Package 'randomizeR'

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Title Randomization for Clinical Trials

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Description This tool enables the user to choose a randomization procedure based on sound scientific criteria. It comprises the generation of randomization sequences as well the assessment of randomization procedures based on carefully selected criteria. Furthermore, 'randomizeR' provides a function for the comparison of randomization procedures.

Depends R (>= 3.6.0), methods, ggplot2, plotrix, survival

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Suggests testthat, knitr

VignetteBuilder knitr

RoxygenNote 7.0.1

NeedsCompilation no

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Description

randomizeR-package

This tool enables the user to choose a randomization procedure based on sound scientific criteria. It comprises the generation of randomization sequences as well the assessment of randomization procedures based on carefully selected criteria. Furthermore, randomizeR provides a function for the comparison of randomization procedures.

Randomization for Clinical Trials

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References

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- M. V. Rueckbeil, R. D. Hilgers, N. Heussen (2019). "Randomization in survival studies: An evaluation method that takes into account selection and chronological bias." PLOS ONE, 14(6): e0217946. doi: 10.1371/journal.pone.0217946 (URL: https://doi.org/10.1371/journal.pone.0217946).

See Also

For functionality for randomization procedures, see randPar and genSeq. For the criteria for the assessment of randomization procedures, see issues. For the assessment and comparison of randomization procedures, see assess and compare.

а

Function returning the adjusting parameter a slot of an S4 object

Description

Function returning the adjusting parameter a slot of an S4 object

Usage

a(obj)

Arguments

obj

object of class randPar

abcdPar 5

abcdPar	Representing Accelerated Biased Coin Design
3.5 Ca. Ca.	The problem in the 2 table a count 2 table.

Description

Represents the randomization procedure Accelerated Biased Coin Design.

Usage

```
abcdPar(N, a, groups = LETTERS[1:2])
```

Arguments

N	integer for the total sample size of the trial.
a	nonnegative parameter which controls the degree of randomness: For decreasing a the allocations become deterministic, while for increasing a the randomization procedure tends to complete randomization.
groups	character vector of labels for the different treatments.

Details

This is a class of 'biased coins' where the probability of selecting the under-represented treatment is dependent from the absolute difference between the two treatment allocations up to the current step.

Value

S4 object of the class abcdPar.

References

A. B. Antognini and A. Giovagnoli (2004) A new 'biased coin design' for the sequential allocation of two treatments. *Journal of the Royal Statistical Society. Series C (Applied Statistics)* **53**, No. 4, 651-664

See Also

```
Other randomization procedures: bbcdPar, bsdPar, chenPar, crPar, createParam(), ebcPar, gbcdPar, hadaPar, mpPar, pbrPar, rarPar, rpbrPar, rtbdPar, tbdPar, udPar
```

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assess

Assessing randomization sequences

Description

Assesses randomization sequences based on specified issues in clinical trials.

Usage

```
assess(randSeq, ..., endp)
## S4 method for signature 'randSeq,missing'
assess(randSeq, ..., endp)
## S4 method for signature 'randSeq,endpoint'
assess(randSeq, ..., endp)
```

Arguments

randSeq object of class randSeq.
... at least one object of class issue or just a list of objects of the class issue.
endp object of class endpoint, or missing.

Details

Randomization sequences behave differently with respect to issues like selection bias, chronological bias, or loss in power estimation. The assess function evaluates the behavior of randomization sequences with respect to these issues. The first argument should be a result of one of the functions genSeq or getAllSeq. The second argument should be any number of issues arising in a clinical trial. The last argument endp may be provided if the assessment should take the distribution of the treatment groups into account, e.g. for power evaluation.

Value

S4 object of class assessment summarizing the assessment of the randomization procedure.

See Also

```
Representation of randomization procedures: randPar
Generation of randomization sequences: genSeq
issues for the assessment of randomization sequences
```

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Examples

```
# assess the full set of Random Allocation Rule for N=4 patients
sequences <- getAllSeq(rarPar(4))</pre>
issue1 <- corGuess("CS")</pre>
issue2 <- corGuess("DS")</pre>
issue3 <- imbal("imb")</pre>
issue4 <- imbal("maxImb")</pre>
assess(sequences, issue1, issue2, issue3, issue4)
# assess one sequence of the Big Stick Design with respect to correct guesses
sequence <- genSeq(bsdPar(10, 2), seed = 1909)</pre>
assess(sequence, issue1)
# assess the same sequence with respect to selection bias and power for a normal endpoint
endp \leftarrow normEndp(c(2, 2), c(1, 1))
issue5 <- selBias("CS", 4, "exact")</pre>
issue6 <- setPower(2, "exact")</pre>
assess(sequence, issue1, issue5, issue6, endp = endp)
# assess the same sequence with respect to selection bias for an exponential endpoint
endp \leftarrow expEndp(lambda = c(0.5, 0.5), cenRate=0.1, accrualTime=1, cenTime=5)
issue7 <- selBias("CS", 0.1, "exact")</pre>
assess(sequence, issue1, issue7, endp = endp)
# recommended plot for the assessment of rejection probabilities
RP <- getAllSeq(crPar(6))</pre>
cB <- chronBias(type = "linT", theta = 1/6, method = "exact")</pre>
sB <- selBias(type= "CS", eta = 1/4, method = "exact")
normEndp \leftarrow normEndp(c(0, 0), c(1, 1))
A <- assess(RP, cB, sB, endp = normEndp)
D <- A$D
desiredSeq \leftarrow round(sum(D[,2][D[,3] \leftarrow 0.05 \& D[,4] \leftarrow 0.05]), digits = 4)
colnames(D) <- c("Seq", "Prob", "SB", "linT")</pre>
g \leftarrow ggplot(D, aes(x = SB, y = linT))
g \leftarrow g + annotate("rect", xmin = 0, xmax = 0.05, ymin = 0, ymax = 0.05,
alpha=0.2, fill="green")
g <- g + geom_point(alpha = 1/10, size = 3, col = "orange")
g <- g <- g + geom_vline(xintercept = 0.05, col = "red")</pre>
g <- g + geom_hline(yintercept = 0.05, col = "red")</pre>
g <- g + geom_text(data = NULL, x = 0, y = 0,
label = paste("Proportion:", desiredSeq), hjust=0, vjust=0, size = 7)
```

bbcdPar

Representing Bayesian Biased Coin Design

Description

Represents the randomization procedure Bayesian Biased Coin Design.

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Usage

```
bbcdPar(N, a, groups = LETTERS[1:2])
```

Arguments

N integer for the total sample size of the trial.

a nonnegative parameter which controls the degree of randomness: For decreasing

a the allocations become deterministic, while for increasing a the randomization

procedure tends to complete randomization.

groups character vector of labels for the different treatments.

Details

Extension of Efron's biased coin design.

Value

S4 object of the class bbcdPar.

References

A. B. Antognini and Maroussa Zagoraiou (2014) Balance and randomness in sequential clinical trials: the dominant biased coin design. *Pharmaceutical Statistics* **13(2)**, 119-127

See Also

Other randomization procedures: abcdPar, bsdPar, chenPar, crPar, createParam(), ebcPar, gbcdPar, hadaPar, mpPar, pbrPar, rarPar, rpbrPar, rtbdPar, tbdPar, udPar

blocks

Function returning the block slot of an S4 object

Description

Function returning the block slot of an S4 object

Usage

```
blocks(obj)
```

Arguments

obj

object of class pbrPAr

bsdPar 9

bsdPar	Representing Big Stick Design

Description

Represents the randomization procedure Big Stick Design.

Usage

```
bsdPar(N, mti, groups = LETTERS[1:2])
```

Arguments

N integer for the total sample size of the trial.

mti maximum tolerated imbalance in patient numbers during the trial.

groups character vector of labels for the different treatments.

Details

Tossing a fair coin as long as the difference in group sizes does not exceed the mti. If the mti is reached a deterministic allocation is done, so that the difference in group sizes is reduced.

Value

S4 object of the class bsdPar.

References

J. F. Soares and C. F. Jeff Wu (1983) Some Restricted Randomization Rules in Sequential Designs. *Comm. in Stat.*, **12**, 2017-34.

See Also

```
Other randomization procedures: abcdPar, bbcdPar, chenPar, crPar, createParam(), ebcPar, gbcdPar, hadaPar, mpPar, pbrPar, rarPar, rpbrPar, rtbdPar, tbdPar, udPar
```

10 chenPar

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Representing Chen's Design

Description

Represents the randomization procedure Chen's Design.

Usage

```
chenPar(N, mti = N, p = 0.5, groups = LETTERS[1:2])
```

Arguments

N integer for the total sample size of the trial.

mti maximum tolerated imbalance in patient numbers during the trial.

p success probability of the biased coin (e.g. in Efron's Biased Coin Design).

groups character vector of labels for the different treatments.

Details

Flip a biased coin with probability p in favor of the treatment which is allocated less frequently as long as the difference in group sizes does not exceed the mti. If the mti is reached a deterministic allocation is done, so that the difference in group sizes is reduced. If both treatments have been assigned equally often a fair coin is tossed.

Value

S4 object of the class chenPar.

References

Chen Yung-Pin (1999) Biased coin design with imbalance tolerance. Comm. in Stat., 15, 953-975.

See Also

```
Other randomization procedures: abcdPar, bbcdPar, bsdPar, crPar, createParam(), ebcPar, gbcdPar, hadaPar, mpPar, pbrPar, rarPar, rpbrPar, rtbdPar, tbdPar, udPar
```

chronBias 11

	chronBias	Representing chronological bias	
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Description

Represents the issue of chronological bias in a clinical trial.

Usage

```
chronBias(type, theta, method, saltus, alpha = 0.05)
```

Arguments

type	character string, should be one of "linT", "logT", or "stepT", see Details.
theta	factor of the time trend for further details see type.
method	character string, should be one of "sim" or "exact", see Description.
saltus	integer or missing specifying the patient index (i.e. position) of the step in case of step time trend.
alpha	significance level

Details

Chronological bias can be an issue in the design of a clinical trial. The chronBias function is a constructor function for an S4 object of the class chronBias representing the issue of chronological bias, s.a. time trends, in a clinical trial. It supports two possible modes, method="sim" and method="exact", and three different types of trend.

If method="sim", the object represents the simulated type-I-error rate given the level alpha, the selection effect eta and the biasing strategy type. When calling assess for a chronBias object with method="sim", one test decision is computed for each sequence of randSeq. The type-I-error rate (power) is the proportion of falsely (correctly) rejected null hypotheses.

If method="exact", the object represents the exact type-I-error probability given the level alpha, the selection effect eta and the biasing strategy type. When calling assess for a chronBias object with method="exact", the p-value of each randomization sequence is computed. For normal endpoints and two treatment groups these p-values are exact values which can be calculated from the sum of the corresponding quantiles of the doubly noncentral t-distribution. For more than two treatment groups, exact p-values are computed using a doubly noncentral F distribution. For exponential endpoints the p-values are obtained using an approximation formula.

Types of chronological bias:

type = "linT" Represents linear time trend. Linear time trend means that the time trend function of the patients, i.e. expected response for normal endpoints, increases evenly by theta/(N-1) with every patient included in the study, until reaching theta after N patients. Linear time trend may occur as a result of gradually relaxing in- or exclusion criteria throughout the trial. It can be represented by the formula:

$$f(i) = (i-1)/(N-1)\theta$$

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type = "logT" Represents logarithmic time trend. Logarithmic time trend means that the time trend function of the patients, i.e. expected response for normal endpoints, increases logarithmically in the patient index by theta/log(N) with every patient included in the study, until reaching theta after N patients. Logarithmic time trend may occur as a result of a learning curve, i.e. in a surgical trial. It can be represented by the formula:

$$\log(i)/\log(N)\theta$$

type = "stepT" Represents step trend. Step trend means that the expected response of the patients increases by theta after a given point ("saltus") in the allocation process. Step trend may occur if a new device is used after the point c = "saltus", or if the medical personal changes after this point. Step time trend can be represented by the formula:

$$f(i) = 1_{c < i < N} \theta$$

Value

S4 object of class chronBias, a formal representation of the issue of chronological bias in a clinical trial.

References

- G. K. Rosenkranz (2011) The impact of randomization on the analysis of clinical trials. *Statistics in Medicine*, **30**, 3475-87.
- M. Tamm and R.-D. Hilgers (2014) Chronological bias in randomized clinical trials under different types of unobserved time trends. *Methods of Information in Medicine*, **53**, 501-10.

See Also

```
Other issues: combineBias(), corGuess, imbal, issue, selBias, setPower()
```

Examples

```
# create a linear time trend with theta = 0.5 for which the exact rejection probabilities
# are calculated
cbias <- chronBias("linT", 0.5, "exact")

# create a stepwise time trend with theta = 1 after 10 allocations for which the test
# decision is simulated
cbias <- chronBias("stepT", 1, "sim", 10)</pre>
```

coin

Function returning the coin slot of an S4 object

Description

Function returning the coin slot of an S4 object

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Usage

```
coin(obj)
```

Arguments

obj

object extending class randPar or randSeq

combineBias

Combined bias criterion

Description

This class combines a selBias object and a chronBias object to a new object. In the analysis within the new object the two types of bias are treated as additive effect for normal endpoints and as multiplicative effect for exponential endpoints.

Usage

```
combineBias(selBias, chronBias)
```

Arguments

selBias object of class selBias chronBias object of class chronBias

See Also

```
Other issues: chronBias, corGuess, imbal, issue, selBias, setPower()
```

Examples

```
chronBias <- chronBias(type="linT", theta=1, method="sim")
selBias <- selBias(type="CS", eta=1, method="sim")
combineBias(selBias, chronBias)</pre>
```

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compare

Comparison of randomization procedures

Description

Compares randomization procedures based on a specified issue in clinical trials.

Usage

```
compare(issue, ..., endp)
## S4 method for signature 'issue,missing'
compare(issue, ..., endp)
## S4 method for signature 'issue,endpoint'
compare(issue, ..., endp)
```

Arguments

```
issue object of class issue.... at least one object of class randSeq or a list of objects of class randSeq.endp object of class endpoint, or missing.
```

Details

Randomization procedures behave differently with respect to issues like selection bias, chronological bias, or loss in power estimation. The compare function evaluates the behavior of randomization procedures with respect to one issue. Its first argument should represent one of the implemented issues. The second argument should be any number of objects of the class randSeq. These objects represent the randomization procedures for the planned comparison. The last argument endp may be provided if the assessment should take the distribution of the treatment groups into account, e.g. for power evaluation.

Value

S4 object of class comparison summarizing the comparison of the randomization procedures.

See Also

```
Representation of randomization procedures: randPar
Generation of randomization sequences: genSeq
issues for the assessment of randomization sequences
```

corGuess 15

Examples

```
# compare Random Allocation Rule and Big Stick for N = 4 with respect to
# correct guesses
RAR <- getAllSeg(rarPar(4))</pre>
BSD <- getAllSeq(bsdPar(4, mti = 2))
corGuess <- corGuess("CS")</pre>
(comp <- compare(corGuess, RAR, BSD))</pre>
plot(comp)
# compare the same procedures with respect to selection bias for a normal endpoint
endp <- normEndp(c(2, 2), c(1, 1))
selBias <- selBias("CS", 4, "exact")</pre>
(comp <- compare(selBias, RAR, BSD, endp = endp))</pre>
plot(comp)
# compare the same procedures with respect to selection bias for an exponential endpoint
endp <- expEndp(lambda = c(0.5, 0.5), cenRate=0.1, accrualTime=1, cenTime=5)
selBias <- selBias("CS", 0.1, "exact")</pre>
(comp <- compare(selBias, RAR, BSD, endp = endp))</pre>
plot(comp)
```

corGuess

Representing the expected number of correct guesses

Description

Represents the expected number of correct guesses of randomization sequences.

Usage

```
corGuess(type)
```

Arguments

type

character string, should be one of "CS" or "DS", see Details.

Details

Selection bias can be an issue in the design of a clinical trial. The expected number of correct guesses is one measure for selection bias. The corGuess function is a constructor function for an S4 object of the class corGuess representing the issue of correct guesses in a clinical trial. The parameter type takes the following values:

- "CS" refers to "convergence strategy", i.e. the investigator predicts the treatment which has hitherto occurred less often.
- "DS" refers to "divergence strategy", i.e. the investigator predicts the treatment which has hitherto occurred more often.

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Value

S4 object of class corGuess, a formal representation of the issue of correct guesses in a clinical trial

References

D. Blackwell and J.L. Hodges Jr. (1957) Design for the control of selection bias. *Annals of Mathematical Statistics*, **25**, 449-60.

See Also

Other issues: chronBias, combineBias(), imbal, issue, selBias, setPower()

createParam	Representing any randomization procedure	

Description

Represents any randomization procedure for a two-armed clinical trial.

Usage

```
createParam(method, N, mti, bc, rb, p, ini, add, filledBlock)
```

Arguments

method	walues PBR, RAR, HAD, PWR, EBC, BSD, CR, TBD, UD, and MP.
N	integer for the total sample size of the trial.
mti	maximum tolerated imbalance in patient numbers during the trial.
bc	vector which contains the lengths k_1, \ldots, k_l of each block. This means that the vector bc will have one entry for each block.
rb	block lengths of the blocks that can be selected equiprobable at random.
p	success probability of the biased coin (e.g. in Efron's Biased Coin Design).
ini	integer representing the initial urn composition.
add	integer representing the number of balls that are added to the urn in each step.
filledBlock	logical whether the last block should be filled or not.

Details

Depending on the input of the user, createParam creates an object representing a randomization procedures for a two-armed clinical trial (see also randPar).

Value

S4object of the corresponding randomization procedure class.

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See Also

Other randomization procedures: abcdPar, bbcdPar, bsdPar, chenPar, crPar, ebcPar, gbcdPar, hadaPar, mpPar, pbrPar, rarPar, rpbrPar, rtbdPar, tbdPar, udPar

createSeq Query to create a randomization sequence of a particular randomization procedure

Description

This function is a query to create an corresponding randomization sequence for a two-armed clinical trial. If file is defined, the generated sequence is automatically saved to the corresponding path.

Usage

```
createSeq(file)
```

Arguments

file

A connection, or a character string naming the file to write to.

Value

an object Param, which is available

crPar

Representing Complete Randomization

Description

Represents the randomization procedure Complete Randomization.

Usage

```
crPar(N, K = 2, ratio = rep(1, K), groups = LETTERS[1:K])
```

Arguments

groups

N	integer for the total sample size of the trial.
K	number of treatment groups (e.g. K=2 if we compare one experimental against one control treatment).
ratio	vector of length K. The total sample number N and all used block lengths (bc) have to be divisible by sum(ratio).

character vector of labels for the different treatments.

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Details

Toss a fair coin N times in case K=2 and assign the treatments according to the result of the coin. In case of K>2, replace the coin by a die with K sides.

Value

S4 object of the class crPar.

References

W. F. Rosenberger and J. M. Lachin (2002) Randomization in Clinical Trials. Wiley.

See Also

Other randomization procedures: abcdPar, bbcdPar, bsdPar, chenPar, createParam(), ebcPar, gbcdPar, hadaPar, mpPar, pbrPar, rarPar, rpbrPar, rtbdPar, tbdPar, udPar

derFunc

Representing Derringer-Suich desirability functions

Description

Represents the Derringer-Suich desirability approach.

Usage

```
derFunc(TV, SLs, b)
```

Arguments

TV numeric specifying the optimal desired value called the target value.

SLs numeric vector of length at most 2 specifying the lower and/or upper specified

border.

b numeric vector of length at most 2 specifying the weight(s) for the punishment

of deviations from the target value.

Details

derFunc represents the framework for left, right and two-sided desirability functions introduced by Derringer and Suich (1980). For all three different kinds of desirability functions the parameter TV must be specified. If the parameter SLs has length 1, either the left- or right-sided desirability function is created depending from whether the value is smaller (left-sided) or greater (right-sided) than the target value. By specifying SLs as a vector of length 2 a two-sided desirability function is created where the lower specified border is determined as the smaller value of SLs and thus the upper specified border is determined as the greater value. If there are no values specified for the weights, then they are automatically set to 1 (linear loss).

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Value

S4 object of class derFunc, a formal representation of desirability functions introduced by Derringer and Suich.

References

Derringer, G., and Suich, R., (1980) Simultaneous Optimization of Several Response Variables. *Journal of Quality Technology*, **12**, 214-219.

See Also

```
Other desirability topics: evaluate(), getDesScores(), plotDes(), plotEv(), probUnDes()
```

Examples

```
# create an object of a left-sided desirability function
dLeft <- derFunc(0.5, 0.3, 2)

# create an object of a right-sided desirability function
dRight <- derFunc(0.5, 0.8, 1)

# create an object of a two-sided desirability function
dLR <- derFunc(0.5, c(0.3, 0.9), c(3, 1))</pre>
```

desirability

Desirability functions within the scope of clinical trials

Description

Illustrates the interplay between functions related to desirability indices.

Details

Currently, randomizeR encompasses the class of desirability functions introduced by Derringer and Suich (1980) and corresponding functions to evaluate and compare randomization sequences which have been assessed on the basis of desirability indices of specific issues:

- derFunc represents the class of desirability functions according to Derringer-Suich (1980).
- **getDesScores** can be applied to an object of class assessment together with prespecified desirability functions to compare the behavior of randomization sequences (on a common scale [0,1]).
- plotDes plots a desScores object on a radar chart.
- **evaluate** performs a comparison of sequences from different randomization sequences on the basis of object of the class desScores.
- plotEv plots an evaluation object on a radar chart.
- **probUnDes** computes the probability of undesired randomization sequences with respect to certain issues and desirability functions.

20 ebcPar

Examples

```
# perform a comparison of randomization sequences from different randomization procedures
# with the help of desirability functions
issue1 <- corGuess("CS")</pre>
issue2 <- chronBias(type = "linT", theta = 1/4, method = "exact")</pre>
RAR <- getAllSeq(rarPar(4))</pre>
BSD <- getAllSeq(bsdPar(4, mti = 2))</pre>
A1 <- assess(RAR, issue1, issue2, endp = normEndp(c(0,0), c(1,1)))
A2 <- assess(BSD, issue1, issue2, endp = normEndp(c(0,0), c(1,1)))
d1 \leftarrow derFunc(TV = 0.5, 0.75, 2)
d2 \leftarrow derFunc(0.05, c(0, 0.1), c(1, 1))
# apply the getDesScores function to the assessment output with the specified desirability
\# functions to evaluate the behaviour of randomization sequences on a [0,1] scale
DesScore <- getDesScores(A1, d1, d2, weights = c(5/6, 1/6))
DesScore2 <- getDesScores(A2, d1, d2, weights = c(5/6, 1/6))
# plotting the desScores objects
plotDes(DesScore, quantiles = TRUE)
plotDes(DesScore2, quantiles = TRUE)
# summarize the results of getDesScore with respect to the statistic "mean"
evaluate(DesScore, DesScore2)
# plot the evaluation objects for a visualized comparison
plotEv(evaluate(DesScore, DesScore2))
# display which randomzation procedure produces more undesired randomization sequences
# with respect to certain issues and desirability functions
probUnDes(DesScore)
probUnDes(DesScore2)
```

ebcPar

Representing Efron's Biased Coin Design

Description

Represents the randomization procedure Efron's Biased Coin Design.

Usage

```
ebcPar(N, p, groups = LETTERS[1:2])
```

21 evaluate

Arguments

N	integer for the total	sample size of the trial.

success probability of the biased coin (e.g. in Efron's Biased Coin Design). р

character vector of labels for the different treatments. groups

Details

Flip a biased coin with probability p in favor of the treatment which is allocated less frequently. If both treatments have been assigned equally often a fair coin is tossed.

Value

S4 object of the class ebcPar.

References

B. Efron (1971) Forcing a sequential experiment to be balanced. *Biometrika*, **58**, 403-17.

See Also

Other randomization procedures: abcdPar, bbcdPar, bsdPar, chenPar, crPar, createParam(), gbcdPar, hadaPar, mpPar, pbrPar, rarPar, rpbrPar, rtbdPar, tbdPar, udPar

evaluate

Evaluation of several randomization procedures with respect to certain desirability functions applied to specified issues.

Description

Evaluation of several randomization procedures with respect to certain desirability functions applied to specified issues.

Usage

```
evaluate(..., statistic)
## S4 method for signature 'missing'
evaluate(..., statistic)
## S4 method for signature 'character'
evaluate(..., statistic)
```

Arguments

statistic

at least one object of the class desScores or a list of objects of the class desScores. character string that specifies on the basis of which statistic the evaluate function should be applied. The statistic can be chosen from "mean", "median", "min" or "max".

22 evaluate

Details

The evaluate function allows the user to compare and evaluate different randomization procedures. It expects a number of objects that result when applying the getDesScores function to an assess object and specified desirability functions. The evaluate function summarizes the desirability scores of each randomization procedure on the basis of a prespecified statistic and incorporates them into a data frame. If no statistic is specified then it is automatically set to mean. If the function is applied to only one object it corresponds simply to summary(getDesScores(...)).

Value

S4 object of class evaluation Comparison of randomization procedures with respect to desirability functions applied to specified issues, summarized by a prespecified statistic.

References

D. Schindler Assessment of Randomization Procedures in the Presence of Selection and Chronological Bias. PhD Thesis.

See Also

Representation of randomization procedures: randPar

Generation of randomization sequences: genSeq

issues for the desirability of randomization sequences

Other desirability topics: derFunc, getDesScores(), plotDes(), plotEv(), probUnDes()

Examples

```
# compare Random Allocation Rule to Big Stick Design with respect to different issues
# and their corresponding desirability functions
issue1 <- corGuess("CS")
issue2 <- corGuess("DS")
RAR <- getAllSeq(rarPar(4))
BSD <- getAllSeq(bsdPar(4, mti = 2))
A1 <- assess(RAR, issue1, issue2)
A2 <- assess(BSD, issue1, issue2)

d1 <- derFunc(TV = 0.1, 0.7, 2)
d2 <- derFunc(0.5, c(0.3, 0.8), c(1, 1))
DesScore <- getDesScores(A1, d1, d2, weights = c(5/6, 1/6))
DesScore2 <- getDesScores(A2, d1, d2, weights = c(5/6, 1/6))
evaluate(DesScore, DesScore2)
evaluate(DesScore, DesScore2, statistic = "max")</pre>
```

expEndp 23

expEndp	Representation of exponentially distributed endpoints

Description

Represents exponentially distributed endpoints in clinical trials.

Usage

```
expEndp(lambda, cenRate, accrualTime = 0, cenTime)
```

Arguments

lambda vector of the exponential rate parameters in each treatment group.

cenRate exponential censoring rate in a survival study.

accrualTime duration of the accrual period in a survival study.

cenTime total duration of a survival study (maximum length of followup).

Details

The expEnd function is a constructor function for an S4 object of the class expEnd representing an exponentially distributed endpoint in a clinical trial. In conjunction with the assess function, exponential endpoints admit the calculation of the 'exact' type-I-error probability and power using an approximation formula.

See Also

Compute exact or simulated type-I-error: assess.

Other endpoint types: normEndp, survEndp

Examples

```
# set the parameters of two exponentially distributed endpoints endp <- expEndp(lambda = c(1, 2), cenTime = 10, cenRate = 0.01)
```

24 gbcdPar

Ø	bc	dΡ	'ar

Representing Generalized Biased Coin Design

Description

Represents the randomization procedure Generalized Biased Coin Design.

Usage

```
gbcdPar(N, rho, groups = LETTERS[1:2])
```

Arguments

N integer for the total sample size of the trial.

rho nonnegative parameter which my be adjusted according to how strongly it is

desired to balance the experiment. If rho = 1, we have Wei's urn design with

alpha = 0. If rho = 0, we have complete randomization.

groups character vector of labels for the different treatments.

Details

Generalization of Wei's urn and Efron's biased coin design.

Value

S4 object of the class gbcdPar.

References

R. L. Smith (1984) Sequential treatment allocation using biased coin designs. *Journal of the Royal Statistical Society B*, **46**, 519-543.

W. F. Rosenberger and J. M. Lachin (2002) Randomization in Clinical Trials. Wiley, 64-65

See Also

Other randomization procedures: abcdPar, bbcdPar, bsdPar, chenPar, crPar, createParam(), ebcPar, hadaPar, mpPar, pbrPar, rarPar, rpbrPar, rtbdPar, tbdPar, udPar

generateAllSequences 25

generateAllSequences Complete set of randomization sequences

Description

Computes all randomization sequences for the given randomization procedure, and stores them in an object along with the parameters belonging to the randomization procedure.

Usage

```
getAllSeq(obj)
## S4 method for signature 'abcdPar'
getAllSeq(obj)
## S4 method for signature 'bbcdPar'
getAllSeq(obj)
## S4 method for signature 'ebcPar'
getAllSeq(obj)
## S4 method for signature 'bsdPar'
getAllSeq(obj)
## S4 method for signature 'chenPar'
getAllSeq(obj)
## S4 method for signature 'crPar'
getAllSeq(obj)
## S4 method for signature 'gbcdPar'
getAllSeq(obj)
## S4 method for signature 'hadaPar'
getAllSeq(obj)
## S4 method for signature 'mpPar'
getAllSeq(obj)
## S4 method for signature 'pbrPar'
getAllSeq(obj)
## S4 method for signature 'rarPar'
getAllSeq(obj)
## S4 method for signature 'tbdPar'
getAllSeq(obj)
```

```
## S4 method for signature 'udPar'
getAllSeq(obj)
```

Arguments

obj

object specifying the randomization procedure, see randPar or createParam.

Details

getAllSeq is a generic function which dispatches different methods depending on the type of input. The set of sequences of a procedure is computed by enumerating all possible sequences and eliminating those that are not possible in the randomization procedure specified by obj. The parameters of the randomization procedure are saved along with the sequences to ensure reproducibility of the results.

Value

An object inheriting from randSeq, representing the set of randomization sequences for the given parameters. The output consists of the parameters used for the generation of the randomization sequences (see createParam) and the matrix M that stores the randomization sequences in its rows.

See Also

createParam

Examples

```
# all randomization sequences of Efron's Biased Coin Design with p = 0.667 for N = 6
myPar <- ebcPar(6, 0.667)
getAllSeq(myPar)

# all randomization sequences of Big Stick Design with mti = 2 for N = 6
myPar <- bsdPar(6, 2)
getAllSeq(myPar)

# all randomization sequences of Permuted Block Randomization with block sizes 4 and 2
myPar <- pbrPar(c(4, 2))
getAllSeq(myPar)</pre>
```

generateRandomSequences

Generate random sequences

Description

Generates randomization sequences from a given randomization procedure.

Usage

```
genSeq(obj, r, seed)
## S4 method for signature 'abcdPar, numeric, numeric'
genSeq(obj, r, seed)
## S4 method for signature 'abcdPar, numeric, missing'
genSeq(obj, r, seed)
## S4 method for signature 'abcdPar, missing, numeric'
genSeq(obj, r, seed)
## S4 method for signature 'abcdPar,missing,missing'
genSeq(obj, r, seed)
## S4 method for signature 'bbcdPar, numeric, numeric'
genSeq(obj, r, seed)
## S4 method for signature 'bbcdPar,numeric,missing'
genSeq(obj, r, seed)
## S4 method for signature 'bbcdPar, missing, numeric'
genSeq(obj, r, seed)
## S4 method for signature 'bbcdPar, missing, missing'
genSeq(obj, r, seed)
## S4 method for signature 'ebcPar, numeric, numeric'
genSeq(obj, r, seed)
## S4 method for signature 'ebcPar,missing,numeric'
genSeq(obj, r, seed)
## S4 method for signature 'ebcPar, numeric, missing'
genSeq(obj, r, seed)
## S4 method for signature 'ebcPar,missing,missing'
genSeq(obj, r, seed)
```

```
## S4 method for signature 'bsdPar, numeric, numeric'
genSeq(obj, r, seed)
## S4 method for signature 'bsdPar, numeric, missing'
genSeq(obj, r, seed)
## S4 method for signature 'bsdPar, missing, numeric'
genSeq(obj, r, seed)
## S4 method for signature 'bsdPar,missing,missing'
genSeq(obj, r, seed)
## S4 method for signature 'chenPar, numeric, numeric'
genSeq(obj, r, seed)
## S4 method for signature 'chenPar,numeric,missing'
genSeq(obj, r, seed)
## S4 method for signature 'chenPar, missing, numeric'
genSeq(obj, r, seed)
## S4 method for signature 'chenPar,missing,missing'
genSeq(obj, r, seed)
## S4 method for signature 'crPar, numeric, numeric'
genSeq(obj, r, seed)
## S4 method for signature 'crPar,missing,numeric'
genSeq(obj, r, seed)
## S4 method for signature 'crPar, numeric, missing'
genSeq(obj, r, seed)
## S4 method for signature 'crPar,missing,missing'
genSeq(obj, r, seed)
## S4 method for signature 'gbcdPar,numeric,numeric'
genSeq(obj, r, seed)
## S4 method for signature 'gbcdPar, numeric, missing'
genSeq(obj, r, seed)
## S4 method for signature 'gbcdPar, missing, numeric'
genSeq(obj, r, seed)
## S4 method for signature 'gbcdPar,missing,missing'
genSeq(obj, r, seed)
```

genSeq(obj, r, seed)

```
## S4 method for signature 'hadaPar,numeric,numeric'
genSeq(obj, r, seed)
## S4 method for signature 'hadaPar,missing,numeric'
genSeq(obj, r, seed)
## S4 method for signature 'hadaPar, numeric, missing'
genSeq(obj, r, seed)
## S4 method for signature 'hadaPar,missing,missing'
genSeq(obj, r, seed)
## S4 method for signature 'mpPar,numeric,numeric'
genSeq(obj, r, seed)
## S4 method for signature 'mpPar,missing,numeric'
genSeq(obj, r, seed)
## S4 method for signature 'mpPar, numeric, missing'
genSeq(obj, r, seed)
## S4 method for signature 'mpPar,missing,missing'
genSeq(obj, r, seed)
## S4 method for signature 'pbrPar, missing, numeric'
genSeq(obj, r, seed)
## S4 method for signature 'pbrPar, numeric, numeric'
genSeq(obj, r, seed)
## S4 method for signature 'pbrPar,missing,missing'
genSeq(obj, r, seed)
## S4 method for signature 'pbrPar, numeric, missing'
genSeq(obj, r, seed)
## S4 method for signature 'rarPar, numeric, numeric'
genSeq(obj, r, seed)
## S4 method for signature 'rarPar, missing, numeric'
genSeq(obj, r, seed)
## S4 method for signature 'rarPar, numeric, missing'
genSeq(obj, r, seed)
## S4 method for signature 'rarPar,missing,missing'
```

```
## S4 method for signature 'rpbrPar, missing, numeric'
genSeq(obj, r, seed)
## S4 method for signature 'rpbrPar, numeric, numeric'
genSeq(obj, r, seed)
## S4 method for signature 'rpbrPar, missing, missing'
genSeq(obj, r, seed)
## S4 method for signature 'rpbrPar, numeric, missing'
genSeq(obj, r, seed)
## S4 method for signature 'tbdPar, numeric, numeric'
genSeq(obj, r, seed)
## S4 method for signature 'tbdPar,missing,numeric'
genSeq(obj, r, seed)
## S4 method for signature 'tbdPar, numeric, missing'
genSeq(obj, r, seed)
## S4 method for signature 'tbdPar,missing,missing'
genSeq(obj, r, seed)
## S4 method for signature 'rtbdPar, numeric, numeric'
genSeq(obj, r, seed)
## S4 method for signature 'rtbdPar, missing, numeric'
genSeq(obj, r, seed)
## S4 method for signature 'rtbdPar, numeric, missing'
genSeq(obj, r, seed)
## S4 method for signature 'rtbdPar,missing,missing'
genSeq(obj, r, seed)
## S4 method for signature 'udPar, numeric, numeric'
genSeq(obj, r, seed)
## S4 method for signature 'udPar, missing, numeric'
genSeq(obj, r, seed)
## S4 method for signature 'udPar, numeric, missing'
genSeq(obj, r, seed)
## S4 method for signature 'udPar, missing, missing'
genSeq(obj, r, seed)
```

Arguments

obj	object specifying the randomization procedure, see randPar or createParam.
r	numeric indicating the number of random sequences to be generated at random, or missing.
seed	a single value, interpreted as an integer, that specifies the seed for the random number generation.

Details

genSeq generates randomization sequences for a randomization procedure as defined by the input parameters. genSeq has two modes, according to the input.

- 1. genSeq(obj,r): gives r random sequences from the design specified by obj, along with the parameters stored in obj.
- 2. genSeq(obj): gives one random sequences from the design specified by obj, along with the parameters stored in obj.

The sequences are generated by using the Monte-Carlo sampling technique to sample from the true distribution of the sequences according to the randomization procedure specified by obj. The parameters of the randomization procedure are saved along with the sequences to ensure reproducibility of the results.

Value

An object inheriting from randSeq, representing the r randomization sequences generated at random for the specified randomization procedure. The output consists of the parameters used for the generation of the randomization sequences (see createParam) and the matrix M that stores the randomization sequences in its r rows. If r is missing, one sequence is generated by default.

Examples

```
# generate randomization sequences using Complete Randomization for N = 10
myPar <- crPar(10)
genSeq(myPar, 4)
genSeq(myPar)

# generate randomization sequences using the Random Allocation Rule for N = 10
myPar <- rarPar(10)
genSeq(myPar, 4)
genSeq(myPar)

# generate randomization sequences using the Maximal Procedure with mti = 2 and N = 10
myPar <- mpPar(10, 2)
genSeq(myPar, 4)
genSeq(myPar)</pre>
```

32 getDesFunc

getCorGuesses

Matrix of the guesses of the investigator

Description

Calculates the guesses of the investigator of a randomization list following the specified guessing strategy.

Usage

```
getCorGuesses(randSeq, guessing)
```

Arguments

randSeq object of the class randSeq. guessing object of the class corGuess.

Value

Matrix of the guesses of the investigator following the specified guessing strategy. No guess is abbreviated with "nG".

Examples

```
myPar <- bsdPar(10, 2)
M <- genSeq(myPar, 2)
type <- corGuess("CS")
getCorGuesses(M, type)</pre>
```

getDesFunc

Type of Desirability function

Description

Generates a character vector which specifies the used desirability function and its parameters

Usage

```
getDesFunc(obj)
## S4 method for signature 'derringerLs'
getDesFunc(obj)
## S4 method for signature 'derringerRs'
getDesFunc(obj)
```

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```
## S4 method for signature 'derringerTs'
getDesFunc(obj)
```

Arguments

obj

object of the class desFunc.

getDesign

Design of a randomization procedure

Description

Generates a character vector which specifies the used randomization method

Usage

```
getDesign(obj)
## S4 method for signature 'abcdPar'
getDesign(obj)
## S4 method for signature 'abcdSeq'
getDesign(obj)
## S4 method for signature 'bbcdPar'
getDesign(obj)
## S4 method for signature 'bbcdSeq'
getDesign(obj)
## S4 method for signature 'ebcPar'
getDesign(obj)
## S4 method for signature 'bsdPar'
getDesign(obj)
## S4 method for signature 'bsdSeq'
getDesign(obj)
## S4 method for signature 'chenPar'
getDesign(obj)
## S4 method for signature 'chenSeq'
getDesign(obj)
## S4 method for signature 'crPar'
```

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```
getDesign(obj)
## S4 method for signature 'crSeq'
getDesign(obj)
## S4 method for signature 'ebcSeq'
getDesign(obj)
## S4 method for signature 'gbcdPar'
getDesign(obj)
## S4 method for signature 'gbcdSeq'
getDesign(obj)
## S4 method for signature 'hadaPar'
getDesign(obj)
## S4 method for signature 'hadaSeq'
getDesign(obj)
## S4 method for signature 'mpPar'
getDesign(obj)
## S4 method for signature 'mpSeq'
getDesign(obj)
## S4 method for signature 'pbrPar'
getDesign(obj)
## S4 method for signature 'pbrSeq'
getDesign(obj)
## S4 method for signature 'rRtbdSeq'
getDesign(obj)
## S4 method for signature 'rRpbrSeq'
getDesign(obj)
## S4 method for signature 'rarPar'
getDesign(obj)
## S4 method for signature 'rarSeq'
getDesign(obj)
## S4 method for signature 'rpbrPar'
getDesign(obj)
## S4 method for signature 'tbdPar'
```

getDesScores 35

```
getDesign(obj)

## S4 method for signature 'rtbdPar'
getDesign(obj)

## S4 method for signature 'tbdSeq'
getDesign(obj)

## S4 method for signature 'udPar'
getDesign(obj)

## S4 method for signature 'udSeq'
getDesign(obj)
```

Arguments

obj

object of the class randSeq or randPar.

getDesScores

Applying desirability functions on issues of individual randomization sequences

Description

Applying desirability function on issues of individual randomization sequences.

Usage

```
getDesScores(assess, ..., weights)
## S4 method for signature 'assessment,missing'
getDesScores(assess, ..., weights)
## S4 method for signature 'assessment,numeric'
getDesScores(assess, ..., weights)
```

Arguments

assess object of class assessment.

... at least one object of class derFunc or a list of objects of the class derFunc.

weights weights for computing the geometric mean of several desirability scores. If missing, the issues are automatically equally weighted.

36 getExpectation

Details

Randomization sequences behave differently with respect to issues like selection bias, chronological bias, or loss in power estimation. The getDesScores function evaluates the behavior of randomization sequences with respect to these issues. The difference to the assess function is that it scales them to [0,1] and makes them easier interpretable. The first argument should be a result of the assess function. The second argument should be any number of derFunc objects that represent the desirability functions. The last argument weights may be provided if the desirability functions should be weighted differently.

Value

S4 object of class desirability summarizing the desirability of the randomization procedure.

See Also

```
Representation of randomization procedures: randPar

Generation of randomization sequences: genSeq

issues for the desirability of randomization sequences

Other desirability topics: derFunc, evaluate(), plotDes(), plotEv(), probUnDes()
```

Examples

```
# compute the desire-function for the full set of Random Allocation Rule for N = 4
sequences <- getAllSeq(rarPar(4))
issue1 <- corGuess("CS")
issue2 <- chronBias("linT", 0.25, "exact")
endp <- normEndp(mu = c(0,0), sigma = c(1,1))
A <- assess(sequences, issue1, issue2, endp = endp)
d1 <- derFunc(0.5, 0.75, 1)
d2 <- derFunc(0.05, 0.1, 1)

D1 <- getDesScores(A, d1, d2)
summary(D1)

D2 <- getDesScores(A, d1, d2, weights = c(3/4, 1/4))
summary(D2)</pre>
```

getExpectation

Get expectations of a randomization list

Description

Generates a matrix of the expectations of the included patients in the clinical trial.

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Usage

```
getExpectation(randSeq, issue, endp)
## S4 method for signature 'randSeq,missing,expEndp'
getExpectation(randSeq, endp)
## S4 method for signature 'randSeq,missing,normEndp'
getExpectation(randSeq, endp)
## S4 method for signature 'randSeq,power,normEndp'
getExpectation(randSeq, issue, endp)
## S4 method for signature 'randSeq,chronBias,normEndp'
getExpectation(randSeq, issue, endp)
## S4 method for signature 'randSeq,chronBias,expEndp'
getExpectation(randSeq, issue, endp)
## S4 method for signature 'randSeq,chronBias,missing'
getExpectation(randSeq, issue)
## S4 method for signature 'randSeq, selBias, normEndp'
getExpectation(randSeq, issue, endp)
## S4 method for signature 'randSeq, selBias, expEndp'
getExpectation(randSeq, issue, endp)
## S4 method for signature 'randSeq, selBias, missing'
getExpectation(randSeq, issue)
## S4 method for signature 'randSeq,combinedBias,normEndp'
getExpectation(randSeq, issue, endp)
## S4 method for signature 'randSeq,combinedBias,expEndp'
getExpectation(randSeq, issue, endp)
## S4 method for signature 'randSeq,combinedBiasStepTrend,normEndp'
getExpectation(randSeq, issue, endp)
## S4 method for signature 'randSeq,combinedBiasStepTrend,expEndp'
getExpectation(randSeq, issue, endp)
```

Arguments

randSeq object of the class randSeq.
issue object of the class issue (optional).

endp object of the class endpoint (optional).

38 getProbabilities

Details

It is assumed that the expectations of the included patients in a clinical trial can be influenced in three different ways:

- The strength of selection bias and the guessing strategy of the investigator (see selBias).
- The strength of a linear time trend, which is described by an object of the class chronBias.
- The expectations of the investigated treatment groups can be different (see e.g. normEndp).

Examples

```
# get Expectation for a normal endpoint
myPar <- bsdPar(10, 2)
M <- genSeq(myPar, 2)
cs <- selBias("CS", 2, "sim")
endp <- normEndp(mu = c(2, 2), sigma = c(1, 1))
getExpectation(M, cs, endp)

# get Expectation for an exponential endpoint
cs <- selBias("CS", 0.1 , "sim")
endp <- expEndp(lambda = c(0.5, 1), cenTime = 10, cenRate = 0.01)
getExpectation(M, cs, endp)</pre>
```

getProbabilities

Theoretical probability for randomization sequences

Description

Calculate theoretical probability for observed randomization sequences

Usage

```
getProb(obj)
## S4 method for signature 'abcdSeq'
getProb(obj)
## S4 method for signature 'bbcdSeq'
getProb(obj)
## S4 method for signature 'bsdSeq'
getProb(obj)
## S4 method for signature 'chenSeq'
getProb(obj)
## S4 method for signature 'chenSeq'
```

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```
getProb(obj)
## S4 method for signature 'ebcSeq'
getProb(obj)
## S4 method for signature 'gbcdSeq'
getProb(obj)
## S4 method for signature 'hadaSeq'
getProb(obj)
## S4 method for signature 'mpSeq'
getProb(obj)
## S4 method for signature 'pbrSeq'
getProb(obj)
## S4 method for signature 'rarSeq'
getProb(obj)
## S4 method for signature 'tbdSeq'
getProb(obj)
## S4 method for signature 'udSeq'
getProb(obj)
```

Arguments

obj

object of a class inheriting from randSeq. Formal representation of a randomization sequences together with the parameters that belong to the procedure that generated the sequences.

```
myPar <- bsdPar(10, 2)
M <- genSeq(myPar, 2)
getProb(M)

# all Sequences
par <- pbrPar(bc=c(2,2))
refSet <- getAllSeq(myPar)
probs <- getProb(refSet)

# sequences with probabilities
cbind(probs, refSet$M)</pre>
```

40 hadaPar

Description

Get the randomization list coded in its groups.

Usage

```
getRandList(obj)
```

Arguments

obj

object specifying the randomization procedure, see randPar or createParam.

Examples

```
myPar <- bsdPar(10, 2)
M <- genSeq(myPar, 2)
getRandList(M)</pre>
```

hadaPar

Representing Hadamard Randomization

Description

Represents the randomization procedure Hadamard Randomization.

Usage

```
hadaPar(N, groups = LETTERS[1:2])
```

Arguments

N integer for the total sample size of the trial.

groups character vector of labels for the different treatments.

Details

Hadamard randomization has been proposed by R.A. Bailey. The key idea is to use the columns of a special Hadamard Matrix as a randomization scheme. The implemented algorithm uses the Hadamard Matrix with N=12 columns proposed in the paper, see references.

Value

S4 object of the class hadaPar.

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Note

getProb and getAllSeq are currently only supported for hadaPar with total sample size N=12.

References

R.A. Bailey and P.R. Nelson (2003) Hadamard Randomization: A valid restriction of random permuted blocks. *Biometrical Journal*, **45**, 554-60.

See Also

Other randomization procedures: abcdPar, bbcdPar, bsdPar, chenPar, crPar, createParam(), ebcPar, gbcdPar, mpPar, pbrPar, rarPar, rpbrPar, rtbdPar, tbdPar, udPar

imbal

Representing the allocation imbalance

Description

Represents the imbalance of the treatment assignments of patients in a clinical trial.

Usage

imbal(type)

Arguments

type

character string, should be one of "imb", "absImb", "loss", or "maxImb", see Details.

Details

Balance of the treatment assignment of patients can be an issue in the design of a clinical trial. The imbal function is a constructor function for an S4 object of class imbal representing the issue of imbalance of a clinical trial. The parameter type can take the following values: The type

"imb" the final imbalance, i.e. difference in group sizes at the end of a trial

"absImb" the absolute value of the final imbalance

"loss" the loss in power estimation, i.e. imb^2/N

"maxImb" the maximal attained imbalance during the trial

Value

S4 object of class imbal, a formal representation of the issue of imbalance in a clinical trial.

References

A.C. Atkinson (2014) Selecting a biased coin design. Statistical Science, 29, Vol. 1, 144-163.

42 issue

See Also

Other issues: chronBias, combineBias(), corGuess, issue, selBias, setPower()

issue

Assessment criteria for clinical trials

Description

Summarizes the criteria for the assessment of randomization procedures.

Details

Randomization in clinical trials is supposed to control certain properties in clinical trials. In the randomizeR package, these properties are called issues. It is crucial to decide which of the issues is relevant in the present clinical trial, because a randomization procedure that manages well one issue might behave very badly for another. The issues include

- Selection bias can occur if future treatment allocations are predictable due to restricted randomization and unmasking of past treatment assignments. The influence of selection bias on the test decision is represented by the selBias class. The measure for the predictability of a randomization procedure is implemented in the corGuess class representing the expected number of correct guesses.
- Chronological bias can occur if a time trend is present in the data. Time trends occur due to learning curves, relaxed inclusion/ exclusion criteria or new co-medication. Chronological bias is represented by the chronBias class.
- Additive combination of chronological and selection bias may occur if a time trend and selection bias are present in the data. The combined bias is represented by the combineBias class.
- Balance is important in order to ensure proper power estimation properties of the treatments. However, a high degree of balance favors selection bias. Depending on the clinical context, a randomization procedure should be chosen that admits a suitable imbalance. Imbalance bias is represented by the imbal class. The power loss due to imbalance can be assessed directly via the setPower class

See Also

Representation of randomization procedures: randPar

Generation of randomization sequences: genSeq
Assessment of randomization sequences: assess
Comparison of randomization sequences: compare

Other issues: chronBias, combineBias(), corGuess, imbal, selBias, setPower()

K 43

Κ

Function returning the total sample size slot of an S4 object

Description

Function returning the total sample size slot of an S4 object

Usage

K(obj)

Arguments

obj

object of class randPar

lambda

Method returning the rate parameter of an expEndp S4 object

Description

Method returning the rate parameter of an expEndp S4 object

Usage

lambda(obj)

Arguments

obj

object of class expEndp

method

Function returning the method of an S4 object

Description

Function returning the method of an S4 object

Usage

method(obj)

Arguments

obj

object inheriting from randPar

mpPar

senting Maximal Procedure

Description

Represents the Maximal Procedure.

Usage

```
mpPar(N, mti, ratio = c(1, 1), groups = LETTERS[1:2])
```

Arguments

N	integer for the total sample size of the trial.
mti	maximum tolerated imbalance in patient numbers during the trial.
ratio	vector of length K. The total sample number N and all used block lengths (bc) have to be divisible by sum(ratio).
groups	character vector of labels for the different treatments.

Details

Fix the total sample size N and the mti. Afterwards, the patients are assigned to each treatment arm according to the ratio. All randomization sequences are equiprobable.

Value

S4 object of the class mpPar.

References

V.W. Berger, A. Ivanova and M.D. Knoll (2003) Minimizing predictability while retaining balance through the use of less restrictive randomization procedures. *Statistics in Medicine*, **19**, 3017-28.

See Also

Other randomization procedures: abcdPar, bbcdPar, bsdPar, chenPar, crPar, createParam(), ebcPar, gbcdPar, hadaPar, pbrPar, rarPar, rpbrPar, rtbdPar, tbdPar, udPar

mti 45

mti

Function returning the MTI slot of an S4 object

Description

Function returning the MTI slot of an S4 object

Usage

mti(obj)

Arguments

obj

object of class bsdPar or mpPar

mu

Access the expectation value slot of a normEndp S4 object

Description

Access the expectation value slot of a normEndp S4 object

Usage

mu(obj)

Arguments

obj

object of class normEndp

Ν

Function returning the sample size slot of an S4 object

Description

Function returning the sample size slot of an S4 object

Usage

N(obj)

Arguments

obj

object inheriting from randPar

46 overview

normEndp	Representation of normally distributed endpoints	

Description

Represents normally distributed endpoints in clinical trials.

Usage

```
normEndp(mu, sigma)
```

Arguments

mu vector of the expected responses of the treatment groups, should have length K

(i.e. one entry for each treatment group).

sigma vector of the standard deviations in each treatment group, should have length K

(i.e. one entry for each treatment group).

Details

The normEnd function is a constructor function for an S4 object of the class normEnd representing a normally distributed endpoint in a clinical trial. In conjunction with the assess function, normal endpoints admit the calculation of the exact type-I-error probability and power.

See Also

Compute exact or simulated type-I-error: assess.

Other endpoint types: expEndp, survEndp

Examples

```
# set the parameters of two normally distributed endpoints endp <- normEndp(mu = c(1, 2), sigma = c(1, 1))
```

overview

Overview over the parameters used in the randomizeR package

Description

This list of parameters yields a comprehensive overview of the parameters used in the randomizeR package.

overview 47

Arguments

a nonnegative parameter which controls the degree of randomness: For decreasing

a the allocations become deterministic, while for increasing a the randomization

procedure tends to complete randomization.

accrualTime duration of the accrual period in a survival study.

add integer representing the number of balls that are added to the urn in each step.

alpha the significance level of the test in each simulation.

be vector which contains the lengths k_1, \ldots, k_l of each block. This means that

the vector bc will have one entry for each block.

b numeric vector of length at most 2 specifying the weight(s) for the punishment

of deviations from the target value.

cenRate exponential censoring rate in a survival study.

cenTime total duration of a survival study (maximum length of followup).

d effect size.

df degrees of freedom (i.a. N-2).

eta numeric specifying the magnitude of selection bias.

file A connection, or a character string naming the file to write to.

filledBlock logical whether the last block should be filled or not.

FTI final tolerated imbalance. This is the difference in number of patients of groups

A and B that is permitted at the end of a trial. Usually this is set to zero.

groups character vector of labels for the different treatments.

ini integer representing the initial urn composition.

k length of the block to be permuted. k should be divisible by the number of

treatment arms.

K number of treatment groups (e.g. K=2 if we compare one experimental against

one control treatment).

lb lower bound for the starting value of the poisson distribution.

lambda vector of the exponential rate parameters in each treatment group.

method method that is used to generate the (random) allocation sequence. It can take

values PBR, RAR, HAD, PWR, EBC, BSD, CR, TBD, UD, and MP.

mti maximum tolerated imbalance in patient numbers during the trial.

mu vector of the expected responses of the treatment groups, should have length K

(i.e. one entry for each treatment group).

N integer for the total sample size of the trial.

name of a variable.

obj object specifying the randomization procedure, see randPar or createParam.

object any R object.

p success probability of the biased coin (e.g. in Efron's Biased Coin Design).

pr vector with patient responses, i.e. each patients resulting value after the treat-

ment.

48 overview

"cut-off" value in [0.5,1]. This is the ratio of patients up from which the q experimenter imposes selection bias on the data. numeric indicating the number of random sequences to be generated at random, or missing. vector of length K. The total sample number N and all used block lengths (bc) ratio have to be divisible by sum(ratio). rb block lengths of the blocks that can be selected equiprobable at random. rho nonnegative parameter which my be adjusted according to how strongly it is desired to balance the experiment. If rho = 1, we have Wei's urn design with alpha = 0. If rho = 0, we have complete randomization. randomization sequence (of one block). rsob randomization sequence (of all blocks). rs matrix for the computation of the probabilities in the maximal procedure. S saltus integer or missing specifying the patient index (i.e. position) of the step in case of step time trend. seed a single value, interpreted as an integer, that specifies the seed for the random number generation. vector of the standard deviations in each treatment group, should have length K sigma (i.e. one entry for each treatment group). SLs numeric vector of length at most 2 specifying the lower and/or upper specified border. theta factor of the time trend for further details see type. character vector indicating which biasing strategy the experimenter is using (setype lection bias) and which other bias is present in the clinical trial (e.g. time trend). All biases included in the vector are combined (i.e. added up) to form the total bias. Possible values are "none" (if no bias occurs), "CS" (resp. "DS") (if the experimenter uses the convergence (resp. divergence) strategy to invoke selection bias), LinT for linear time trend, LogT for log-linear time trend, StepT for step time trend, SigT for sigmoid time trend, PWR for knowledge of all up to the first observation in each block, MTI the next observation after reaching the maximal tolerated imbalance is reached will be known to the physician. T۷ numeric specifying the optimal desired value called the target value. upper bound for the last value of the poisson distribution. ub

logical parameter for the t.test: Shall the variances be treated as equal (TRUE=

t.test) or different (FALSE= Welch.test).

a variable x.

varEq

Х

pbrPar 49

pbrPar	Representing Permuted Block Randomization	

Description

Represents the randomization procedure Permuted Block Randomization.

Usage

```
pbrPar(bc, K = 2, ratio = rep(1, K), groups = LETTERS[1:K])
```

Arguments

bc	vector which contains the lengths k_1, \ldots, k_l of each block. This means that the vector bc will have one entry for each block.
K	number of treatment groups (e.g. K=2 if we compare one experimental against one control treatment).
ratio	vector of length K. The total sample number N and all used block lengths (bc) have to be divisible by sum(ratio).
groups	character vector of labels for the different treatments.

Details

Fix the block constellation bc, the number of treatment groups K, and the vector of the ratio. Afterwards, in each block the patients are assigned according to the ratio to the corresponding treatment groups. All generated randomization sequences are equiprobable.

Value

S4 object of the class pbrPar.

References

W. F. Rosenberger and J. M. Lachin (2002) Randomization in Clinical Trials. Wiley.

See Also

```
Other randomization procedures: abcdPar, bbcdPar, bsdPar, chenPar, crPar, createParam(), ebcPar, gbcdPar, hadaPar, mpPar, rarPar, rpbrPar, rtbdPar, tbdPar, udPar
```

50 plot

plot

Generic plotting of comparison objects

Description

Generic plotting of comparison objects

Usage

```
plot(x, y, ...)
## S4 method for signature 'comparison, character'
plot(x, y)
## S4 method for signature 'comparison, missing'
plot(x, y)
```

Arguments

```
x object of class comparison.
y character "boxplot", or "violin", or "missing".
... "missing"
```

Details

Creates a box- or violinplot of an object x of the class comparison.

Value

A plot created with the additional package ggplot2.

See Also

compare for creating S4 objects of the class comparison

```
# compare Random Allocation Rule and Big Stick for N = 4 with respect to
# correct guesses
RAR <- getAllSeq(rarPar(4))
BSD <- getAllSeq(bsdPar(4, mti = 2))
corGuess <- corGuess("CS")
comp <- compare(corGuess, RAR, BSD)
plot(comp)</pre>
```

plotDes 51

desScore plotting

Description

Plot of an desScore object.

Usage

```
plotDes(desScore, labels, colAv = "red", quantiles = FALSE)
```

Arguments

desScore object of type desScore.

labels labels used in the plot. Can be NULL.

colAv color of the line representing the average of the desirability scores in the plot.

quantiles logical whether the quantiles should be depicted in the plot.

See Also

```
Other desirability topics: derFunc, evaluate(), getDesScores(), plotEv(), probUnDes()
```

```
# compute the desirability scores of the full set of PBR(4)
sequences <- getAllSeq(rarPar(4))
issue1 <- corGuess("CS")
issue2 <- chronBias("linT", 1/4, "exact")
endp <- normEndp(mu = c(0,0), sigma = c(1,1))
A <- assess(sequences, issue1, issue2, endp = endp)
d1 <- derFunc(0.5, 0.75, 1)
d2 <- derFunc(0.05, 0.1, 1)

D <- getDesScores(A, d1, d2)
summary(D)
plotDes(D)
plotDes(D, quantiles = TRUE)</pre>
```

52 plotEv

plotEv

Evaluation plotting

Description

Plot of an evaluation object.

Usage

```
plotEv(evaluation, labels, cols)
```

Arguments

evaluation object of type evaluation.

labels labels used in the plot. Can be NULL.

cols colors of the lines representing the desirability scores in the plot. Can be NULL.

See Also

Other desirability topics: derFunc, evaluate(), getDesScores(), plotDes(), probUnDes()

```
# compare Random Allocation Rule to Big Stick Design with respect to different issues
# and their corresponding desirability functions
issue1 <- corGuess("CS")
issue2 <- chronBias(type = "linT", theta = 1/4, method = "exact")
RAR <- getAllSeq(rarPar(4))
BSD <- getAllSeq(bsdPar(4, mti = 2))
A1 <- assess(RAR, issue1, issue2, endp = normEndp(c(0,0), c(1,1)))
A2 <- assess(BSD, issue1, issue2, endp = normEndp(c(0,0), c(1,1)))
d1 <- derFunc(TV = 0.5, 0.75, 2)
d2 <- derFunc(0.05, c(0, 0.1), c(1, 1))
DesScore <- getDesScores(A1, d1, d2, weights = c(5/6, 1/6))
DesScore2 <- getDesScores(A2, d1, d2, weights = c(5/6, 1/6))
E <- evaluate(DesScore, DesScore2)
plotEv(E)</pre>
```

plotSeq 53

Description

Plot all randomization sequences of a randSeq object

Usage

```
plotSeq(sequences, plotAllSeq = FALSE, emph = NA, rs = NA)
```

Arguments

sequences object of type randSeq

plotAllSeq logical. If plotAllSeq=TRUE, the complete set of randomization sequences will

be plotted in light gray.

emph integer indicating which sequence should be highlighted in blue.

rs vector of a randomization sequence that should be highlighted.

probUnDes Computing the probability of having desirability scores of zero

Description

Computing the probability of having desirability scores of zero for each desirability function applied to an issue.

Usage

```
probUnDes(desScore)
## S4 method for signature 'desScores'
probUnDes(desScore)
```

Arguments

desScore an object of the class desScores, i.e. an object resulting from applying the

function getDesScores

Details

The function probUnDes expects an object that results from the getDesScores function. For each issue it computes the probability that it achieves an undesirable score, i.e. a desirability score of 0. In doing so, it weights the zero desirability scores with the probability that the sequence occurs.

54 randBlocks

Value

S4 object of class probUnDesirable computing the probability of getting undesirable scores, i.e. desirability scores of 0.

See Also

```
Representation of randomization procedures: randPar

Generation of randomization sequences: genSeq

issues for the desirability of randomization sequences
```

Other desirability topics: derFunc, evaluate(), getDesScores(), plotDes(), plotEv()

Examples

```
# compare Random Allocation Rule to Big Stick Design with respect to different issues
# and their corresponding desirability functions
RAR <- getAllSeq(rarPar(4))
issue1 <- corGuess("CS")
issue2 <- corGuess("DS")
A1 <- assess(RAR, issue1, issue2)

d1 <- derFunc(TV = 0.1, 0.7, 2)
d2 <- derFunc(0.5, c(0.3, 0.8), c(1, 1))
DesScore <- getDesScores(A1, d1, d2, weights = c(5/6, 1/6))
probUnDes(DesScore)</pre>
```

randBlocks

Function returning the block slot of an S4 object

Description

Function returning the block slot of an S4 object

Usage

```
randBlocks(obj)
```

Arguments

obj

object of class pbrPAr

randPar 55

randPar

Settings for randomization procedures

Description

Randomization procedures in randomizeR are represented by objects that inherit from randPar. The representation can then be used in order to generate randomization sequences. In order generate a representation of a randomization procedure, call createParam or one of the following functions.

Supported randomization procedures

- Complete Randomization (crPar)
- Random Allocation Rule (rarPar)
- Permuted Block Randomization (pbrPar)
- Permuted Block Randomization with random block length (rpbrPar)
- Truncated Binomial Design (tbdPar)
- Truncated Binomial Design with random block length (rtbdPar)
- Efron's Biased Coin Design (ebcPar)
- Big Stick Design (bsdPar)
- Maximal Procedure (mpPar)
- Wei's Urn Design (udPar)
- Chen's Design (chenPar)
- Generalized Biased Coin Design (gbcdPar)
- Accelerated Biased Coin Design (abcdPar)
- Bayesian Biased Coin Design (bbcdPar)
- Hadamard Randomization (hadaPar)

See Also

Generate randomization sequences genSeq. Calculate the the complete set of randomization sequences of a randomization procedure. getAllSeq.

56 rarPar

randSeq-class	An S4 Class for the representation of randomization sequences

Description

This set of classes provides functionality of storing randomization sequences of different randomization procedures along with the parameters representing the design.

Slots

N total number of patients included in the trial

M matrix containing randomization sequences of length N in its rows.

K number of treatment groups

groups character string of length K defining the names of the treatment groups

Description

Represents the randomization procedure Random Allocation Rule.

Usage

```
rarPar(N, K = 2, ratio = rep(1, K), groups = LETTERS[1:K])
```

Arguments

N	integer for the total sample size of the trial.
K	number of treatment groups (e.g. K=2 if we compare one experimental against one control treatment).
ratio	vector of length K. The total sample number N and all used block lengths (bc) have to be divisible by sum(ratio).
groups	character vector of labels for the different treatments.

Details

Fix a total sample size N the number of treatment groups K, and the vector of the ratio. Afterwards, all patients are assigned according to the ratio to the corresponding treatment groups. All randomization sequences are equiprobable.

Value

S4 object of the class rarPar.

ratio 57

References

W. F. Rosenberger and J. M. Lachin (2002) Randomization in Clinical Trials. Wiley.

See Also

Other randomization procedures: abcdPar, bbcdPar, bsdPar, chenPar, crPar, createParam(), ebcPar, gbcdPar, hadaPar, mpPar, pbrPar, rpbrPar, rtbdPar, tbdPar, udPar

ratio

Function returning the allocation ratio slot of an S4 object

Description

Function returning the allocation ratio slot of an S4 object

Usage

```
ratio(obj)
```

Arguments

obj

object of class randPar

rho

Function returning the adjusting parameter rho slot of an S4 object

Description

Function returning the adjusting parameter rho slot of an S4 object

Usage

rho(obj)

Arguments

obj

object of class randPar

58 rpbrPar

rpbrPar	Representing Randomized Permuted Block Randomization
ι μυτι αι	Representing Randomized Fermited Block Randomization

Description

Represents the randomization procedure Randomized Permuted Block Randomization.

Usage

```
rpbrPar(
   N,
   rb,
   K = 2,
   ratio = rep(1, K),
   groups = LETTERS[1:K],
   filledBlock = FALSE
)
```

Arguments

N	integer for the total sample size of the trial.
rb	block lengths of the blocks that can be selected equiprobable at random.
K	number of treatment groups (e.g. K=2 if we compare one experimental against one control treatment).
ratio	vector of length K. The total sample number N and all used block lengths (bc) have to be divisible by sum(ratio).
groups	character vector of labels for the different treatments.
filledBlock	logical whether the last block should be filled or not.

Details

Fix the possible random block lengths rb, the number of treatment groups K, the sample size N and the vector of the ratio. Afterwards, one block length is randomly selected of the random block lengths. The patients are assigned according to the ratio to the corresponding treatment groups. This procedure is repeated until N patients are assigned. Within each block all possible randomization sequences are equiprobable.

Value

S4 object of the class rpbrPar.

References

W. F. Rosenberger and J. M. Lachin (2002) Randomization in Clinical Trials. Wiley.

rtbdPar 59

See Also

Other randomization procedures: abcdPar, bbcdPar, bsdPar, chenPar, crPar, createParam(), ebcPar, gbcdPar, hadaPar, mpPar, pbrPar, rarPar, rtbdPar, tbdPar, udPar

rtbdPar

Representing Randomized Truncated Binomial Design

Description

Represents the randomization procedure Randomized Truncated Binomial Design.

Usage

```
rtbdPar(N, rb = N, groups = LETTERS[1:2], filledBlock = FALSE)
```

Arguments

N integer for the total sample size of the trial.

rb block lengths of the blocks that can be selected equiprobable at random.

groups character vector of labels for the different treatments.

filledBlock logical whether the last block should be filled or not.

Details

Fix the possible random block lengths rb and the sample size of the trial N. Afterwards, one block length is randomly selected of the random block lengths. In this block a fair coin is tossed for the patient assignments until half of the patients have been assigned to one of the treatment arms. Afterwards, the block is filled with the other treatment. This procedure is repeated until N patients are assigned.

Value

S4 object of the class rtbdPar.

References

W. F. Rosenberger and J. M. Lachin (2002) Randomization in Clinical Trials. Wiley.

See Also

```
Other randomization procedures: abcdPar, bbcdPar, bsdPar, chenPar, crPar, createParam(), ebcPar, gbcdPar, hadaPar, mpPar, pbrPar, rarPar, rpbrPar, tbdPar, udPar
```

60 saveRand

saveAssess

Saving an assess object

Description

Saves the full information of an assess object in a .csv data sheet.

Usage

```
saveAssess(obj, file = "assessObject.csv")
```

Arguments

obj object of class assessment, e.g. the output of the assess function.

file A connection, or a character string naming the file to write to.

Value

Creates a .csv data in the home folder.

See Also

Other saving functions: saveRand()

saveRand

Saving a randomization lists

Description

Saves the parameters of a randSeq object in a .csv data sheet.

Usage

```
saveRand(obj, file = "randList.csv")
```

Arguments

obj object of class randSeq containing a single randomization sequence.

file A connection, or a character string naming the file to write to.

Value

Creates a .csv data in the home folder and saves the randomization list as a column vector.

See Also

Other saving functions: saveAssess()

seed 61

seed	Function returning the allocation seed slot of an object	

Description

Returns the seed that was either generated at random or user specified. The seed can be specified for any random operation e.g. genSeq.

Usage

```
seed(obj)
```

Arguments

obj object specifying the randomization procedure, see randPar or createParam.

selBias Representing selection bias

Description

Represents the issue of selection bias in a clinical trial.

Usage

```
selBias(type, eta, method, alpha = 0.05)
```

Arguments

type character string, should be one of "CS", "CS2" or "DS", see Details.

eta numeric specifying the magnitude of selection bias.

method character string, should be one of "sim" or "exact", see Details.

alpha significance level.

Details

Selection bias can be an issue in the design of a clinical trial. The selBias function is a constructor function for an S4 object of the class selBias representing the issue of third order selection bias in a clinical trial. It supports two possible modes, method="sim" and method="exact". This representation is particularly useful in interaction with the assess function.

method="sim" Represents the simulated type-I-error rate given the level alpha, the selection effect eta and the biasing strategy type. When calling assess for a selBias object with method="sim", one test decision is computed for each sequence of randSeq. The type-I-error rate (power) is the proportion of falsely (correctly) rejected null hypotheses.

62 selBias

method="exact" Represents the exact type-I-error probability given the level alpha, the selection effect eta and the biasing strategy type. When calling assess for a selBias object with method="exact", the p-value of each randomization sequence is computed. For normal endpoints and two treatment groups these p-values are exact values which can be calculated from the sum of the corresponding quantiles of the doubly noncentral t-distribution. For more than two treatment groups, exact p-values are computed using a doubly noncentral F distribution. For exponential endpoints the p-values are obtained using an approximation formula.

It also supports three types of selection bias:

- type="DS" Refers to the divergence strategy according to Blackwell and Hodges (1957). Under this guessing strategy, the investigator guesses that the upcoming treatment is the one that has so far been allocated *more* frequently.
- type="CS" Refers to the convergence strategy according to Blackwell and Hodges (1957). Under this guessing strategy, the investigator guesses that the upcoming treatment is the one that has so far been allocated *less* frequently. In multi-arm trials, type="CS" refers to the first generalization of the convergence strategy according to Uschner et al (2018). The investigator guesses the treatment that had been allocated less frequently whenever all the treatments of the opposite group are larger than the smallest of the present group.
- type="CS2" In trials with two treatment arms, type="CS2" is equivalent to type="CS". In multiarm trials, type="CS2" refers to the second generalization of convergence strategy according to Uschner et al (2018). The investigator guesses the treatment that had been allocated less frequently whenever all the treatments of the opposite group are larger than the smallest of the present group.

Value

S4 object of class selBias, a formal representation of the issue of selection bias in a clinical trial.

References

- D. Blackwell and J.L. Hodges Jr. (1957) Design for the control of selection bias. *Annals of Mathematical Statistics*, **25**, 449-60.
- M. Proschan (1994) Influence of selection bias on the type-I-error rate under random permuted block designs. *Statistica Sinica*, **4**, 219-31.
- D. Uschner, R.-D. Hilgers, N. Heussen (2018) The impact of selection bias in randomized multi-arm parallel group clinical trials *PLOS ONE*, **13**(1), 1-18.

See Also

Compute exact or simulated rejection probability: assess.

Other issues: chronBias, combineBias(), corGuess, imbal, issue, setPower()

```
# create a selection bias of the convergency strategy type with eta = 0.25 for which
# the exact rejection probabilities are calculated
sbias <- selBias("CS", 0.25, "exact")</pre>
```

setPower 63

setPower Representing the power

Description

Represents the expected power of the individual randomization sequences.

Usage

```
setPower(d, method, alpha = 0.05)
```

Arguments

d effect size.

method character string, should be one of "sim" or "exact", see Description.

alpha significance level.

Details

The attained power of an individual randomization sequence can be an issue in the design of a clinical trial. The power of a randomization sequence is computed depending on the effect size d and the difference in group sizes.

If method="sim", the object represents the simulated power of an individual randomization sequence. When calling assess for a power object with method="sim", one test decision is computed for each randomization sequence of randSeq. The power is the proportion of falsely (correctly) rejected null hypotheses.

If method="exact", the object represents the exact power of an individual randomization sequence. When calling assess for a power object with method="exact", the exact *p*-value of each randomization sequence is computed. So far, this is only supported for normal endpoints. Then the power is the sum of the corresponding quantiles of the noncentral t-distribution.

Value

S4 object of class power, a formal representation of the issue of power in a clinical trial.

See Also

Other issues: chronBias, combineBias(), corGuess, imbal, issue, selBias

64 summary

sigma

Function returning the standard deviation slot of a normEndp S4 object

Description

Function returning the standard deviation slot of a normEndp S4 object

Usage

```
sigma(obj)
```

Arguments

obj

object of class normEndp

summary

Summary of assessments of a randomization procedure

Description

Summary of assessments of a randomization procedure

Summary of desirability scores of a randomization procedure

Usage

```
summary(object, ...)
## S4 method for signature 'assessment'
summary(object)

summary(object, ...)
## S4 method for signature 'desScores'
summary(object)
```

Arguments

```
object assessment object.
```

. . . additional arguments affecting the summary that will be produced.

survEndp 65

Details

For each issue the assessment of the sequences is summarized to permit a design-based assessment of the randomization procedure. This approach uses the sequence-wise values of the assessment and the probabilities in order to give an overall summary.

For each issue the desirability score of the sequences is summarized to permit a design-based desirability score of the randomization procedure. This approach uses the sequence-wise values of the desirability and the probabilities in order to give an overall summary.

Value

Data frame with a summary of the assessment object.

Data frame with a summary of the desirability scores object.

Examples

```
# assess the full set of PBR(4)
seq <- getAllSeq(pbrPar(4))
issue <- corGuess("CS")
A <- assess(seq, issue)
summary(A)

# compute the desirability scores of the full set of PBR(4)
seq <- getAllSeq(pbrPar(4))
issue1 <- corGuess("CS")
issue2 <- corGuess("DS")
A <- assess(seq, issue1, issue2)
d1 <- derFunc(0.5, c(0.1, 0.8), c(1, 1))
d2 <- derFunc(0.1, 0.7, 2)
D <- getDesScores(A, d1, d2, weights = c(5/6, 1/6))
summary(D)</pre>
```

survEndp

Representation of survival endpoints

Description

Represents survival endpoints in clinical trials.

Usage

```
survEndp(cenRate, accrualTime, cenTime)
```

Arguments

cenRate exponential censoring rate in a survival study.

accrualTime duration of the accrual period in a survival study.

cenTime total duration of a survival study (maximum length of followup).

66 tbdPar

Details

The survEnd function is a constructor function for an S4 object of the class survEnd representing a survival endpoint in a clinical trial.

See Also

Other endpoint types: expEndp, normEndp

tbdPar

Representing Truncated Binomal Design

Description

Represents the Truncated Binomial Design.

Usage

```
tbdPar(bc = N, groups = LETTERS[1:2])
```

Arguments

bc vector which contains the lengths k_1, \ldots, k_l of each block. This means that

the vector bc will have one entry for each block.

groups character vector of labels for the different treatments.

Details

A fair coin is tossed until half of the patients have been assigned to one of the treatment arms. Afterwards, the randomization list is filled with the other treatment.

Value

S4 object of the class tbdPar.

References

W. F. Rosenberger and J. M. Lachin (2002) Randomization in Clinical Trials. Wiley.

See Also

```
Other randomization procedures: abcdPar, bbcdPar, bsdPar, chenPar, crPar, createParam(), ebcPar, gbcdPar, hadaPar, mpPar, pbrPar, rarPar, rpbrPar, rtbdPar, udPar
```

TV 67

ΤV

Function returning the target value slot of an S4 object

Description

Function returning the target value slot of an S4 object

Usage

TV(obj)

Arguments

obj

object inheriting from derFunc

type

Get type of an object

Description

Accesses the type slot of an S4 object

Usage

```
type(obj)
```

Arguments

obj

a bias object (i.e. S4 object inheriting from bias)

Value

Character string specifying the type of bias obj represents, e.g. "linT" in case of chronological bias.

68 udPar

udPar	Representing Wei's Urn Design	
udPar	Representing Wei's Urn Design	

Description

Represents Wei's Urn Design.

Usage

```
udPar(N, ini, add, groups = LETTERS[1:2])
```

Arguments

N integer for the total sample size of the trial.

ini integer representing the initial urn composition.

add integer representing the number of balls that are added to the urn in each step.

groups character vector of labels for the different treatments.

Details

An urn is filled with a number of ini balls of both of the treatments. Afterwards, a ball is drawn randomly from the urn. Finally, add balls are added to the urn from the opposite treatment. This procedure is repeated until N patients are assigned.

Value

S4 object of the class udPar.

References

L.J. Wei (1977) A Class of Designs for Sequential Clinical Trials. *Journal of the American Statistical Association*, **72**, 382-6.

See Also

```
Other randomization procedures: abcdPar, bbcdPar, bsdPar, chenPar, crPar, createParam(), ebcPar, gbcdPar, hadaPar, mpPar, pbrPar, rarPar, rpbrPar, rtbdPar, tbdPar
```

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