of an unbiased observer.

# Value

Returns the value of d'

# Author(s)

Kenneth Knoblauch

#### References

MacMillan, N. A. and Creeman, C. D. (1991) *Detection Theory: A User's Guide* Cambridge University Press

Green, D. M. and Swets, J. A. (1966) *Signal Detection Theory and Psychophysics* Robert E. Krieger Publishing Company

#### See Also

```
dprime.mAFC, dprime.SD, dprime.oddity
```

```
dprime.ABX(H = 0.75, F = 0.3)
dprime.ABX(H = 0.75, F = 0.3, method = "IO")
dprime.ABX(zdiff = qnorm(0.75) - qnorm(0.3))
dprime.ABX(Pc.unb = pnorm( (qnorm(0.75) - qnorm(0.3))/2 ))
```

4 dprime.mAFC

dprime.mAFC

d' for m-alternative Forced-choice

# **Description**

Calculate the value of d' for an m-alternative forced choice paradigm

# Usage

```
dprime.mAFC(Pc, m)
```

# **Arguments**

Pc The proportion of correct responses based on either the Hit rate or based on an

unbiased observer

m The number of alternative choices, an integer > 1.

#### **Details**

The probability of a correct response in m-alternative forced-choice, assuming independence, is based on the product of the likelihoods of the signal alternative generating the strongest response and the m - 1 noise alternatives generating responses less than this value (Green and Dai, 1991). For a Yes-No paradigm, the sensitivity is calculated more simply as

$$d' = \mathsf{qnorm}(H) - \mathsf{qnorm}(F)$$

where H and F are the Hit and False Alarm rates, respectively.

#### Value

Returns the value of d'

# Note

Currently is only valid for d' in the interval [-10, 10] which should be well outside the range of sensory differences that this paradigm is used to investigate.

# Author(s)

Kenneth Knoblauch

#### References

Green, D. M. and Dai, H. (1991) Probability of being correct with 1 of M orthogonal signals. *Perception & Psychophysics*, **49**, 100–101.

Green, D. M. and Swets, J. A. (1966) *Signal Detection Theory and Psychophysics* Robert E. Krieger Publishing Company

dprime.oddity 5

# See Also

```
See Also dprime. ABX, dprime. SD, dprime.oddity
```

# **Examples**

```
dprime.mAFC(0.8, 4)
```

dprime.oddity

d' for 3 Stimulus Oddity Paradigm

# Description

Calculate d' for a 3 stimulus (triangular) paradigm. Two of the stimuli are the same and the observer must designate the stimulus that is different.

# Usage

```
dprime.oddity(Pc.tri)
```

# **Arguments**

Pc.tri

numeric in (1/3, 1). The proportion of correct responses for an unbiased observer.

# Value

Returns the value of d'

# Author(s)

Kenneth Knoblauch

# References

Frijters, G. S., Kooistra, A. and Verijken, P. F. G. (1980) Tables of d' for the triangular method and the 3-AFC signal detection procedure. *Perception & Psychophysics*, **27**, 176–178.

MacMillan, N. A. and Creeman, C. D. (1991) *Detection Theory: A User's Guide* Cambridge University Press

Green, D. M. and Swets, J. A. (1966) *Signal Detection Theory and Psychophysics* Robert E. Krieger Publishing Company

#### See Also

```
dprime.mAFC, dprime.SD, dprime.ABX
```

```
dprime.oddity(0.8)
```

6 dprime.SD

dprime.SD d'for Same-different Paradigm
---

# **Description**

Calulate d' for same-different paradigm either assuming a differencing strategy or independent observations

# Usage

```
dprime.SD(H, FA, zdiff, Pcmax, method = "diff")
```

# **Arguments**

Н	numeric in [0, 1] corresponding to Hit rate
FA	numeric in [0, 1] corresponding to False alarm rate
zdiff	numeric. Difference of z-scores for Hit and False Alarm rates ( only valid for method " ${\rm IO}$ ")
Pcmax	numeric in [0, 1]. Proportion correct for an unbiased observer, pnorm(zdiff) (only valid for method "IO").
method	character. Specifies the model to describe the observer's criterion for dividing up the decision space, must be either "diff" for a differencing strategy (the default) or "IO" for independent observations.

#### **Details**

Two different strategies have been described for how the observer partitions the decision space in the same-different paradigm. With Independent Observations, d' can be calculated either from the H and FA rates, from the difference of z-scores or from the probability correct of an unbiased observer. Only one of these three choices should be specified in the arguments. For the differencing strategy, only the first of these choices is valid.

# Value

Returns the value of d'

# Author(s)

Kenneth Knoblauch

# References

MacMillan, N. A. and Creeman, C. D. (1991) *Detection Theory: A User's Guide* Cambridge University Press

Green, D. M. and Swets, J. A. (1966) *Signal Detection Theory and Psychophysics* Robert E. Krieger Publishing Company

ecc2 7

# See Also

```
dprime.mAFC, dprime.ABX, dprime.oddity
```

# **Examples**

```
dprime.SD(H = 0.642, F = 0.3)
dprime.SD(H = 0.75, F = 0.3, method = "IO")
dprime.SD(zdiff = qnorm(0.75) - qnorm(0.3), method = "IO")
dprime.SD(Pcmax = pnorm( (qnorm(0.75) - qnorm(0.3))/2 ), method = "IO")
```

ecc2

4-afc Detection and Identification of Letters

# **Description**

Letter detection and identification at 2 degrees eccentricity in the visual field. On each trial, one of four letters (b, d, p, q) were presented in one of four positions (superior, inferior, left, right) in the visual field. In a given session, the letter height was fixed. Six contrast levels were tested in each session. The data indicate the proportion of correctly identified positions, referred to here as detection, and the proportion of correctly identified letters, conditional on correct identification.

# Usage

```
data(ecc2)
```

# **Format**

A data frame with 48 observations on the following 5 variables.

Contr numeric. The contrast of the stimulus, defined as Weberian contrast.

task a factor with levels DET ID indicating the two tasks, detection and identification.

Size a numeric vector indicating the letter height

Correct an integer vector indicating the number of correct responses (DET or ID).

Incorrect an integer vector, indicating the number of incorrect responses.

#### References

Yssaad-Fesselier, R. and Knoblauch, K. (2006) Modeling psychometric functions in R. *Behav Res Methods.*, **38(1)**, 28–41.

8 glm.lambda

# **Examples**

```
data(ecc2)
library(lattice)
xyplot(Correct/(Correct + Incorrect) ~ Contr | Size * task, ecc2,
type = "b", scale = list(x = list(log = TRUE),
y = list(limits = c(0, 1.05))),
xlab = "Contrast", ylab = "Proportion Correct Response",
panel = function(x, y, ...) {
panel.xyplot(x, y, ...)
panel.abline(h = 0.25, lty = 2)
})
```

glm.lambda

mafc Probit Fit to Psychometric Function Profiled on Upper Asymptote

# **Description**

A wrapper for glm in which the deviance for the model with binomial family and link probit.lambda is profiled as a function of lambda, the upper asymptote of the psychometric function.

# Usage

```
glm.lambda(formula, data, NumAlt = 2, lambda = seq(0, 0.1, len = 40), plot.it = FALSE, ...)
```

# **Arguments**

formula	a symbolic description of the model to be fit
data	an optional data frame, list or environment (or object coercible by as.data.frame to a data frame) containing the variables in the model. If not found in data, the variables are taken from environment(formula), typically the environment from which glm is called.
NumAlt	the number of alternatives, m in the mafe experiment from which the data arise
lambda	a sequence of values to profile for the upper asymptote of the psychometric function
plot.it	logical indicating whether to plot the profile of the deviances as a function of lambda
	further arguments passed to glm

# **Details**

The psychometric function fit to the data is described by

$$P(x) = 1/m + (1 - 1/m - \lambda)\Phi(x)$$

where m is the number of alternatives and the lower asymptote,  $1 - \lambda$  is the upper asymptote and  $\Phi$  is the cumulative normal function.

glm.lambda 9

# Value

returns an object of class 'lambda' which inherits from classes 'glm' and 'lm'. It only differs from an object of class 'glm' in including two additional components, lambda, giving the estimated minimum of the profile by fitting a quadratic to the profile and a data frame containing the profiled deviance values for each value of lambda tested. The degrees of freedom are reduced by 1 to take into account the estimation of lambda.

#### Note

If the minimum occurs outside the interval examined, an error might occur. In any case, re-running the function with a new range of lambda that includes the minimum should work. if the plotted profile indicates that the fitted quadratic does not describe well the profile at the minimum, refitting with a more restricted range of lambda is recommended.

#### Author(s)

Ken Knoblauch

#### References

Wichmann, F. A. and Hill, N. J. (2001) The psychometric function: I.Fitting, sampling, and goodness of fit. Percept Psychophys., 63(8), 1293–1313.

Yssaad-Fesselier, R. and Knoblauch, K. (2006) Modeling psychometric functions in R. *Behav Res Methods.*, **38(1)**, 28–41. (for examples with gnlr).

#### See Also

```
mafc, glm, probit.lambda, family
```

```
b <- 3.5
g <- 1/3
d <- 0.025
a <- 0.04
p <- c(a, b, g, d)
num.tr <- 160
cnt <- 10^seq(-2, -1, length = 6) # contrast levels
#simulated Weibull-Quick observer responses
set.seed(12161952)
truep \leftarrow g + (1 - g - d) * pweibull(cnt, b, a)
ny <- rbinom(length(cnt), num.tr, truep)</pre>
nn <- num.tr - ny
phat <- ny/(ny + nn)
resp.mat <- matrix(c(ny, nn), ncol = 2)
## First with upper asymptote at 1
dd.glm <- glm(resp.mat ~ cnt, family = binomial(mafc.probit(3)))</pre>
summary(dd.glm)
```

10 glm.WH

```
dd.lam <- glm.lambda(resp.mat ~ cnt, NumAlt = 3, lambda = seq(0, 0.03,
len = 100), plot.it = TRUE)
summary(dd.lam)
## can refine interval, but doesn't change result much
dd.lam2 <- glm.lambda(resp.mat ~ cnt, NumAlt = 3,</pre>
lambda = seq(dd.lam$lambda/sqrt(2), dd.lam$lambda*sqrt(2),
len = 100), plot.it = TRUE)
summary(dd.lam2)
## Compare fits w/ and w/out lambda
anova(dd.glm, dd.lam2, test = "Chisq")
plot(cnt, phat, \log = x^*, \cos = 1.5, y = c(0, 1))
pcnt <- seq(0.01, 0.1, len = 100)
lines(pcnt, predict(dd.glm, data.frame(cnt = pcnt),
                    type = "response"), lwd = 2)
lines(pcnt, predict(dd.lam, data.frame(cnt = pcnt),
                    type = "response"), lwd = 2, lty = 2)
```

glm.WH

mafc Probit Fit to Psychometric Function with Upper Asymptote Less than One

# **Description**

A probit fit of a psychometric function with upper asymptote less than 1 is obtained by cycling between a fit with glm using the probit.lambda link and optimize to estimate lambda, 1 - the upper asymptotic value, until the log Likelihood changes by less than a pre-set tolerance.

# Usage

```
glm.WH(formula, data, NumAlt = 2, lambda.init = 0.01, interval = c(0, 0.05), trace = FALSE, tol = 1e-06, ...)
```

# **Arguments**

formula	a symbolic description of the model to be fit.
data	an optional data frame, list or environment (or object coercible by as.data.frame containing the variables in the model. If not found in data, the variables are taken from the environment(formula), typically the environment from glm.WH was called.
NumAlt	integer indicating the number of alternatives (> 1) in the mafc-task. (Default: 2).
lambda.init	numeric, initial estimate of 1 - upper asymptote.
interval	numeric vector giving interval endpoints within which to search for lambda.
trace	logical, indicating whether or not to print out a trace of the iterative process.
tol	numeric, tolerance for ending iterations.
	futher arguments passed to glm.

glm.WH

# **Details**

The psychometric function fit to the data is described by

$$P(x) = 1/m + (1 - 1/m - \lambda)\Phi(x)$$

where m is the number of alternatives and the lower asymptote,  $1 - \lambda$  is the upper asymptote and  $\Phi$  is the cumulative normal function.

#### Value

returns an object of class 'lambda' which inherits from classes 'glm' and 'lm'. It only differs from an object of class 'glm' in including an additional components, lambda, giving the estimated minimum of lambda. The degrees of freedom are reduced by 1 to take into account the estimation of lambda.

# Author(s)

Ken Knoblauch

#### References

Wichmann, F. A. and Hill, N. J. (2001) The psychometric function: I.Fitting, sampling, and goodness of fit. Percept Psychophys., 63(8), 1293–1313.

Yssaad-Fesselier, R. and Knoblauch, K. (2006) Modeling psychometric functions in R. *Behav Res Methods.*, **38(1)**, 28–41. (for examples with gnlr).

# See Also

```
mafc, glm,glm.lambda, probit.lambda, family
```

```
b <- 3.5
g < -1/4
d < -0.04
a <- 0.04
p <- c(a, b, g, d)
num.tr <- 160
cnt <- 10^seq(-2, -1, length = 6) # contrast levels
#simulated Weibull-Quick observer responses
truep \leftarrow g + (1 - g - d) * pweibull(cnt, b, a)
ny <- rbinom(length(cnt), num.tr, truep)</pre>
nn <- num.tr - ny
phat <- ny/(ny + nn)
resp.mat <- matrix(c(ny, nn), ncol = 2)</pre>
tst.glm <- glm(resp.mat ~ cnt, binomial(mafc.probit(1/g)))</pre>
pcnt < - seq(0.005, 1, len = 1000)
plot(cnt, phat, log = "x", ylim = c(0, 1), xlim = c(0.005, 1),
cex = 1.75)
```

12 logit.2asym

```
lines(pcnt, predict(tst.glm, data.frame(cnt = pcnt), type = "response"), lwd = 2)
tst.lam <- glm.WH(resp.mat ~ cnt, NumAlt = 1/g, trace = TRUE)
lines(pcnt, predict(tst.lam, data.frame(cnt = pcnt),
type = "response"), lty = 2, lwd = 2)</pre>
```

logit.2asym

Links for Binomial Family with Variable Upper/Lower Asymptotes

# **Description**

These functions provide links for the binamial family so that psychometric functions can be fit with *both* the upper and lower asymptotes different from 1 and 0, respectively.

# Usage

```
logit.2asym(g, lam)
probit.2asym(g, lam)
cauchit.2asym(g, lam)
cloglog.2asym(g, lam)
weib.2asym( ... )
```

# **Arguments**

g	numeric in the range $(0, 1)$ , normally $\leq 0.5$ , however, which specifies the lower asymptote of the psychometric function.
	asymptote of the psychometric function.
lam	numeric in the range $(0, 1)$ , specifying 1 - the upper asymptote of the psychometric function.
	used just to pass along the formals of cloglog, 2asym as arguments to weib, 2asym.

# **Details**

These links are used to specify psychometric functions with the form

$$P(x) = \gamma + (1 - \gamma - \lambda)p(x)$$

where  $\gamma$  is the lower asymptote and lambda is 1- the upper asymptote, and p(x) is the base psychometric function, varying between 0 and 1.

# Value

Each link returns a list containing functions required for relating the response to the linear predictor in generalized linear models and the name of the link.

linkfun	The link function
linkinv	The inverse link function
mu.eta	The derivative of the inverse link
valideta	The domain over which the linear predictor is valid
link	A name to be used for the link

logit.2asym

#### Author(s)

Kenneth Knoblauch

#### References

Klein S. A. (2001) Measuring, estimating, and understanding the psychometric function: a commentary. *Percept Psychophys.*, **63(8)**, 1421–1455.

Wichmann, F. A. and Hill, N. J. (2001) The psychometric function: I.Fitting, sampling, and goodness of fit. *Percept Psychophys.*, **63(8)**, 1293–1313.

#### See Also

```
glm, glm make.link, psyfun.2asym
```

```
#A toy example,
b <- 3
g <- 0.05 # simulated false alarm rate
d < -0.03
a <- 0.04
p <- c(a, b, g, d)
num.tr <- 160
cnt <- 10^seq(-2, -1, length = 6) # contrast levels</pre>
#simulated Weibull-Quick observer responses
truep \leftarrow g + (1 - g - d) * pweibull(cnt, b, a)
ny <- rbinom(length(cnt), num.tr, truep)</pre>
nn <- num.tr - ny
phat <- ny/(ny + nn)
resp.mat <- matrix(c(ny, nn), ncol = 2)
ddprob.glm <- psyfun.2asym(resp.mat ~ cnt, link = probit.2asym)</pre>
ddlog.glm <- psyfun.2asym(resp.mat ~ cnt, link = logit.2asym)</pre>
# Can fit a Weibull function, but use log contrast as variable
ddweib.glm <- psyfun.2asym(resp.mat ~ log(cnt), link = weib.2asym)</pre>
ddcau.glm <- psyfun.2asym(resp.mat ~ cnt, link = cauchit.2asym)</pre>
plot(cnt, phat, log = "x", cex = 1.5, ylim = c(0, 1))
pcnt <- seq(0.01, 0.1, len = 100)
lines(pcnt, predict(ddprob.glm, data.frame(cnt = pcnt),
type = "response"), lwd = 5)
lines(pcnt, predict(ddlog.glm, data.frame(cnt = pcnt),
type = "response"), lwd = 2, lty = 2, col = "blue")
lines(pcnt, predict(ddweib.glm, data.frame(cnt = pcnt),
type = "response"), lwd = 3, col = "grey")
lines(pcnt, predict(ddcau.glm, data.frame(cnt = pcnt),
type = "response"), lwd = 3, col = "grey", lty = 2)
```

14 mafc

mafc

Links for Binomial Family for m-alternative Forced-choice

# **Description**

These provide links for the binomial family for fitting m-alternative forced-choice psychophysical functions

# Usage

```
mafc.logit( .m = 2 )
mafc.probit( .m = 2 )
mafc.cloglog( .m = 2 )
mafc.weib( ... )
mafc.cauchit( .m = 2 )
```

# **Arguments**

.m is the integer number (>1) of choices (Default to 2AFC). For m = 1 (Yes/No paradigm), use one of the built-in links for the binomial family.
... just to pass along the formals of mafc.cloglog.

#### **Details**

These functions provide links for fitting psychometric functions arising from an m-alternative forced-choice experiment. The estimated coefficients of the linear predictor influence both the location and the slope of the psychometric function(s), but provide no means of estimating the upper aymptote which is constrained to approach 1. If the upper asymptote must be estimated, it would be better to maximize directly the likelihood, either with a function like optim or gnlr from package **gnlm** (available at <a href="https://www.commanster.eu/rcode.html">https://www.commanster.eu/rcode.html</a>). Alternatively, the function probit.lambda can be used with a known upper asymptote, or glm.lambda or glm.WH to estimate one, with a probit link. mafc.weib is just an alias for mafc.cloglog.

#### Value

Each link returns a list containing functions required for relating the response to the linear predictor in generalized linear models and the name of the link.

linkfun The link function
linkinv The inverse link function
mu.eta The derivative of the inverse link
valideta The domain over which the linear predictor is valid
link A name to be used for the link

# Author(s)

Kenneth Knoblauch

mafc 15

#### References

Williams J, Ramaswamy D and Oulhaj A (2006) 10 Hz flicker improves recognition memory in older people *BMC Neurosci*. 2006 5;7:21 https://www.ncbi.nlm.nih.gov/pmc/articles/PMC1434755/ (for an example developed prior to this one, but for m = 2).

Klein S. A. (2001) Measuring, estimating, and understanding the psychometric function: a commentary. *Percept Psychophys.*, **63(8)**, 1421–1455.

Wichmann, F. A. and Hill, N. J. (2001) The psychometric function: I.Fitting, sampling, and goodness of fit. *Percept Psychophys.*, **63(8)**, 1293–1313.

Yssaad-Fesselier, R. and Knoblauch, K. (2006) Modeling psychometric functions in R. *Behav Res Methods.*, **38(1)**, 28–41. (for examples with gnlr).

#### See Also

family, make.link, glm, optim, probit.lambda, glm.lambda, glm.WH

```
#A toy example,
b < -3.5
g < -1/3
d < -0.0
a < -0.04
p < -c(a, b, g, d)
num.tr <- 160
cnt <- 10^seq(-2, -1, length = 6) # contrast levels
#simulated observer responses
truep \leftarrow g + (1 - g - d) * pweibull(cnt, b, a)
ny <- rbinom(length(cnt), num.tr, truep)</pre>
nn <- num.tr - ny
phat <- ny/(ny + nn)
resp.mat <- matrix(c(ny, nn), ncol = 2)
ddprob.glm <- glm(resp.mat ~ cnt, family = binomial(mafc.probit(3)))</pre>
ddlog.glm <- glm(resp.mat ~ cnt, family = binomial(mafc.logit(3)))</pre>
# Can fit a Weibull function, but use log contrast as variable
ddweib.glm <- glm(resp.mat ~ log(cnt), family = binomial(mafc.cloglog(3)))</pre>
ddcau.glm <- glm(resp.mat ~ log(cnt), family = binomial(mafc.cauchit(3)))</pre>
plot(cnt, phat, log = "x", cex = 1.5, ylim = c(0, 1))
pcnt <- seq(0.01, 0.1, len = 100)
lines(pcnt, predict(ddprob.glm, data.frame(cnt = pcnt),
type = "response"), lwd = 2)
lines(pcnt, predict(ddlog.glm, data.frame(cnt = pcnt),
type = "response"), lwd = 2, lty = 2)
lines(pcnt, predict(ddweib.glm, data.frame(cnt = pcnt),
type = "response"), lwd = 3, col = "grey")
lines(pcnt, predict(ddcau.glm, data.frame(cnt = pcnt),
type = "response"), lwd = 3, col = "grey", lty = 2)
```

16 probit.lambda

```
# Weibull parameters \alpha and \beta
cc <- coef(ddweib.glm)</pre>
alph \leftarrow exp(-cc[1]/cc[2])
bet <- cc[2]
#More interesting example with data from Yssaad-Fesselier and Knoblauch
ecc2.glm <- glm(cbind(Correct, Incorrect) ~ Contr * Size * task,
family = binomial(mafc.probit(4)), data = ecc2)
summary(ecc2.glm)
ecc2$fit <- fitted(ecc2.glm)</pre>
library(lattice)
xyplot(Correct / (Correct + Incorrect) ~ Contr | Size * task, data = ecc2,
subscripts = TRUE, ID = with(ecc2, Size + as.numeric(task)),
scale = list(x = list(log = TRUE),
y = list(limits = c(0, 1.05))),
xlab = "Contrast", ylab = "Proportion Correct Response",
aspect = "xy",
panel = function(x, y, subscripts, ID, ...) {
which = unique(ID[subscripts])
llines(x, ecc2$fit[which ==ID], col = "black", ...)
panel.xyplot(x, y, pch = 16, ...)
panel.abline(h = 0.25, lty = 2, ...)
)
```

probit.lambda

mafc Probit Link for Binomial Family with Upper Asymptote < 1

# **Description**

This function provides a link for the binomial family for fitting m-alternative forced-choice, with a probit link and with the upper asymptote permitted to be less than 1.

# Usage

```
probit.lambda(m = 2, lambda = 0)
```

# Arguments

m is the integer number (>1) of choices (Default to 2AFC).

1 number in [0, 1] indicating 1 minus the upper asymptotic value of the psychometric function.

probit.lambda 17

# **Details**

This function provides a link for fitting psychometric functions arising from an m-alternative forcedchoice experiment using a probit link and allowing that the upper aymptote is less than 1. The psychometric function fit to the data is described by

$$P(x) = 1/m + (1 - 1/m - \lambda)\Phi(x)$$

where m is the number of alternatives and the lower asymptote,  $1 - \lambda$  is the upper asymptote and  $\Phi$  is the cumulative normal function.

#### Value

The link returns a list containing functions required for relating the response to the linear predictor in generalized linear models and the name of the link.

linkfun The link function

linkinv DTHe inverse link function

mu.eta The derivative of the inverse link function

valideta The domain over which the linear predictor is valid

link A name to be used for the link

#### Note

Due to the difficulty of the task, subject error or incorrectly recorded data, psychophysical data may reveal less than perfect performance when stimulus differences are readily visible. When this occurs, letting the upper asymptote be less than 1 often results in a better fit to the data and a less-biased estimate of the steepness of the curve (see example below).

# Author(s)

Ken Knoblauch

#### References

Wichmann, F. A. and Hill, N. J. (2001) The psychometric function: I.Fitting, sampling, and goodness of fit. *Percept Psychophys.*, 63(8), 1293–1313.

# See Also

```
mafc, glm, glm.lambda, family, make.link
```

```
b <- 3.5
g <- 1/3
d <- 0.025
a <- 0.04
p <- c(a, b, g, d)
num.tr <- 160
```

18 psyfun.2asym

```
cnt <- 10^seq(-2, -1, length = 6) # contrast levels
#simulated Weibull-Quick observer responses
truep \leftarrow g + (1 - g - d) * pweibull(cnt, b, a)
ny <- rbinom(length(cnt), num.tr, truep)</pre>
nn <- num.tr - ny
phat <- ny/(ny + nn)
resp.mat <- matrix(c(ny, nn), ncol = 2)
ddprob.glm <- glm(resp.mat ~ cnt, family = binomial(mafc.probit(3)))</pre>
ddprob.lam <- glm(resp.mat ~ cnt, family = binomial(probit.lambda(3, 0.025)))</pre>
AIC(ddprob.glm, ddprob.lam)
plot(cnt, phat, \log = x^n, \cos = 1.5, y = c(0, 1))
pcnt <- seq(0.01, 0.1, len = 100)
lines(pcnt, predict(ddprob.glm, data.frame(cnt = pcnt),
                         type = "response"), lwd = 2)
lines(pcnt, predict(ddprob.lam, data.frame(cnt = pcnt),
                         type = "response"), 1wd = 2, 1ty = 2)
```

psyfun.2asym

Fit Psychometric Functions and Upper and Lower Asymptotes

# **Description**

Fits psychometric functions allowing for variation of both upper and lower asymptotes. Uses a procedure that alternates between fitting linear predictor with glm and estimating the asymptotes with optim until a minimum in -log likelihood is obtained within a tolerance.

# Usage

```
psyfun.2asym(formula, data, link = logit.2asym, init.g = 0.01,
init.lam = 0.01, trace = FALSE, tol = 1e-06,
mxNumAlt = 50, ...)
```

# **Arguments**

formula	a two sided formula specifying the response and the linear predictor
data	a data frame within which the formula terms are interpreted
link	a link function for the binomial family that allows specifying both upper and lower asymptotes
init.g	numeric specifying the initial estimate for the lower asymptote
init.lam	numeric specifying initial estimate for 1 - upper asymptote
trace	logical indicating whether to show the trace of the minimization of -log likelihood
tol	numeric indicating change in -log likelihood as a criterion for stopping iteration.
mxNumAlt	integer indicating maximum number of alternations between glm and optim steps to perform if minimum not reached.
	additional arguments passed to glm

psyfun.2asym 19

# **Details**

The function is a wrapper for glm for fitting psychometric functions with the equation

$$P(x) = \gamma + (1 - \gamma - \lambda)p(x)$$

where  $\gamma$  is the lower asymptote and lambda is 1- the upper asymptote, and p(x) is the base psychometric function, varying between 0 and 1.

# Value

list of class 'lambda' inheriting from classes 'glm' and 'lm' and containing additional components

lambda numeric indicating 1 - upper asymptote gam numeric indicating lower asymptote

SElambda numeric indicating standard error estimate for lambda based on the Hessian of

the last interation of optim. The optimization is done on the value transformed

by the function plogis and the value is stored in on this scale

SEgam numeric indicating standard error estimate for gam estimated in the same fashion

as SElambda

If a diagonal element of the Hessian is sufficiently close to 0, NA is returned.

#### Note

The cloglog.2asym and its alias, weib.2asym, don't converge on occasion. This can be observed by using the trace argument. One strategy is to modify the initial estimates.

# Author(s)

Kenneth Knoblauch

#### References

Klein S. A. (2001) Measuring, estimating, and understanding the psychometric function: a commentary. *Percept Psychophys.*, **63(8)**, 1421–1455.

Wichmann, F. A. and Hill, N. J. (2001) The psychometric function: I.Fitting, sampling, and goodness of fit. *Percept Psychophys.*, **63(8)**, 1293–1313.

# See Also

```
glm, optim, glm.lambda, mafc
```

```
#A toy example,
set.seed(12161952)
b <- 3
g <- 0.05 # simulated false alarm rate
d <- 0.03
a <- 0.04</pre>
```

20 RGB

```
p < -c(a, b, g, d)
num.tr <- 160
cnt <- 10^seq(-2, -1, length = 6) # contrast levels</pre>
#simulated Weibull-Quick observer responses
truep \leftarrow g + (1 - g - d) * pweibull(cnt, b, a)
ny <- rbinom(length(cnt), num.tr, truep)</pre>
nn <- num.tr - ny
phat <- ny/(ny + nn)
resp.mat <- matrix(c(ny, nn), ncol = 2)</pre>
ddprob.glm <- psyfun.2asym(resp.mat ~ cnt, link = probit.2asym)</pre>
ddlog.glm <- psyfun.2asym(resp.mat ~ cnt, link = logit.2asym)</pre>
# Can fit a Weibull function, but use log contrast as variable
ddweib.glm <- psyfun.2asym(resp.mat ~ log(cnt), link = weib.2asym)</pre>
ddcau.glm <- psyfun.2asym(resp.mat ~ cnt, link = cauchit.2asym)</pre>
plot(cnt, phat, \log = x^n, \cos = 1.5, y = c(0, 1))
pcnt <- seq(0.01, 0.1, len = 100)
lines(pcnt, predict(ddprob.glm, data.frame(cnt = pcnt),
type = "response"), lwd = 5)
lines(pcnt, predict(ddlog.glm, data.frame(cnt = pcnt),
type = "response"), lwd = 2, lty = 2, col = "blue")
lines(pcnt, predict(ddweib.glm, data.frame(cnt = pcnt),
type = "response"), lwd = 3, col = "grey")
lines(pcnt, predict(ddcau.glm, data.frame(cnt = pcnt),
type = "response"), lwd = 3, col = "grey", lty = 2)
summary(ddprob.glm)
```

Luminance Calibration Data from Video Projector

#### Description

RGB

The data were obtained from the measurements of the luminance of the R, G and B channels individually, as well as the three together, W, for each of 21 grey levels, GL from a screen on which a video projector was displaying an image of a uniform field. Grey level has been normalized to the interval [0, 1], though originally it is specified as integers in [0, 255]. The measurements were obtained with a Photo Research 650 spectro-radiometer.

#### Usage

```
data(RGB)
```

# Format

A data frame with 84 observations on the following 3 variables.

Lum numeric vector of the measured luminance in candelas/meter<sup>2</sup> GL The grey level normalized to the interval [0, 1] Gun factor with levels R G B W

SS.RGBcalib 21

# **Examples**

data(RGB)

SS.RGBcalib Self-Start Functions for Fitting Luminance vs Grey Level Relation on CRT displays

# Description

This selfStart model evaluates the parameters for describing the luminance vs grey level relation of the R, G and B guns of a CRT-like display, fitting a single exponent, gamma, for each of the 3 guns. It has an initial attribute that will evaluate initial estimates of the parameters, Blev, Br, Bg, Bb and gamm. In the case of fitting data from a single gun or for a combination of guns, as in the sum of the three for calibrating the *white*, the parameter k is used for the coefficient. Both functions include gradient and hessian attributes.

# Usage

```
SS.calib(Blev, k, gamm, GL)
SS.RGBcalib(Blev, Br, Bg, Bb, gamm, Rgun, Ggun, Bgun)
```

# Arguments

Blev	numeric. The black level is the luminance at the 0 grey level
k	numeric, coefficient of one gun for fitting single gun
Br	numeric, coefficient of the R gun
Bg	numeric, coefficient of the G gun
Bb	numeric, coefficient of the B gun
gamm	numeric, the exponent, gamma, applied to the grey level
GL	numeric, is the grey level for the gun tested, covariate in model matrix in one gun case
Rgun	numeric, is a covariate in the model matrix that indicates the grey level for the R gun. See the example below.
Ggun	numeric, is a covariate in the model matrix that indicates the grey level for the $\boldsymbol{G}$ gun
Bgun	numeric, is a covariate in the model matrix that indicates the grey level for the B gun

22 SS.RGBcalib

#### **Details**

The model

$$Lum(GL) = Blev + \beta_i * GL^{\gamma}$$

where i is in {R, G, B}, usually provides a reasonable description of the change in luminance of a display gun with grey level, GL. This selfStart function estimates  $\gamma$  and the other parameters using the nls function. It is assumed that grey level is normalized to the interval [0, 1]. This results in lower correlation between the linear coefficients of the guns,  $\beta_i$ , than if the actual bit-level is used, e.g., [0, 255], for an 8-bit graphics card (see the example). Also, with this normalization of the data, the coefficients,  $\beta_i$ , provide estimates of the maximum luminance for each gun. The need for the arguments Rgun, Ggun and Bgun is really a kludge in order to add gradient and hessian information to the model.

#### Value

returns a numeric vector giving the estimated luminance given the parameters passed as arguments and a gradient matrix and a hessian array as attributes.

# Author(s)

Kenneth Knoblauch

#### References

~put references to the literature/web site here ~

#### See Also

nls

```
data(RGB)
#Fitting a single gun
W.nls <- nls(Lum ~ SS.calib(Blev, k, gamm, GL), data = RGB,
subset = (Gun == "W"))
summary(W.nls)

#curvature (parameter effect) is greater when GL is 0:255
Wc.nls <- nls(Lum ~ SS.calib(Blev, k, gamm, GL*255), data = RGB,
subset = (Gun == "W"))
MASS::rms.curv(W.nls)
MASS::rms.curv(Wc.nls)
pairs(profile(Wc.nls), absVal = FALSE)
pairs(profile(W.nls), absVal = FALSE)

#Fitting 3 guns with independent gamma's
RGB0.nls <- nlme::nlsList(Lum ~ SS.calib(Blev, k, gamm, GL) | Gun,</pre>
```

summary.lambda 23

summary.lambda

Summary Method for Objects of Class 'lambda'

# Description

Identical to summary.glm but with one line of additional output: the estimate of lambda from glm.lambda, obtained by profiling the deviance and estimating its minimum.

# Usage

```
## S3 method for class 'lambda'
summary(object, ...)
## S3 method for class 'summary.lambda'
print(x, digits = max(3, getOption("digits") - 3),
    symbolic.cor = x$symbolic.cor,
    signif.stars = getOption("show.signif.stars"), ...)
```

# **Arguments**

object	Fitted model object of class "lambda" inheriting from glm and lm. Typically the output of glm.lambda.
x	an object of class "summary.lambda", usually a result of a call to summary.lambda.
digits	the number of significant digits to use when printing.
symbolic.cor	logical. If TRUE, print the correlations in a symbolic form (see symnum) rather than as numbers.
signif.stars	logical. If TRUE, "significance stars" are printed for each coefficient.
	further arguments passed to or from other methods.

# **Details**

Provides a summary of the class lambda object generated by glm.lambda.

24 summary.lambda

# Value

Returns the same structure as summary.glm with an added component, lambda.  $1-\lambda$  is the estimated upper asymptote of the psychometric function.

# Author(s)

Ken Knoblauch

# See Also

probit.lambda, glm.lambda

# **Index**

* datasets	glm.WH, 10, <i>14</i> , <i>15</i>
ecc2, <b>7</b>	
RGB, 20	logit.2asym, 12
* methods	6 0 11 14 17 10
summary.lambda,23	mafc, 9, 11, 14, 17, 19
* models	make.link, <i>13</i> , <i>15</i> , <i>17</i>
${\tt glm.lambda,8} \\ {\tt glm.WH,10}$	nls, 22
logit.2asym, 12 mafc, 14	optim, <i>15</i> , <i>19</i>
<pre>probit.lambda, 16 psyfun.2asym, 18</pre>	print.summary.lambda(summary.lambda).
SS.RGBcalib, 21	<pre>probit.2asym(logit.2asym), 12</pre>
* nonlinear	probit.lambda, 9, 11, 14, 15, 16, 24
SS.RGBcalib, 21	psyfun.2asym, <i>13</i> , 18
* package	psyphy (psyphy-package), 2
psyphy-package, 2	psyphy-package, 2
* print	pospiny package, 2
summary.lambda, 23	RGB, 20
* univar	,
dprime.ABX,2	SS.calib(SS.RGBcalib), 21
dprime.mAFC, 4	SS.RGBcalib, 21
dprime.oddity, 5	summary.glm, 24
dprime.SD, 6	summary.lambda, 23
and data Comman 0, 10	symnum, 23
as.data.frame, <i>8</i> , <i>10</i>	weib.2asym(logit.2asym),12
cauchit.2asym(logit.2asym), 12	werb. Zasylli (Togit. Zasylli), 12
cloglog.2asym(logit.2asym), 12	
cloglog.zasylii (loglt.zasylii), 12	
dprime.ABX, 2, 5, 7	
dprime.mAFC, 3, 4, 5, 7	
dprime.oddity, 3, 5, 5, 7	
dprime.SD, 3, 5, 6	
ecc2, 7	
family, 9, 11, 15, 17	
glm, 9, 11, 13, 15, 17, 19 glm lambda 8 11 14 15 17 19 24	