

# Package ‘scpm’

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**Author** Mario A. Martinez Araya [aut,cre,cph]

**Maintainer** Mario A. Martinez Araya <r@marioma.me>

**Description** Group of functions for spatial smoothing using cubic splines and variogram maximum likelihood estimation. Also allow the inclusion of linear parametric terms and change-points for segmented smoothing splines models.

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scpm-package	<i>'An R Package for Spatial Smoothing'</i>
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## Description

Group of functions for spatial smoothing using cubic splines and variogram maximum likelihood estimation. Also allow the inclusion of linear parametric terms and change-points for segmented smoothing splines models.

## Author(s)

Mario A. Martinez Araya [aut,cre,cph]

## Examples

```

data(landim1, package = "scpm")
if(FALSE){
  library(scpm)
  ##create tthe dataset
  d <- as.sss(landim1, coords = NULL, coords.col = 1:2, data.col = 3:4)
  ##fitting spatial linear model with response A and covariate B
  ##Gneiting covariance function in the errors
  m0 <- scp(A ~ linear(~ B), data = d, model = "RMgneiting")
  ##adding a bivariate cubic spline based on the coordinates
  m1 <- scp(A ~ linear(~ B) + s2D(penalty = "cs"), data = d, model = "RMgneiting")
  ##plotting observed and estimated field from each model
  par(mfrow=c(2,2))
  plot(m0, what = "obs", type = "persp", main = "Model null - y")
  plot(m0, what = "fit", type = "persp", main = "Model null - fit")
  plot(m1, what = "obs", type = "persp", main = "Model alternative - y")
  plot(m1, what = "fit", type = "persp", main = "Model alternative - fit")
  ##plotting the estimated semivariogram from each model
  par(mfrow=c(1,2))
  Variogram(m0,main="Semivariogram - model null", ylim = c(0,0.7))
  Variogram(m1,main="Semivariogram - model alternative", ylim = c(0,0.7))
  ##summary of the estimated coefficients
  summary(m0)
  summary(m1)
  ##some information criteria
  AIC(m0)
  AIC(m1)

```

```

AICm(m0)
AICm(m1)
AICc(m0)
AICc(m1)
BIC(m0)
BIC(m1)
}

```

---

A1. Create sss data     *Convert an object to the class 'sss' for spatial smoothing splines*

---

### Description

Create a matrix or data.frame to a valid dataset of class 'sss' for spatial smoothing splines. Those dataset can be used later by functions [s2D](#) for tensor product (natural) cubic splines or p-splines, and [scp](#) for estimating spatial smoothing splines models.

### Usage

```

as.sss(X, coords, coords.col, data.col, ...)
create.sss(coords, data, ...)
is.sss(x)
sss2df(x)

```

### Arguments

<code>X</code>	a matrix or data-frame. Every row must correspond to a point location in a two-dimensional space (coordinates). Coordinates columns can be included in <code>X</code> or defined separately using the argument <code>coords</code> . Some columns can also correspond to variables measured at the different point locations.
<code>coords</code>	two-columns numeric matrix of coordinates (optional).
<code>data</code>	a data-frame containing the variables measured at the locations given by <code>coords</code> .
<code>coords.col</code>	numeric vector. The number of columns in <code>X</code> that contains the coordinates.
<code>data.col</code>	numeric vector. The number of columns in <code>X</code> that contains variables measured at the points locations.
<code>...</code>	slots elements to create a new <code>sss</code> dataset. Required slots are <code>data</code> , <code>coords</code> , <code>grid</code> , <code>knots</code> , <code>W</code> , <code>contract</code> (to be discarded in the future), and <code>regular</code> . See <i>Value</i> for an explanation about each slot requirements.
<code>x</code>	an object to check validity as member of class <code>sss</code> .

### Value

**data** a data-frame containing the variables measured at the locations given by `coords`.  
**coords** a matrix containing the two columns of observed coordinates for the data.  
**grid** a grid matrix containing the two columns of coordinates.

**knots** a named list with the design points (knots) in every coordinate. Equivalent to a `grid.list` object.

**W** a spatial incidence matrix. If `contract=TRUE` it is  $W_{ij}$ , otherwise  $W_{ji}$ .

**contract** logical. The same value as the argument `contract`.

**regular** logical. If the coordinates are observed at regular points it is TRUE, FALSE otherwise (missing coordinates in any direction).

### Author(s)

Mario A. Martinez Araya, <r@marionoma.me>

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## A2. Define linear terms

### *Linear components of the mean of the model*

---

### Description

Define parametric components of the mean as linear terms.

### Usage

```
linear(formula, data = NULL, contrasts = NULL, intercept = FALSE)
```

### Arguments

<code>formula</code>	formula expression. A formula expression as described in <a href="#">formula</a> .
<code>data</code>	data frame. Where to search for the covariates?
<code>contrasts</code>	character. A contrast method for factor covariates. Default to <code>'contr.treatment'</code> .
<code>intercept</code>	logical. TRUE to include an intercept term, FALSE otherwise (default).

### Author(s)

Mario A. Martinez Araya, <r@marionoma.me>

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A3. Define unknown changes

*Changes in the pattern of response*


---

**Description**

Define unknown changes in the pattern of response to be estimated.

**Usage**

```
cp(x, psi, data = NULL, groups = NULL, contrasts = NULL,
   only.UV = FALSE)
```

**Arguments**

x	numeric vector. Covariate over which range define unknown change-points.
psi	numeric vector. Starting values for the change-points.
data	data frame. Where to search for the covariate?
groups	not used at the moment. To be implemented.
contrasts	character. A contrast method for factor covariates in groups. Default to 'contr.treatment'.
only.UV	logical. Not required.

**Author(s)**

Mario A. Martinez Araya, <r@marioma.me>

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A4. Define bivariate Spline

*Bivariate spline*


---

**Description**

Define a bivariate spline using tensor products or thin plate splines.

**Usage**

```
s2D(data = NULL, penalty = c("none", "cs", "ps", "tps"),
     is.X = c("none", "tensor", "tps"), intercept = TRUE,
     ps.order = 2, aniso.angle = 0, aniso.ratio = 1,
     env = .GlobalEnv, ...)
```

**Arguments**

data	sss object. Data of class sss generated by <a href="#">as.sss</a> or <a href="#">create.sss</a> .
penalty	character. Type of spline to use and penalty to define. One of 'cs' or 'ps' for cubic splines based on tensor products, 'tps' for thin plate splines or 'none'. 'cs' define the penalty based on roughness matrices of natural cubic splines while 'ps' define the penalty based on differences of order ps.order. See <a href="#">scp</a> . If penalty="none" then no spline nor penalty are defined and the model for the spatial surface is defined by is.X.
is.X	character. Model for the spatial surface. One of 'tensor', 'tps' or 'none'. Only required if penalty="none". See details.
intercept	logical. Define whether to include an intercept or not. Default to TRUE.
ps.order	integer. Order for differences if penalty = "ps".
aniso.angle	numeric. Angle for geometric anisotropy.
aniso.ratio	numeric. Ratio between [0, 1] for geometric anisotropy.
env	environment. Where to search for data if data=NULL.
...	additional arguments. Not required.

**Details**

Note that is.X is only needed if penalty="none". By defining is.X="none" it only define an intercept (if intercept=TRUE), is.X="tps" defines an intercept, coordinate 1, and coordinate 2 as covariates, while is.X="tensor" defines also the interaction coordinate 1\*coordinate 2. See [scp](#).

**Author(s)**

Mario A. Martinez Araya, <r@marioma.me>

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A5. Estimate the model

*Spatial smoothing with unknown changes in the pattern of response*

---

**Description**

Fit a spatial semiparametric model based on splines including unknown changes in the pattern of response.

**Usage**

```
scp(formula, data, initial = NULL, contrasts = NULL,
    model = "exponential", fix.nugget = FALSE, fix.kappa = FALSE,
    nugget.tol = 1e-15, angle = 0, ratio = 1, use.reml = FALSE,
    use.profile = TRUE, chMaxiter = 20, control = list())
```

**Arguments**

formula	formula. An expression to specify the model to fit. See 2. <i>Mean model</i> .
data	sss class object. A dataset object generated by any of the commands <a href="#">as.sss</a> or <a href="#">create.sss</a> .
initial	named list. The starting values for the covariance parameters of the model. If <code>initial=NULL</code> then it is used an internal grid search to define the starting values.
contrasts	character. A contrast method for factor covariates. Default to <code>'contr.treatment'</code> .
model	character. Name of the semivariogram model to estimate for the spatial dependence. See <i>Semivariogram Model</i> .
fix.nugget	logical or numeric. If FALSE the nugget $\tau^2$ is estimated. If <code>fix.nugget</code> is a numeric value then the nugget $\tau^2$ is set to the value defined for <code>fix.nugget</code> .
fix.kappa	logical or numeric vector. If FALSE the parameters $\kappa$ are estimated. If <code>fix.kappa</code> is a numeric vector then $\kappa$ is set to the values of the vector defined for <code>fix.kappa</code> .
nugget.tol	numeric. Threshold for microscale spatial variations to define the nugget effect. Default to $1.0e-15$ . Do not modify unless know what is being doing.
angle	numeric. Angle for geometric anisotropy. Note that this overwrites any specification for <code>aniso.angle</code> in <a href="#">s2D</a> .
ratio	numeric. Ratio between $[0, 1]$ for geometric anisotropy. Note that this overwrites any specification for <code>aniso.ratio</code> in <a href="#">s2D</a> .
use.reml	logical. For using REML estimation set to TRUE, for ML estimation set to FALSE (default).
use.profile	logical. For profiling set to TRUE (default).
chMaxiter	integer. Maximum number of iterations for the loop estimating changes in the pattern of response.
control	named list. Options to control the optimization. See argument <code>control</code> in command <a href="#">optim</a> .

**1. Semiparametric model**

Assume that the response variable admit the trend surface model

$$Y(s) = a^T b + g(s) + \epsilon(s)$$

where  $a$  is a known vector of covariates and  $b$  their coefficients;  $g(s)$  is a deterministic bivariate spline and  $\epsilon(s)$  is a Gaussian spatial process (GSP) with mean zero and covariance depending only on the distance  $h$  and given by  $Cov(\epsilon(s+h), \epsilon(s))$ . This model is also called a *trend surface model*. Given  $n$  observed locations  $s_1, \dots, s_n \in S \subset \mathbb{R}^2$  in a two-dimensional space, then the model is

$$Y = Ab + g + \epsilon$$

where  $Y = (Y(s_1), \dots, Y(s_n))^T$ ,  $A$  is the known matrix of covariates,  $g = (g(s_1), \dots, g(s_n))^T$  and  $\epsilon = (\epsilon(s_1), \dots, \epsilon(s_n))^T$ . The covariance matrix is given by  $Cov(\epsilon, \epsilon) = \Sigma = \sigma^2 R$  with  $R$  a valid correlation matrix. Thus  $Y \sim N_n(\mu, \Sigma)$  where  $\mu = Ab + g$  and the likelihood function is  $L(b, g, \sigma^2, \theta; Y) = (2\pi)^{-n/2} |\Sigma|^{-1/2} \exp\{-\frac{1}{2}(Y - \mu)^T \Sigma^{-1} (Y - \mu)\}$  with  $\theta$  the parameters that define the correlation matrix  $R$ .

## 2. Mean model

It can be defined by the commands:

`linear` that defines the covariates in the matrix  $A$ . Note that more than one `linear` command can be defined. See [linear](#).

`cp` defines changes in the pattern of response by including the covariates  $(z_d - \psi_d^{(0)}) \times 1\{z_d > \psi_d^{(0)}\}$  and  $-1\{z_d > \psi_d^{(0)}\}$  for  $d = 1, \dots, G$  into the matrix  $A$ . Note that more than one `cp` command can be defined. See [cp](#).

`s2D` define the bivariate spline  $g$ . Note that only one `s2D` command can be defined. See [s2D](#).

## 3. Covariance model and nugget effect

Given a distance  $h$  define  $u = \|T_{\text{angle, ratio}}^{1/2} h\| = (h^T T_{\text{angle, ratio}} h)^{1/2} \in \mathfrak{R}$  where  $T_{\text{angle, ratio}}$  is a rotation matrix for geometric anisotropy. The errors are given by the process  $\epsilon(s) = \eta(s) + \xi(s)$  where  $\xi$  is a GSP with mean zero and covariance

$$\begin{aligned} \text{Cov}(\xi(s), \xi(s+h)) &= C_\xi(u; \phi, \kappa) \\ &= \sigma_0^2 \rho_\xi(u; \phi, \kappa) \end{aligned}$$

with  $\rho_\xi(u; \phi, \kappa)$  the correlation function; and  $\eta$  is a nugget effect with covariance

$$\begin{aligned} \text{Cov}(\eta(s), \eta(s+h)) &= C_\eta(u; \tau^2, \text{tol.nugget}) \\ &= \tau^2 \rho_\eta(u; \text{tol.nugget}) \end{aligned}$$

with correlation function  $\rho_\eta(u; \text{tol.nugget}) = 1\{u < \text{tol.nugget}\}$ . Therefore the covariance of the process  $\epsilon$  is given by

$$\begin{aligned} \text{Cov}(\epsilon(s), \epsilon(s+h)) &= C_\epsilon(u; \sigma^2, \theta, \text{tol.nugget}) \\ &= \sigma^2 \rho_\epsilon(u; \theta, \text{tol.nugget}) \end{aligned}$$

with correlation function given by

$$\rho_\epsilon(u; \theta, \text{tol.nugget}) = (1 - \rho_*) \rho_\eta(u; \text{tol.nugget}) + \rho_* \rho_\xi(u; \phi, \kappa)$$

where  $\theta = (\rho_*, \phi, \kappa)^T$  are the parameters with  $\rho_* = \sigma_0^2 / \sigma^2$ ,  $\sigma^2 = \tau^2 + \sigma_0^2$ , and `tol.nugget` is the argument that controls the largest distance at which micro-scale variations can affect the observed outcome. By default `tol.nugget` is set to  $1.0e-15$ . The parameters  $\phi, \kappa$  define the correlation function of the process  $\xi$  with  $\phi$  usually called the *range parameter* and  $\kappa$  depending on the model selected. The semivariogram can be expressed as

$$\gamma_\epsilon(u; \sigma^2, \theta, \text{tol.nugget}) = \sigma^2(1 - \rho_\epsilon(u; \theta, \text{tol.nugget}))$$

where  $\tau^2$  is the nugget effect,  $\sigma^2$  is the sill, and  $\sigma_0^2$  is the partial sill. Note that when `angle = 0` and `ratio = 1` the matrix  $T_{\text{angle, ratio}}$  is an identity matrix and  $u = h$  so the correlation  $\rho_\epsilon(u; \theta, \text{tol.nugget})$  is isotropic. Use different values for `angle` and `ratio` to define a geometric anisotropic correlation function. Then the covariance matrix  $\Sigma = \sigma^2 R$  where  $R$  is the correlation matrix originated from  $\rho_\epsilon(u; \theta, \text{tol.nugget})$ . It is possible to define the argument `model=name` where `name` is one of the following: ‘matern’, ‘powered.exponential’, ‘spherical’, ‘wave’, ‘exponential’, ‘gaussian’, ‘cubic’, ‘circular’, ‘gencauchy’, ‘cauchy’, ‘RMmatern’, ‘RMwhittle’, ‘RMgneiting’, and ‘RMnugget’. For `.semiVar` one of ‘matern’, ‘gaussian’, ‘exponential’, ‘power’, ‘cubic’, ‘penta.spherical’, ‘spherical’, ‘wave’, ‘sin.hole’, ‘pure.nugget’ and ‘identity’. By default the covariance model is set to ‘exponential’ with `angle=0` and `ratio=1`.



#### 4. Penalized maximum likelihood estimation

Estimation can be performed by maximisation with respect to  $b, g, \sigma^2, \theta$ , and  $\alpha$  of the penalized log likelihood

$$\ell_p(b, g, \sigma^2, \theta, \alpha) = \log(L(b, g, \sigma^2, \theta; Y)) - \frac{1}{2\sigma^2} J_\alpha(g)$$

where  $J_\alpha(g) = g^T Q_\alpha g$  is the penalty and  $Q_\alpha$  is the roughness matrix.

#### 5. Penalties

Depending on the type of spline assumed for  $g$  the penalty is defined differently depending on the roughness matrix  $Q_\alpha$  which is given by:

**Tensor product spline.** Given  $\tau_{1,1}, \dots, \tau_{1,K_1}$  and  $\tau_{2,1}, \dots, \tau_{2,K_2}$  the design points in each coordinate then

$$Q_\alpha = \alpha_1 I_{K_2} \otimes Q_1 + \alpha_2 Q_2 \otimes I_{K_1}$$

where  $Q_1, Q_2$  are unidimensional roughness matrices from the design points in each coordinate and  $\alpha_1, \alpha_2$  are smoothing parameters in each direction.

**Thin plate spline.** Given the  $n$  locations,  $Q_\alpha = \alpha E$  where  $\alpha$  is the smoothing parameter and the  $n \times n$  matrix  $E$  has elements  $E_{i,j} = \vartheta(|s_i - s_j|)$  for  $i, j = 1, \dots, n$  where

$$\vartheta(u) = \begin{cases} \frac{1}{16\pi} \times u^2 \log(u^2) & , u > 0 \\ 0 & , \text{otherwise.} \end{cases}$$

#### 6. Mixed model representation

The spline can be written as  $g = X\beta + Zr$  with  $\beta$  and  $r$  the coefficients and  $X$  and  $Z$  design matrices conveniently defined. Then for the observed responses the model can be expressed as a the mixed model

$$Y = Ab + X\beta + Zr + \epsilon$$

where  $r \sim Normal(0, I_V)$  with  $V$  the number of columns in  $Z$ . Then,  $Y \sim N_n(\mu_m, \Sigma)$  where  $\mu_m = Ab + X\beta$  and  $\Sigma = \sigma^2 R$ ; and  $Y|r \sim N_n(\mu, V)$  where  $\mu = Ab + X\beta + Zr$  and  $V = ZZ^T + \Sigma$ . Let us denote  $\vartheta = (b, \beta, \sigma^2, \theta, \alpha)^T$ , then the conditional log-likelihood of the model is given by

$$\ell(\vartheta|r) \propto -\frac{1}{2} \{ \log |\Sigma| + (Y - \mu)^T \Sigma^{-1} (Y - \mu) \}$$

and the marginal log-likelihood is given by

$$\ell(\vartheta) \propto -\frac{1}{2} \{ \log |V| + (Y - Ab - X\beta)^T V^{-1} (Y - Ab - X\beta) \}.$$

#### Author(s)

Mario A. Martinez Araya, <r@marioma.me>

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A6. Obtain approximation

*Linear approximation to a spline.*

---

### Description

Approximation to a spatial semiparametric model based on a bivariate spline.

### Usage

```
## S4 method for signature 'sssFit'
scpApproximate(object, tol)
```

### Arguments

object	an object of class <code>sssFit</code> from command <code>scp</code> .
tol	numeric. Numeric tolerance to use for some inversion of matrices. Default to <code>.Machine\$double.neg.eps*1.0e-10</code> .

### Details

`scpApproximate` compute an approximation to the spatial semiparametric model obtained from `scp`. This command update the fitted values and fitted spline in the input object of class `sssFit`. Then we can use the command `plot` for plotting the approximated semiparametric model.

### Value

This command return an object of class `sssFit`.

### Author(s)

Mario A. Martinez Araya, <r@marioma.me>

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B1. Testing surface    *Testing the surface model*

---

### Description

Test the model for the surface of response. The null hypothesis is assumed as a linear model defined by the coordinates while the alternative hypothesis is assumed a bivariate spline (tensor product or thin-plate spline).

### Usage

```
## S4 method for signature 'sssFit'
testSurface(object, tol)
```

**Arguments**

object	an object of class <code>sssFit</code> from command <code>scp</code> .
tol	numeric. Numeric tolerance to use for some inversion of matrices. Default to <code>.Machine\$double.neg.eps*1.0e-10</code> .

**Details**

If we have defined a bivariate spline using `s2D` in the formula of `scp` then the model is an spatial semiparametric model based on splines (tensor products or thin-plate splines). In this case `testSurface` performs a test for the null hypothesis  $H_0 : g = X\beta$  (linear model) against the alternative  $H_1 : g = X\beta + Zr$  (spline model). When  $g$  is assumed as a thin-plate spline then this test is equivalent to test the null hypothesis  $H_0 : \text{the pattern of response in the space is a plane}$  against the alternative  $H_1 : \text{the pattern of response in the space is a bivariate thin-plate spline}$ . In one dimension this test is equivalent to a test for linearity in the pattern of response.

**Value**

Returns a table with the degrees of freedom, sum of squares and mean squares from different sources and the F test and its associated p-value.

**Author(s)**

Mario A. Martinez Araya, <r@marioma.me>

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B2. Plotting

*Plot observed, fitted values or estimated spline from scp object.*

---

**Description**

Draw an image, perspective or levelplot of the observed, fitted values or estimated bivariate spline from the elements in a `scp` object.

**Usage**

```
## S4 method for signature 'sssFit,missing'
plot(x, what, type, which, col.args, col.contour,
     level.at, border, theta, phi, shade, ...)
```

**Arguments**

x	<code>sssFit</code> object from <code>scp</code> .
what	character. What to plot? One of 'obs' (for observed responses), 'fit' (for fitted values, the default) or 'g' (for the estimated bivariate spline).
type	character. Which type of plot? One of 'image' (the default), 'levelplot', 'persp' or 'persp3d'.

<code>which</code>	character. Which color pattern? One of <code>'colorRampPalette'</code> (default), <code>'colorRamp'</code> , <code>'rainbow'</code> , <code>'heat.colors'</code> , <code>'terrain.colors'</code> , <code>'topo.colors'</code> , or <code>'cm.colors'</code> .
<code>col.args</code>	named list. List with argument to pass to the color pattern function defined by <code>which</code> . See <a href="#">colorRampPalette</a> , <a href="#">colorRamp</a> , <a href="#">rainbow</a> , <a href="#">heat.colors</a> , <code>'terrain.colors'</code> , <code>'topo.colors'</code> , and <code>'cm.colors'</code> .
<code>col.contour</code>	character. Only for <code>type="image"</code> . Color for the contours.
<code>level.at</code>	character or numeric vector. Only for <code>type="levelplot"</code> . Where to draw the levels at. If character, it is the name of the function to compute where to put the levels.
<code>border</code>	character. Color of the border.
<code>theta, phi, shade</code>	numeric. See <a href="#">persp</a> or <a href="#">persp3d</a> .
<code>...</code>	other arguments for <a href="#">levelplot</a> , <a href="#">image</a> , <a href="#">persp</a> or <a href="#">persp3d</a> .

**Author(s)**

Mario A. Martinez Araya, <r@marioma.me>

---

B3. Summary

*Summary of the estimated model from scp object.*

---

**Description**

Report estimated coefficients, standard errors and t-tests for parametric effects of the semiparametric model from a scp object.

**Usage**

```
## S4 method for signature 'sssFit'
summary(object, alpha=0.05)
```

**Arguments**

<code>object</code>	sssFit object from <a href="#">scp</a> .
<code>alpha</code>	numeric [0, 1]. The level for confidence intervals.

**Author(s)**

Mario A. Martinez Araya, <r@marioma.me>

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 B4. Information criterion

*Information criterion of the estimated model from scp object.*

---

**Description**

Return the information criterion of the estimated model from a scp object.

**Usage**

```
## S4 method for signature 'sssFit'
AIC(object, k, only.criterion)
## S4 method for signature 'sssFit'
BIC(object, only.criterion)
## S4 method for signature 'sssFit'
AICm(object, k, only.criterion)
## S4 method for signature 'sssFit'
AICc(object, k, only.criterion)
## S4 method for signature 'sssFit'
BICc(object, only.criterion)
## S4 method for signature 'sssFit'
BICj(object, k, tol, only.criterion)
## S4 method for signature 'sssFit'
GIC(object, k, only.criterion)
## S4 method for signature 'sssFit'
GIChq(object, k, only.criterion)
## S4 method for signature 'sssFit'
GICpn(object, only.criterion)
## S4 method for signature 'sssFit'
GICb(object, only.criterion)
```

**Arguments**

object	sssFit object from <a href="#">scp</a> .
k	numeric. Factor multiplying the number of parameters in each criterion. Default to k=2.
tol	numeric. Value for the tolerance in some computation of inverse matrices. By default is set to <code>.Machine\$double.neg.eps</code> .
only.criterion	logical. If TRUE (the default) returns only the value of the criterion.

**Details**

The information criterion for a mixed model is defined as

$$IC = -2\ell + \text{penalty}$$

where  $\ell$  is the log-likelihood  $\ell(\vartheta)$  or conditional log-likelihood  $\ell(\vartheta|r)$  (see [scp](#)). The penalty is expressed as  $k \times a_0 \times \omega_{\mu_*,V}$  where  $\omega_{\mu_*,V} = \omega_{\mu_*} + \omega_V$  is the (effective) number of parameters in the mean and variance and  $k$  and  $a_0$  are factors that depend on the criterion used. Thus the information criterion can be written as

$$IC = -2\ell + k \times a_0 \times \omega_{\mu_*,V}.$$

Note that  $\mu_*$  depends on the criterion being used so it can be  $\mu_* = \mu_m$  or  $\mu_* = \mu$ . See [scp](#).

### Value

If only `.criterion=TRUE` returns the value of the criterion. If only `.criterion=FALSE` returns a list with the following elements:

**logLik** numeric. The log-likelihood or conditional log-likelihood (given  $r$ ) of the model depending of the criterion used.

**criterion** numeric. The value of the information criterion.

**ka0** numeric. Factors  $ka_0$  multiplying the number of parameters. Depends on the criterion selected.

**numpar** numeric. The (effective) number of parameters. Depends on the criterion selected.

**penalty** numeric. The value of the penalty.

### Author(s)

Mario A. Martinez Araya, <r@mariona.me>

### References

- Mueller, Samuel; Scaely, J. L. and Welsh, A. H. (2013) Model Selection in Linear Mixed Models. *Statist. Sci.* **28**, no. 2, 135–167. doi:10.1214/12-STS410. <http://projecteuclid.org/euclid.ss/1369147909>.

---

B5. Variogram

*Compute and plot the semi-variogram from scp object.*

---

### Description

Compute and plot the semi-variogram of the semiparametric model from a scp object.

### Usage

```
## S4 method for signature 'sssFit'
Variogram(object, distance, plot, ...)
```

**Arguments**

object	sssFit object from <a href="#">scp</a> .
distance	numeric vector. The distances at which to compute the semi-variogram. By default is set to NULL.
plot	logical. plot=TRUE (the default) produce the semivariogram plot. plot=FALSE returns the values of the semivariogram at distance. See <i>value</i> .
...	other graphical parameters to pass.

**Author(s)**

Mario A. Martinez Araya, <r@marioma.me>

---

landim1	<i>geoR's landim1 dataset</i>
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---

**Description**

Dataset originally from geoR package. Dataframe with 38 locations with information related to easting (EW), northing (NS), and two generic numeric variables (A and B).

**Usage**

```
data("landim1")
```

**Format**

The format is: chr "landim1"

**Details**

Run `str(landim1)`, `data(landim1)` or `summary(landim1)` to see more details about the dataset.

**Source**

geoR package <https://CRAN.r-project.org/package=geoR>.

---

`sss-class`*Class "sss"*

---

### Description

Create a dataset for spatial smoothing splines. Those dataset can be used later by functions [s2D](#) for tensor product (natural) cubic splines or p-splines, and [scp](#) for estimating spatial smoothing splines models.

### Usage

```
sss(...)
```

### Arguments

... Slots elements to be included into the sss dataset. Allowed slots names are `data`, `coords`, `grid`, `knots`, `W`, `contract` (to be discarded in the future), and `regular`.

### Objects from the Class

Objects can be created by calls of the form `sss(...)`.

### Slots

**data** a data-frame containing the variables measured at the locations given by `coords`.

**coords** a matrix containing the two columns of observed coordinates for the data.

**grid** a grid matrix containing the two columns of coordinates.

**knots** a named list with the design points (knots) in every coordinate. Equivalent to a `grid.list` object.

**W** a spatial incidence matrix. If `contract=TRUE` it is  $W_{ij}$ , otherwise  $W_{ji}$ .

**contract** logical. The same value as the argument `contract`.

**regular** logical. If the coordinates are observed at regular points it is TRUE, FALSE otherwise (missing coordinates in any direction).

### Author(s)

Mario A. Martinez Araya, <r@marioma.me>



---

sssFit-class	Class "sssFit"
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---

**Description**

Output object from `scp` that can be used with methods for post-processing.

**Usage**

```
sssFit(...)
```

**Arguments**

... Slots elements to be included into the `sssFit` object. Allowed slots names are `data`, `zV`, `XL`, `XC`, `XF`, `XS`, `fit`, and `call`.

**Objects from the Class**

Objects of this class are created by calls to the command `scp` (see [scp](#)). It is also possible to define an empty object of this class by calls of the form `sssFit(name)` however for further use this is subject to validity of the object.

**Slots**

**data** an object of `sss` class containing the input data.

**zV** numeric vector. Response variables measured at the locations given by `data@coords`.

**XL** a named list with elements and covariates from `linear` command.

**XC** a named list with elements and covariates from `cp` command.

**XF** not implemented.

**XS** a named list with elements from `s2D` command.

**fit** a named list with different estimated parameters and summaries from the estimated model.

**call** call to the fitted model.

**Author(s)**

Mario A. Martinez Araya, <[r@marioma.me](mailto:r@marioma.me)>

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